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# SYMPHYS-9

IX International Conference on

## Symmetry Methods in Physics

Yerevan, Armenia 2001

Joint Institute for Nuclear Research & Yerevan State University

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IX INTERNATIONAL

CONFERENCE ON

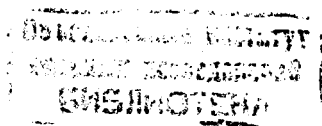
SYMMETRY METHODS

IN PHYSICS

*The Conference takes place in the year of celebration  
of the 1700-th anniversary of adoption of Christianity in Armenia*

Yerevan, Armenia, July 3 - 8, 2001

C 323 + C 324 + C 322



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# GENERAL INFORMATION

## Location

The Conference will be held at the *Physics Department of Yerevan State University* from July 3 to July 8, 2001.

The Conference opens on July 3 at 10.00 in the Conference Hall of the Physics Department of Yerevan State University.

## Proceedings

All contributions will be reviewed but only a limited number will be selected for the Proceedings. The deadline for submission of talks is October 31, 2001 however, to assure swift publication, we encourage the participants to submit their manuscripts already during the conference. For any information concerning publication please contact by

e-mail: symphys9@icas.ysu.ar

Submitted materials must be in English. Please use LaTeX format 12pt, 150x220mm. Size restrictions: for 45 min. and 30 min. talks - 15 and - 12 pages, for 20 min. contributions - 10 pages, for poster session - 6 pages.

## Special Events

- **Monday, July 3**

Welcome Party will be held in Yerevan State University (20:00 - 22:30). (For accompanying persons 10 US\$)

- **Wednesday, July 4**

Trip to Sevan lake with barbecue. (For accompanying persons 25 US\$)

- **Saturday, July 7**

The Conference Banquet (20:00-23:00). (For accompanying persons 20 US\$).

## Accompanying Program

- **Tuesday, July 3:**

A tour round the town, a visit of the museum of ancient manuscripts. The price is 10\$US.

- **Thursday, July 5 :**

A tour to Etchmiadzin, Picture Gallery. The price is 10 US\$.

- **Friday, July 6:**

A tour to Garni and Gegard. The price is 15 US\$.

## Transportation to the Airport

In Yerevan airport "Zvartnoz" all participants will be met by the representatives of the Organizing Committee carrying the label **SYMPHYS-9**.

From the airport there is also a regular bus service (bus N 107) to the University Hostel or metro "Yeritasardakan".

The Organizing Committee can be contacted from the airport by telephone 570-370.

# ABSTRACTS



# Invited Talks

## Applications of Classical and Quantum Algebras to Molecular Thermodynamics

*M. Angelova*

*School of Computing and Mathematics, University of Northumbria, Newcastle upon Tyne, England, GB-NE1 8ST*

Lie-algebraic and quantum-algebraic techniques are used in the analysis of thermodynamic properties of molecules and solids. The local anharmonic effects are described by a Morse-like potential associated with the  $SU(2)$  algebra. A vibrational high-temperature partition function and the related thermodynamic potentials are derived in terms of the parameters of the model. Symmetry-adapted wave functions, related to the local symmetry of the atoms, are used to analyze vibrational energies in molecules and crystals. Quantum analogues of anharmonic bosons,  $q$ -bosons, are introduced and used to describe anharmonic and superfluid properties of molecules and solids. A new algebraic realization of the  $q$ -bosons, for the case of  $q$  being a root of unity is given. This realization represents the symmetry of a linear lattice with periodic boundary conditions.

## Quantum Conformal Equations and Their Solutions

*V. Dobrev*

*Bulgarian Academy of Sciences (Sofia, Bulgaria) and University of Northumbria (Newcastle, UK)*

We consider hierarchies of  $q$ -deformed equations which are quantum conformal invariant. We construct explicit solutions of these equations. The solutions are given in terms of two new  $q$ -deformations of the plane wave written in conjugated bases. We consider in more detail the solutions of the quantum conformal deformations of the Maxwell and potential equations. Compatibility of the equations leads to an asymmetry between the  $q$ -deformations of the fixed helicity constituents of the Maxwell field. This asymmetry and possible alternatives are discussed.

## Novel Applications of Group Theory in Nuclear Physics

*J. Draayer, A. Georgieva<sup>3</sup>, K. Sviracheva<sup>1</sup>,  
Feng Pan<sup>2</sup>*

<sup>1</sup> *Louisiana State University, Department of Physics and Astronomy, Baton Rouge, Louisiana, 70808-4001 USA*

<sup>2</sup> *Department of Physics, Liaoning Normal University, Dalian 116029, P. R. China*

<sup>3</sup> *Institute of Nuclear Research and Nuclear Energy, Bulgarian Academy of Sciences, Sofia 1784, Bulgaria*

While large-scale shell-model calculations may prove useful for reproducing experimental data, insight into the physical underpinnings of many-body quantum phenomena, such as the structure of atomic nuclei, requires a deeper understanding of the underlying principles that can only be achieved through a study of the symmetry or near-symmetry properties of a system. We will review some standard as well as novel algebraic methods, including use of the Bethe ansatz and quantum groups, that have been used to explore special features of atomic nuclei: pairing correlations, quadrupole collectivity, scissors modes, etc. In each case the underlying physics will be linked to a symmetry of the system and its group theoretical representation.

## Superintegrability for Curved Spaces in Two Dimensions.

*E. Kalnins<sup>2</sup>, J. Kress<sup>2</sup> and P. Winternitz<sup>1</sup>*

<sup>1</sup> *CRM, Universite de Montreal, C.P.6128, Montreal, Quebec, Canada*

<sup>2</sup> *Mathematics department, University of Waikato, Hamilton, New Zealand.*

Building on already known completeness results [1] about quadratic superintegrability for constant curvature spaces in two dimensions we indicate how it is possible to make a complete discussion of the superintegrability property for general curved spaces in two dimensions. This is done by making use of a note given in Volume 4 of Darboux's treatise on the theory of surfaces written by G.M.Koenigs. From this note we are able to start to make a comprehensive account of Superintegrability in two dimensions and indicate the mechanism by which this is achieved.

[1] E.G.Kalnins, J.M.Kress, G.S.Pogosyan, W.Miller Jr., Completeness of superintegrability in two-dimensional constant-curvature spaces, J. Phys. A: Math. Gen. 34(2001), 1-16.

## Invariant Variational Principles and Moving Frames

*P. J. Olver*

*School of Mathematics, University of Minnesota,  
Minneapolis, MN, USA 55455*

It has been known, since Lie, that any group-invariant variational problem can be expressed in terms of differential invariants. A similar result holds for the Euler-Lagrange equations. However, until now, except in a handful of particular cases, the general formula that enables one to go directly from the differential invariant form of the variational problem to that of its Euler-Lagrange equations has remained elusive. In this talk I will outline a complete solution to this problem, based on the new equivariant theory of moving frames. Additional applications to the classification of differential invariants, invariant differential operators, and their syzygies (identities) will be presented during the talk.

## Superintegrability, Multiseparability and Exact Solvability in Quantum Mechanics.

*P. Winternitz*

*CRM, Université de Montréal, C.P.6128, Montréal,  
Québec, Canada*

Superintegrable systems are defined by the fact that they allow more integrals of motion than degrees of freedom. Exactly solvable systems are defined by the fact that their energy spectrum can be calculated algebraically. Multiseparable systems allow the separation of variables in more than one coordinate system. We show that that at least in two dimensional Euclidean space all known superintegrable systems are also exactly solvable. The reason is that after an appropriate gauge transformation the corresponding Hamiltonians lie in the enveloping algebra of a parabolic subalgebra of  $sl(3, R)$ .

## 1. Integrable and Superintegrable Systems (ISS)

### Algebraic Structures Associated to Nambu Dynamics

*S. Codrinsky*

*Departamento de Matemáticas y Física, Instituto  
Pedagógico de Caracas, Av Paez, Caracas, Venezuela*

The role played by Grassmann and Clifford algebras in the description of the Nambu dynamical system is explored. Phase space has dimension  $3N$ , the dynamical system is considered to be described by  $N$  triplets; functions over phase space are elements of the Clifford algebra with coefficients that are functions over  $R^{3N}$ . The algebra within a particular triplet is the ordinary exterior algebra while the algebra of triplets is the Clifford one.

### On the Inintegrable Mass Deformed Calogero-Moser-Sutherland Type Hamiltonians

*A. Khvedelidze, D. Mladenov*

*Joint Institute for Nuclear Research, Dubna, Russia*

The geodesic motion on the  $GL^+(n, R)$  group manifold endowed with the bi-invariant metric is studied using the polar decomposition of group elements. Owing to the action of  $SO(n, R)$  isometry group the quotient space  $GL^+(n, R)/SO(n, R)$  is stratified manifold and this geometric peculiarity leads to the dynamical consequences. It is shown that in the case of the *Principal orbit* stratum the dynamics is governed by the generalized Calogero-Moser-Sutherland Hamiltonian with two internal "spin" variables, while for the *Singular orbit* the derived Hamiltonian describes certain integrable deformation of the Calogero-Moser-Sutherland type model, when particles have a non-equal masses. The deformation parameters (ratios of masses) are not arbitrary, they depend on the isotropy group of a given singular stratum and are characterized by the partition of the  $GL(n, R)$  group dimension.

## 2. Contractions of Lie Groups and Quantum Groups (CLGQG)

### Contraction of the Finite Oscillator

*N. Atakishiev<sup>1</sup>, G. Pogosyan<sup>2</sup> and K.B. Wolf*

<sup>1</sup> UNAM, Apardo Postal 273-3 62210 Cuernavaca, Mexico

<sup>2</sup> JINR, Dubna, 141980, Moscow Reg., Russia

<sup>3</sup> Centro de Ciencias Fisicas, Universidad Nacional Autonoma de Mexico

The finite oscillator model has the dynamical algebra  $u(2)$ , consisting of position, momentum and mode number, with a finite number of values. We examine the contraction of this model to the ordinary quantum oscillator as the number and density of points increases. This is done on the level of the algebra, of the wavefunctions, and of the fractional Fourier-Kravchuk transform.

### Continuum Canonical Transforms as Inductive Limits of Discrete Canonical Transforms

*L. Barker*

Department of Mathematics, Bilkent University, 06533 Bilkent, Ankara, Turkey

E-mail: barker@fen.bilkent.edu.tr

Phase space: the motion group  $E(2)$  is a "contraction" of  $SO(3)$ . A refinement for configuration space: the  $L^2(R)$  representation of the Heisenberg-Weyl motion group  $EHW(2)$  (described by the fractional Fourier transform and the Heisenberg-Weyl translates) is an *inductive* (to be explained) limit of finite-dimensional representations of  $U(2)$ . How might we "discretize" the other affine canonical transforms on  $L^2(R)$ ? How might we "discretize" toroidal configuration spaces? What continuum scenario might be "discretized" by  $SL(2, Z/p^n)$ ? These questions (arising in quantum physics, optics, signal analysis) can be clarified by casting them as questions about inductive limits of representations.

### Lie Algebra Contractions and Separation of Variables on $n$ -Sphere. Interbases Expansions

*A. Izmet'ev<sup>1</sup>, G. Pogosyan<sup>1</sup>, A. Sissakian<sup>1</sup>, and P. Winternitz<sup>2</sup>*

<sup>1</sup> JINR, Dubna, 141980, Moscow Reg., Russia

<sup>2</sup> CRM, Universite de Montreal, C.P.6128, Montreal, Quebec, Canada

Lie algebra contractions from  $o(n+1)$  to  $e(n)$  are used to obtain asymptotic limits of interbases expansions between bases corresponding to different subgroup chains for the group  $O(n+1)$ . The contractions

lead to interbases expansions for different subgroup chains of the Euclidean group  $E(n)$ . They provide asymptotic formulae for quantities such as Wigner rotation matrices, Clebsch-Gordan coefficients and Racah coefficients.

### Contractions of Quantum Groups and Quantum Vector Spaces

*N. Gromov, I. Kostyakov, V. Kuratov*

Syktvykar Branch of IMM, Syktvykar, Russia

Contractions of quantum orthogonal groups are studied unlike of Wigner-Inonu in a pure algebraic way with the help of Pimenov algebra  $D(\iota)$ . Namely, the groups under consideration are regarded as an algebra of noncommutative functions but with nilpotent commutative generators. Possible contractions are essentially depended on the choice of primitive elements of Hopf algebra structure of quantum orthogonal group. All such choices are considered for quantum group  $SO_q(N)$  and all allowed contractions in Cayley-Klein scheme are obtained. The quantum vector spaces corresponding to the appropriate contracted quantum group are described explicitly both in cartesian and symplectic generators. Quantum deformations of 1+3 kinematical spaces and groups are regarded as an illustration of the general theory.

### Contractions of Superalgebras $Osp(M/2N)$

*N. Gromov, I. Kostyakov, V. Kuratov*

Syktvykar Branch of IMM, Syktvykar, Russia

We describe how dual numbers technique can be applied to the study of superalgebra contractions. A wide class of Cayley-Klein superalgebras are obtained by this method.



### 3. Algebraic Structures Beyond Lie Algebras (ASBLA)

#### Quantum Motion Algebras

A. Góźdz, M. Miśkiewicz, M. Pietrow

*Institute of Physics, University of Maria Curie-Skłodowska, pl. M. Skłodowskiej-Curie 1, 20-031 Lublin, Poland*

The notion of the groups of motions as the groups of elementary changes of quantum states leads to the Quantum Motion Algebras consisted of the formal sums and "integrals" of the group elements (A. Góźdz: Quantum Motion and Algebraic Generator Coordinate Method, *Symmetries in Science VII*, ed. B. Gruber and T. Otsuka, Plenum Press, 1993). These algebras can be considered as a tool for the quantum many-body problems - especially for the quantum collective motions in the molecular, atomic and nuclear physics. In this sense the formalism is an algebraic generalization of the well known Generator Coordinate Method. In addition, the algebras can be used for constructing of the state spaces for more fundamental physical problems related to principles of quantum mechanics. The last possibility allows to think about some natural modifications of quantum mechanics.

#### Triality Structure of Exceptional Lie Algebras

Z. Silagadze

*Budker Institute of Nuclear Physics, 630 090 Novosibirsk, Russia*

Recently Ramond revealed a remarkable group-theoretical structure behind eleven dimensional supergravity multiplet: it was shown that the supergravity triplet of massless fields stems from the three equivalent ways to embed  $SO(9)$  into  $F_4$  exceptional Lie algebra. In fact  $F_4$  is just an union of these three different copies of  $SO(9)$ , their intersection being  $SO(8)$ , with  $SO(8)$  triality and octonions playing the central role in this construction. We show that the similar simple triality structure holds also for  $E$ -type exceptional Lie algebras.

### 4. Quantum Algebras and Groups, Q-special Functions (QAGQF)

#### Deformations of the Boson and Fermion Representations of $sp(4)$ and $sp(4, R)$

J. Draayer<sup>2</sup>, M. Ivanov<sup>1</sup>, A. Georgieva<sup>1</sup>,  
K. Sviratcheva<sup>2</sup>

<sup>1</sup> *Institute of Nuclear Research and Nuclear Energy, Bulgarian Academy of Sciences, Sofia 1784, Bulgaria* <sup>2</sup> *Louisiana State University, Department of Physics and Astronomy, Baton Rouge, Louisiana, 70808-4001 USA*

With a view towards future applications in nuclear physics, the boson and fermion realization of the compact  $sp(4)$  and noncompact  $sp(4, R)$  and their  $q$ -deformed versions are investigated and compared. The deformed realizations are based on distinct deformations of the boson and fermion creation and annihilation operators. In the boson case there is a simple transformation of the "classical" bosons to  $q$ -deformed ones. In the fermion case an additional index is introduced in order to satisfy the Pauli principle and in this case a simple transformation function between the "classical" and  $q$ -deformed operators is not known. Three important reduction chains of these algebras are explored in both the classical and deformed cases.

For the primary reduction, the  $su(2)$  sub-structure can be interpreted in both cases as a pseudospin algebra. The other two reductions in the fermion case are  $su(2)$  algebras, associated with pairing between identical fermions or coupling of two fermion of different kinds. In the boson case the infinite deformed ladder series  $u_q^0(1, 1)$  and two infinite deformed discrete series  $u_q^\pm(1, 1)$  are obtained. Each reduction provides for a complete classification of the basis states. In the boson case the initial as well as the deformed representations act in the same Fock space, but the deformation in the fermion case leads to basis states whose content is very different from the classical one. In a Hamiltonian theory this implies a dependance of the matrix elements on the deformation parameter, leading to the possibility of greater flexibility and richer structures within the framework of  $q$ -deformed algebraic descriptions

#### Noncommutative Instantons on the 4-sphere from Quantum Groups

M. Tarlini

*I.N.F.N. Sez. Firenze and Dip. of Physics, Univ. of Firenze Italy*

We describe an approach to the noncommutative instantons on the 4-sphere based on quantum group

theory. We quantize the Hopf bundle  $S^7 \rightarrow S^4$  making use of the concept of quantum coisotropic subgroups. The analysis of the semiclassical Poisson-Lie structure of  $U(4)$  shows that the diagonal  $SU(2)$  must be conjugated to be properly quantized. The quantum coisotropic subgroup we obtain is the standard  $SU_q(2)$ ; it determines a new deformation of the 4-sphere  $\Sigma_q^4$  as the algebra of coinvariants in  $S_q^7$ . We show that the quantum vector bundle associated to the fundamental corepresentation of  $SU_q(2)$  is finitely generated and projective and we compute the explicit projector. We give the unitary representations of  $\Sigma_q^4$  and we study the Chern-Connes pairing of the projector. It comes out that even the zero class in cyclic homology is non trivial.

## 5. Periodic and Aperiodic Structures (PAS)

### Wave Functions for Erods with Periodic Structures

*J. Valdes*

*Centro de Ciencias Fisicas, Universidad Nacional Autonoma de Mexico, Apartado Postal 48-3, 62251*

We obtain, both from the theoretical and experimental points of view, the wave functions of longitudinal, bending and torsional modes of elastic rods with an increasing number of obstacles arranged in different ways. The wave functions and their related frequencies are calculated using the transfer matrix method and they are measured experimentally using a new detector based on eddy currents, which is not in contact with the rod. Experimental values agree very well with the theoretical ones.

### Aperiodic Pseudorandom Number Generators

*J. Patera<sup>1</sup>, J. Patera<sup>2</sup>, L.-S. Guimond*

<sup>1</sup> *Dept. of Maths, Faculty of Nuclear Science and Physical Engineering, Czech Technical University, Trojanova 13, 120 00, Praha 2, Czech Republic*

<sup>2</sup> *Centre de recherches mathématiques, Université de Montréal, Montréal H3C 3J7, Québec, Canada*

We discuss the use of aperiodic point sets called quasicrystals in designing deterministic aperiodic pseudorandom number generators. The proposed scheme uses quasicrystals to combine two or three periodic number sequences. We prove that there exists an infinite class of quasicrystals for which the combination scheme (using any nontrivial periodic sequences) produces pseudorandom sequences having no lattice structure. We give empirical results when quasicrystals are used to combine linear congruential generators. Finally, we describe the implementation of two methods for generating quasicrystal points and discuss their respective computational complexities.

### Recurrence Times in Dynamical Systems via Quasicrystal Techniques

*R. Twarock*

*Department of Mathematics, City University Northampton Square, London EC1V 0HB, England*

It is shown that techniques developed in the framework of cut-and-project quasicrystals can be used to derive information about recurrence times for Dynamical systems. Based on this, an alternative proof of results by Florek and Slater as well as Mayer and Lohoefer is deduced. The possibility to derive a generalization of their results to higher dimensions based on the cut-and-project approach is discussed.

## 6. Quantum Field Theory and Strings (QFTS)

### The Diagonal Ghost Equation Ward Identity for Yang-Mills Theories in the Maximal Abelian Gauge

*R. Fazio*

*Dipartimento di Fisica- Statale di Milano*

A BRST perturbative analysis of  $SU(N)$  Yang-Mills theory in a class of maximal Abelian gauges is presented. We point out the existence of a new non-integrated renormalizable Ward identity which allows to control the dependence of the theory from the diagonal ghosts. This identity, called the diagonal ghost equation, plays a crucial role for the stability of the model under radiative corrections implying, in particular, the vanishing of the anomalous dimension of the diagonal ghosts. Moreover, the Ward identity corresponding to the Abelian Cartan subgroup is easily derived from the diagonal ghost equation. Finally, a simple proof of the fact that the beta function of the gauge coupling can be obtained from the vacuum polarization tensor with diagonal gauge fields as external legs is given. A possible mechanism for the decoupling of the diagonal ghosts at low energy is also suggested.

### The Dual Gauge Model Symmetry and a Confinement of Test Charges

*G. Kozlov*

*Bogoliubov Laboratory of Theoretical Physics,  
Joint Institute for Nuclear Research,  
141980 Dubna, Russia*

We reformulate the dual gauge model of the long-distance Yang-Mills theory in terms of two-point Wightman functions with the equations of motion involving higher derivatives. In the flux-tube scheme of monopole condensation, the analytic expressions of both monopole and dual gauge boson fields propagators are obtained. In the system of the test color charges an analytic expression for the string tension is derived.

### Casimir Effect on Background of the Rindler Spacetime

*R. Avagyan, A. Saharian, A. Yeranyan*

*Department of Physics, Yerevan State University,  
375025 Yerevan, Armenia*

The Casimir effect is investigated for the standard geometry of two parallel plates moving with a constant proper acceleration through the Rindler-Fulling vacuum. The both cases of a scalar (with

Dirichlet and Neumann boundary conditions) and electromagnetic fields are considered. The regularization procedure for the vacuum expectation values of the energy-momentum tensor is based on a variant of the Generalized Abel-Plana formula. Expressions are derived for the vacuum energy density and effective pressures in the region between the plates. The various asymptotic cases are considered. The results of the numerical evaluation are presented for the interaction force between the plates due to the vacuum fluctuations.

## 7. Gravitation, Cosmology, Quantum Gravity (GCQG)

### New Insights in Particle Dynamics from Group Cohomology

V. Aldaya, J.L. Jaramillo, J. Guerrero

*Institutop de Astrofísica de Andalucía (CSIC)*

The dynamics of a particle moving in background electromagnetic and gravitational fields is revisited from a Lie group cohomological perspective. Physical constants characterising the particle appear as central extension parameters of a group which is obtained from a previously extended kinematical group (Poincaré or Galilei) by making *local* some subgroup. The corresponding dynamics is generated by a vector field inside the kernel of a presymplectic form which is derived from the canonical left-invariant one-form on the extended group. The non-relativistic (Newtonian) limit is derived from the *geodesic* motion via an Inönü-Wigner contraction. A deeper analysis of the cohomological structure reveals the possibility of a new force associated with a non-trivial mixing of gravity and electromagnetism leading to testable predictions, such as a mass difference between charged particles and anti-particles.

### Chern-Simons Gravity: Non-Topological Approach

A. Borowiec, M. Ferrari, M. Francaviglia

*Institute of Theoretical Physics, Wrocław  
pl. M. Borna 9, 50-204 Wrocław, Poland*

Chern-Simons Lagrangians in  $d = 3$  dimensions are analyzed from the point of view of their covariance and globality. We use the transgression formula to find out a new covariant and global but bimetric Lagrangian for Chern-Simons gravity. We discuss the problem of conservation laws for Yang-Mills and gravitational examples: in particular, the energy-momentum complex and the superpotential is calculated. It is shown that such bimetric formalism is not longer a topological one.

### Higher-loop String Cosmology and Dilaton Stabilization

A. Saharian

*Department of Physics, Yerevan State University,  
375025 Yerevan, Armenia*

We consider the cosmological dynamics described by the low-energy string effective action with higher-loop corrections to the dilaton coupling functions. Under certain conditions on dilaton couplings these

corrections provide an efficient mechanism for dilaton stabilization during the cosmological expansion proposed by Damour and Polyakov. By using qualitative methods we investigate another mechanism proposed by the author and based on the assumption that higher-loop corrections generate dilaton couplings singular for some finite value of the dilaton field. The conditions are specified under which the cosmological evolution drives the dilaton to a stage with small cosmological variations. The phase space diagrams illustrating this type of dilaton stabilization are presented for various qualitatively different cases.

### On the Nature of the Activity of Galactic Nuclei

L. Grigoryan

*Department of Physics, Yerevan State University,  
375025 Yerevan, Armenia*

A model of compact nuclei of galaxies as star clusters far advanced to the state of statistical equilibrium is investigated. It is shown that rapidly spinning neutron stars and white dwarfs are the main constituents of compact galactic nuclei. The gamma radiation from active galactic nuclei is attributed to the radiation from pulsars that are in these nuclei. The X-ray and UV are considered to be synchrotron radiation from ultrarelativistic electrons ejected from pulsars and moved in the magnetic field of galactic nuclei.

### The Vela Pulsar Angular Velocity Relaxation After Its First Eight Jumps

M. Hairapetian, D. Sedrakian

*Department of Physics, Yerevan State University,  
375025 Yerevan, Armenia*

The theory of relaxation of the pulsars angular velocity is compared with the observational data for the first eight jumps of the Vela pulsar. The inverse problem in the theory of relaxation is solved in the exponential and linear relaxation regions. From this solutions the vortex distribution has been found, which leads to the observed relaxation of the Vela pulsar angular velocity. It is shown that the pinning of vortex lines plays a main role in the exponential relaxation regions, but it is necessary take into account the changes of angular velocity of the superfluid component in the linear relaxation region.

## Description of Supernova Data in Conformal Cosmology without Cosmological Constant

*D. Blaschke, D. Proskurin, V. Pervushin*

*Joint Institute for Nuclear Research, Dubna, Russia*

We consider cosmological consequences of a conformal invariant formulation of Einstein's General Relativity where the scale factor of the spatial metrics in the action functional gets replaced by the massless scalar (dilaton) field. The dilaton scales all masses including the Planck mass. Instead of the expansion of the universe we get the Hoyle-Narlikar type of mass evolution, where the temperature history of the universe is replaced by the mass history. We show that this conformal invariant cosmological model gives a satisfactory description of the new supernova Ia data for the luminosity distance-redshift relation without a cosmological constant and make a prediction for the behavior at  $z > 1$  which deviates from that of standard cosmology.

## Meissner Effect for Color Superconducting Quark Matter

*D. Blaschke<sup>1</sup>, K. Shahabasyan<sup>2</sup>, D. Sedrakian<sup>2</sup>*

<sup>1</sup>*Joint Institute for Nuclear Research, Dubna, Russia*

<sup>2</sup>*Department of Physics, Yerevan State University, 375025 Yerevan, Armenia*

The behaviour of the magnetic field inside the superconducting quark matter core of a neutron star is investigated in the framework of the Ginzburg-Landau theory. We take into account the simultaneous coupling of the diquark condensate field to the usual magnetic and to the gluomagnetic gauge fields. We solve the problem for three different physical situations: a semi-infinite region with a planar boundary, a spherical region, and a cylindrical region. We show that Meissner currents near the quark core boundary effectively screen the external static magnetic field.

## 8. Condensed Matter and Statistical Physics (CMSP)

### On Abnormal Strong Influence of Media on Relativistic Electron's Radiation Intensity

*S. Arzumanyan*

*Institute of Applied Problems in Physics  
25 Nersessian Str., 375014 Yerevan, Armenia*

The radiation intensity of an arbitrary moving electron is calculated for a medium with  $n \geq 1$  spherically-symmetric layers with different permittivities. In particular cases the obtained formulas coincide with previously known results. The intensity of radiation from an electron rotating around the equatorial plane inside a dielectric drop ( $n = 1$ ) is developed. The numerical calculations showed that if Cherenkov's condition for the electron and the matter of sphere is satisfied then there exist discrete values of the ratio of the radius of drop on that of electron orbit, at which anomalously strong radiation takes place. Such an intense radiation is formed inside the dielectric drop as a result of repeated reflection of Cherenkov radiation from the surface of the drop. During one period of rotation  $n_k \gg e^2/\hbar c$  quanta of electromagnetic field are emitted.

### Two Particle Correlation on 2D Hubbard Lattice

*A. Saakyan*

*Department of Physics, State Engineering University, of Armenia, 375009 Yerevan, Armenia*

Two Hubbard particles problem on finite square lattice with open and closed boundare is solved. The complete classification of eigenstates of the factorizable parity operator is carried out.

### Super-slipping Carbon Nanotubes

*M. Damnjanović, I. Milošević, T. Vuković*

*Faculty of Physics, POB 368, YU-11001 Belgrade*

Extremely low friction between walls of multi-wall carbon nanotubes is theoretically explained. The analysis stems from three quite general symmetry based principles. Their universality makes the result obtained relevant for the tribology in general offering a recipe for the lubricant selection. It is shown that friction decreases on the account of the symmetry breaking and that such a decrease is always robust in the nanotubes, even causing the Goldstone super-slippy sliding mode in the incommensurate multi-wall carbon nanotubes.

## Vibronic (In)Stability of Dipericodic Systems

*M. Damnjanović, B. Nikolić, I. Milošević*

*Faculty of Physics, POB 368, YU-11001 Belgrade*

Thin layers, multilayers and surfaces are the well known examples of the systems translationally periodic in two directions. Their symmetries are classified within 80 dipericodic groups. For all of them the Jahn-Teller (Peierls) electron-phonon coupling has been examined. This leading coupling term in the framework of the adiabatic approximation is responsible for the vibronic instability through the active vibrational modes.

The breakdown of the Jahn-Teller theorem is found in some highly symmetrical special points of the Brillouin zones of tetragonal and hexagonal dipericodic groups there are degenerate electronic states which are not coupled to the ion vibrations. Remarkably enough, this reduction of the electron-phonon coupling concerns particularly the tetragonal CuO planes in HTS materials and conducting layers of many heavy fermion superconductors, as well as the hexagonal graphite layers.

## Discrete Counterparts of $O(N)$ -Model on Bethe Lattice: $FC_N$ -Model

*N. Ananikyan, L. Ananikyan, V. Ohanyan*

*Yerevan Physics Institute, Yerevan State University*

We have considered the one of possible discrete version of  $O(N)$ -model, so-called Face-Cubic ( $FC_N$ ) model on the recursive Bethe-lattice. The corresponding system of recursion relations for partition function and magnetization per site was found. Using this system of recursion relations we plot the diagrams of magnetization versus the external magnetic field for different finite temperatures. The system was found to exhibit a complex magnetic behavior, including the number of bifurcation and chaos. Corresponding phase diagram was obtained.

## Electronic States In Parabolic Quantum Dot Taking Into Account Boundary Conditions

*E. Kazaryan, H. Sarkisyan, L. Petrosyan*

*Department of Physics, Yerevan State University, 375025 Yerevan, Armenia*

In this paper electronic states in parabolic quantum dot (QD), taking into account boundary conditions, were studied. The threshold habit of level appearance inside the dot was discovered. Electron energy dependence from QD radius and confinement potential height was studied. The discussion of causes to remove random degeneration, as the consequence of confinement potential modernization.

## To the Problems of Violation of Kohn's Theorem in Quantum Dots

*H. Sarkisyan*

*Department of Physics, Yerevan State University, 375025 Yerevan, Armenia*

The problem of Kohn theorem abnormality in semiconductor QD's (Quantum Dot) is investigated. Based on the proof of the theorem and its generalization in case of QDs it is concluded that given theorem is sequent to the dynamic symmetry of oscillating hamiltonian. Two cases of Kohn theorem abnormality are discussed. In the first case theorem abnormality arises due to the account of the boundary conditions, in the second case due to the account of electron dispersion law nonparabolicity. In other words, in the above-mentioned cases there isn't any opportunity to build total system of wave functions, connected to each other by "stair" operator.

## Four-loop RG Functions for $\varphi^4$ -theory with $O(N)$ -symmetric, cubic, and "chiral" interactions in Three Dimensions

*K. Varnashev*

*Saint Petersburg Electrotechnical University, Professor Popov Street 5, St. Petersburg, 197376, Russia*

Using the massive field theory in three dimensions, the RG functions for a generalized GL model of  $N$ -vector complex order parameter with three independent quartic coupling constants associated with  $O(N)$ -symmetric, cubic, and "chiral" interactions are deduced within the four-loop approximation. The model is relevant to the phase transitions in a variety of substances among which unconventional superconductors with exotic pairing, including high- $T_c$  superconductors, stacked triangular antiferromagnets, helical magnets, and certain antiferromagnets with complicated ordering. For all physical quantities of interest the most accurate numerical estimates are obtained. The results achieved are discussed along the line of the predictions given by other theoretical approaches and experimental data.



## 9. Quantum Optics and Coherent States (QOCS)

### Transfer of nonclassical features via lossy channels

*A. Chizhov*<sup>1</sup>, *L. Knöll*<sup>2</sup>, and *D.-G. Welsch*<sup>2</sup>

<sup>1</sup> *BLTP, JINR, 141980 Dubna, Russia*

<sup>2</sup> *Friedrich-Schiller-Universität Jena, 07743 Jena, Germany*

The ultimate limits of continuous-variable quantum teleportation due to absorption are studied, with special emphasis on (quasi)-monochromatic optical fields propagating through fibers. It is shown that the amount of information that would be transferred quantum mechanically over a finite distance is limited and effectively approaches to zero on a length scale that is much shorter than the (classical) absorption length. Only for short distances the state-dependent teleportation fidelity can be close to unity. To realize the largest possible fidelity, an asymmetrical equipment must be used, where the source of the two-mode squeezed vacuum is nearer to Alice than to Bob and in consequence the coherent displacement performed by Bob cannot be chosen independently of the transmission lengths.

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### Nonclassical Statistics and Phase-Space Symmetry in Quantum Chaos

*G. Kryuchkian, S. Manvelyan*

*Yerevan State University, Yerevan, 375025, Armenia*

Quantum manifestation of a classical chaotic dynamics is found in a framework of oscillatory excitation numbers statistics for a model of double driven nonlinear dissipative oscillator. The probability distributions, variances of oscillatory states, Wigner functions and von Neumann entropy are studied for order-chaos transition by numerical simulation of an ensemble of quantum trajectories. The nonclassical, sub-poissonian statistics of oscillatory number-states is established for chaotic dissipative dynamics in the frame of Fano factor and Wigner functions. It is shown that scaling invariance of strange attractor of the model violates in a quantum treatment of chaos. It is demonstrated the correlation between the emergence of chaos and quantum interference. These results are relevant for testing and experimental studying of quantum dissipative chaos.

### Multiphoton Entangled States and n-Fold Symmetries of Wigner Function

*G. Kryuchkian, N. Muradyan*

*Institute for Physical Research, National Academy of Sciences, Ashtarak-2, 378410, Armenia*

In this report we propose a novel approach for synthesizing and generating entangled light-states, using the idea of composite nonlinear interactions of photons in a cavity. We present new types of optical parametric oscillators (OPOs) - so called, three-photon OPOs and four-photon OPOs, which are experimentally feasible due to their low pump-power threshold and will play an important role in application to quantum information processing. The devices are based on cascaded down-conversion processes and consist of second-order media inserted in cavities. Discussion of dissipation and quantum features of the systems is performed by the quantum-jump simulation method, and concerns to the Wigner functions. The important features of three-photon and four-photon entangled states are threefold and fourfold symmetries of the Wigner functions in the phase space.

### Quest for the Separation of Discrete Variables

*K. B. Wolf*

*Centro de Ciencias Fisicas, Universidad Nacional Autonoma de Mexico*

The finite oscillator model based on  $u(2)$  has a finite number of energy levels and also the same number of values of position, and a proper limit to the continuum quantum oscillator. The wavefunctions are Wigner  $d(\pi/2)$ 's given with a factor of Kravchuk polynomials. In two dimensions, there are a Cartesian and a Radial model; position space is a finite pixellation along Cartesian and polar coordinates. These correspond to the two chains  $u(1) \oplus u(1) \subset u(2) \oplus u(2) = so(4) \oplus u(1) \supset so(3)$ . The radial wavefunctions of the latter are  $so(3)$  Clebsch-Gordan's, given with a factor of Hahn polynomials. We propose finite unitary approximants to the Hankel (i.e. Fourier-Bessel) integral transforms, as well as a conversion between square- and round- pixellated images.

## 10. Symmetry in Nuclear and Atomic Physics (SNAP)

### An Application of Vector Coherent State Theory to the $SO(5)$ Proton-Neutron Quasispin Group

W. Berej

*Institute of Physics, Maria Curie-Skłodowska University, 20-031 Lublin, Poland*

Vector coherent state theory (VCS), developed for computing Lie group and Lie algebra representations and coupling coefficients, has been used for many groups of interest in actual physical applications. We show that VCS construction of a rotor type can be performed for the  $SO(5) \sim Sp(4)$  quasispin group where the relevant physical subgroup  $SU(2) \times U(1)$  is generated by the isospin operators and the number of particles operator.

### States with Moving Condensate in Nuclear Matter

A. Isayev

*Kharkov Institute of Physics and Technology, Kharkov, Ukraine*

In this report we consider  $np$  superfluidity of nuclear matter with nonzero total momentum of Cooper pairs (nuclear LOFF phase). It is assumed that coupling between  $T = 0$  and  $T = 1$  isospin pairing channels leads to the emergence of multi-gap superfluid states, characterized by nonvanishing gaps in both pairing channels. The self-consistent equation for such states, generalizing the BCS equation, has been obtained. Various symmetry properties of this equation have been studied, allowing to find different solutions in the case, when one of these solutions, corresponding to the mixed pairing, is known. The structure of phase diagrams at zero temperature, including dependencies of the order parameters from density and superfluid momentum, has been clarified. It is shown, that multi-gap LOFF phase exists in finite density region, excluding some vicinity of zero density, where  $T = 1$  order parameter is always finite and  $T = 0$  one continuously appears and disappears from the zero value.

### Applications of the Deformed Fermion Realization of $sp(4)$

J. Draayer<sup>1</sup> and A. Georgieva<sup>2</sup>, K. Sviratcheva<sup>1</sup>

<sup>1</sup> *Louisiana State University, Department of Physics and Astronomy, Baton Rouge, Louisiana, 70808-4001 USA*

<sup>2</sup> *Institute of Nuclear Research and Nuclear Energy, Bulgarian Academy of Sciences, Sofia 1784, Bulgaria*

A fermion representation of the compact symplectic  $sp(4)$  algebra provides a natural description of the pairing interaction in nuclei. In the non-deformed and deformed cases the reduction chains to different realizations of  $u(2)$  and  $u_q(2)$  are explored for multiple orbits. One of the realizations is associated with the  $SU(2)$  group of the valence isospin. The other reductions describe pairing between identical fermions or proton-neutron configurations. Microscopic non-deformed and deformed Hamiltonians are expressed in terms of the generators of  $Sp(4)$  and  $Sp_q(4)$ . In both cases eigenvalues of the Hamiltonian are fit to experimental ground state energies which allows the role of the deformation to be investigated. The  $q$ -deformation parameter varies the pairing strength, thereby providing for a non-linear expansion of the nuclear collective motion.

### On Symmetry of Elementary Particles

N. Korkhmazyan, N. Korkhmazyan

*Armenian Pedagogical Institute, Yerevan 375010, Armenia  
E-mail: norayrk@yahoo.com*

The new quantum number  $\sigma$  is introduced. It is shown that the conservation of  $\sigma$ -number predicts that the electron type neutrino mass is exactly zero. The quark-lepton symmetry is discussed. It is shown that the nature of quark-lepton symmetry is reflected in the fact that elementary particles of the same generation are subject to the symmetry transformation represented by 4-group of diedr. It is also shown that colorless elementary particles are subject to the same symmetry transformation. The new elementary particles (transbaryons) are predicted. Using  $\sigma$  number definition Gell-Mann-Nishijima relation is obtained.

### The Integrable Three-Body Problem with Induced Gauge Fields

S. Vinitsky

*BLTP, JINR, Dubna, 141980, Moscow reg., Russia*

The Hilbert fiber bundle construction induced by the adiabatic expansion of the wave function of a three-body problem is considered. The canonical transformation of the problem is explicitly constructed

18594 Ep.

to reduce the coupled adiabatic equations with induced gauge field potentials to equations involving only the open channels we are interested in. To demonstrate the efficacy of this Canonical Adiabatic Approach, we choose the model of 3 particles on a line, with attractive pair  $\delta$ -function potentials, since, for this case, exact results are known. The sixfold symmetry picture of the problem is used. The work is supported by the RFBR-BRFBR grant No. 00-02-81023 Bel 2000.a.

## 12. Mathematical Methods (MM)

### The Quantum Motion of Charged Particles in the Circularly Polarized Magnetic Field

A. Baghdasaryan

Yerevan State University, 375025 Yerevan, Armenia, E-mail: abaghd@www.physdep.r.am

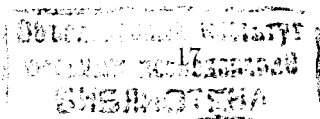
We study the quantum theory of nonlinear interaction of charged particles with a given circularly polarized periodic magnetic field. The approximate nonlinear solution of the Mathieu equation to which the relativistic quantum equation of particle motion in the given field reduces if one ignores the spin-field interaction is found (the Klein-Gordon equation). At the high energy particle motion the obtained solution is valid in the case if the energy change of particle is in the order of particle energy in contrast to the Eikonal approximation. At the small field interaction the obtained solution is the analytic expression of the infinite sum of perturbation theory in the field. We study the stability of solutions and find a class of restricted solutions corresponding to the wave function of the particle. The method developed in the paper can be applied to a broad class of problems reducible to the solution of the Mathieu equation.

### Moyal-Lie Theory and Phase Space Quantization

T. Hakioglu

Physics Department, Bilkent University, Ankara 06533 Turkey

Phase Space  $\star$ -quantization implies a deformed (noncommutative) symplectic phase space flow. The generators of this flow are the deformations of the classical Hamiltonian vector fields. These deformed Hamiltonian vector fields, contrary to their classical counterparts, form an associative algebra, i.e. the Moyal-Lie algebra, as the algebra of nonlinear symplectic maps in deformed phase space. The covariance properties of these symplectic maps are presented.



## Second Order Irreducible Supersymmetry for Periodic Potentials

*D. Fernandez*<sup>2</sup>, *B. Mielnik*<sup>2</sup>, *O. Rosas-Ortiz*<sup>2</sup>,  
*B. Samsonov*<sup>1</sup>

<sup>1</sup>*Department of Quantum field theory, Tomsk State University, 634050, Tomsk, Russia*

<sup>2</sup>*Departamento de Física, CINVESTAV-IPN, A.P. 14-740, 07000 México D.F., México*

We have found that second order Darboux transformations may create regular periodic potentials when the transformation functions involved have eigenvalues inside of a forbidden band. This transformation being presented as a sequence of first order ones is irreducible in the sense that intermediate potentials have poles. We observe that in some cases Darboux transformations result only in a displacement of the initial potential. We call such an effect *translationary invariance with respect to Darboux transformations*. Second order supersymmetrical quantum models built of Darboux transformation operators involved correspond to the case of broken supersymmetry.

## Wavelet Analysis of Secondary Particles Angular Distributions in High Energy Nucleus-Nucleus Interactions

*V. Uzhinskii*

*LIT, JINR, Dubna, Moscow Region, 141980, Russia*

Wavelet analysis is a modern mathematical method aimed to distinguish different unregularities and scale invariance. It is an extension of the well known Fourier analysis. The wavelet analysis is the study of any function by expanding it in the wavelet series (a complete orthonormal system). The system is a two-parametric function family. The main points of the analysis will be presented. An application of it for a study of the particles produced in high energy nuclear collisions will be given. The method allowed to find long-range clusterization of the particles in the pseudorapidity space. Quite interesting results were obtained at a study of the azimuthal distributions of the particles (collective flow signal). A preference scale was not found. Some experimental regularities of the wavelet spectra were observed. Another possibilities of the analysis are considered.

# List of Participants

<i>Anandan, Jeeva S.</i> Department of Physics and Astronomy University of South Carolina Columbia, SC 29208, USA	E-mail: jeeva@sc.edu Fax: +(1 803) 777 3065 Phone: +(1 803) 788 4302
<i>Ananikian, Nerses</i> Yerevan Physic Institute, Alikhanian Br. St. 2, 375036, Yerevan, Armenia	E-mail: ananik@jerewan1.yerphi.am Fax: 3742-350030 Phone: 3742-350150
<i>Angelova, Maia</i> School of Computing and Mathematics, University of Northumbria, GB-NE1 8ST, Newcastle upon Tyne, UK.	E-mail: maia.angelova@unn.ac.uk Fax: +(44 191) 227 3662 Phone: +(44 191) 2274349
<i>Arik, Matin</i> Bogazici University, Physics Department, Bebek Istanbul, 80815 Turkiye	E-mail: arikm@boun.edu.tr Fax: +(90 212) 2872466 Phone: +(90 212) 2631540/1615, 1369
<i>Arzumanian, Svetlana</i> Institute of Applied Problems in Physics Nersessian Str. 25, 375014 Yerevan, Armenia	E-mail: levonshg@iapp.sci.am
<i>Baghdasaryan, Ara</i> Yerevan State University, A. Manoogian 1, 375049, Yerevan, Armenia	E-mail: abaghd@www.physdep.r.am Phone: 3741-740750 Fax: 3741-570428
<i>Barker, Laurence John</i> Department of Mathematics, Bilkent University, 06544 Bilkent, Ankara, Turkey	E-mail: barker@fen.bilkent.edu.tr Fax: +(90 312) 266 4579 Phone: +(90 312) 290 2120
<i>Berej, Waldemar</i> Institute of Physics, Maria Curie-Sklodowska University, 20-031 Lublin, Poland	E-mail: berej@tytan.umcs.lublin.pl Fax: +(48 81) 537 6190 Phone: +(48 81) 537 6164
<i>Bonora, Lorian</i> SISSA, Via Beirut 2-4, 34013, Trieste, Italy	E-mail: bonora@he.sissa.it Fax: +(40) 378 7528 Phone: +(40) 378 7436
<i>Borowiec, Andrzej</i> Institute of Theoretical Physics, University of Wroclaw, pl. M. Born 9, 50-204 Wroclaw, Poland	E-mail: borow@ift.uni.wroc.pl Fax: +(48 71) 321 4454 Phone: +(48 71) 320 1406
<i>Boyle, Laurence</i> University Chemical Laboratory, Canterbury, Kent, England	E-mail: L.L.Boyle@ukc.ac.uk
<i>Burdik, Cestmir</i> Nuclear centre, Faculty of Mathematics and Physics, Charles university, Prague, Czechia	E-mail: burdik@dec1.fjfi.cvut.cz Fax: +(42 2) 290 572 Phone: +(42 2) 296 137

<i>Chavleishvili, Michael</i> Laboratory of Particle Physics, Joint Institute for Nuclear Research, 141980 Dubna, Moscow Reg., Russia	E-mail: chavlei@thsun1.jinr.ru
<i>Chizhov, Alexei</i> Bogoliubov Laboratory of Theoretical Physics, Joint Institute for Nuclear Research, 141980 Dubna, Russia	E-mail: chizhov@thsun1.jinr.ru Fax: +(7 09621) 65 084 Phone: +(7 09621) 62 533
<i>Chizhov, Mihail</i> CERN and Sofia University, CERN 1211, Geneva 23, Switzerland	E-mail: M.chizhov@cern.ch Fax: ++(41 22) 767 31 00 Phone: ++(41 22) 767 60 34;
<i>Chubarian, Edvard</i> Yerevan State University, Alec Manougian, 1, 375049, Yerevan, Armenia	E-mail: pr-nat@sun.ysu.am Fax: +(3742) 554 641 Phone: +(3742) 556 181
<i>Codriansky, Simon</i> Departamento de Matemáticas y Física, Instituto Pedagógico M Caracuo, Caracas 1010, Venezuela	E-mail: codrians@reaccium.ve Fax: (58 02) 90 63 601 Fax: +(58 02) 90 63 402
<i>Daboul, Jamil</i> Physics Department, Ben Gurion University, Beer Sheva 84 105, Israel	E-mail: daboul@bgvms.bgu.ac.il Fax: 972 8 64 60 904 Phone: 972 8 64 72 132
<i>Dobrev, Vladimir</i> Institute of Nuclear Research and Nuclear Energy, Bulgarian Academy of Sciences, Tzarigradsko shosse 72, 1784 Sofia, Bulgaria	E-mail: dobrev@bgearn.acad.bg Fax: +(359 2) 755 019
<i>Draayer, Jerry</i> Department of Physics and Astronomy, Louisiana State University, 202 Nicholson Hall, Baton Rouge, Louisiana, USA	E-mail: draayer@sura.org Fax: 225-578-5855 Phone: 225-578-6844
<i>Fazio, Angelo Raffaele</i> Dipartimento di Fisica-Statale di Milano, I-20133, Italia	E-mail: Raffaele.Fazio@mi.infn.it Fax: +39 022392480 Phone: +39 022392286
<i>Flores Veldeś, Jorge</i> CCF, Universidad Nacional Autónoma de México, Apartado postal 48-3, 62251 Cuernavaca, Morelos, México.	E-mail: jfv@servidor.unam.mx Fax: (7) 317 53 88 Phone (7) 313 89 15
<i>Fronsdal, Christian</i> Physics at the University of California, 415 Hilgard Avenue, Los Angeles, California 90095-1547, USA.	E-mail: fronsdal@physics.ucla.edu
<i>Fursaev, Dmitry</i> Bogoliubov Laboratory of Theoretical Physics, Joint Institute for Nuclear Research, 141980 Dubna, Russia	E-mail: fursaev@thsun1.jinr.ru Fax: +(7 09621) 65 084 Phone: +(7 09621) 62 533
<i>Gadella, Manuel</i> Física Teórica, Facultad de Ciencias, c. Real de Burgos, s.n. 47011, Valladolid, Spain	E-mail: gadella@fta.uva.es Fax: 34-983-423013 Phone: 34-983-423145
<i>Georgieva, Ana</i> Institute of Nuclear Research and Nuclear Energy, Bulgarian Academy of Sciences, Tzarigradsko shosse 72, 1784 Sofia, Bulgaria	E-mail: anageorg@inrnc.bas.bg Fax: (359-2)-975-36-19 Phone: (359)-2-7144/474
<i>Gózdź, Andrzej</i> Institute of Physics, Maria Curie-Skłodowska University, 20-031 Lublin, Poland	E-mail: gozdz@neuron.umcs.lublin.pl E-mail: gozdz@tytan.umcs.lublin.pl Fax: +(48 81) 537 6190 Phone: +(48 81) 537 537 6239



<i>Gromov, Nikolai A.</i> Department of Mathematics, Syktyvkar Branch of IMM, Syktyvkar, Russia	E-mail: gromov@dm.komisc.ru Fax: +(7 8212) 215 740 Phone: +(7 8212) 215 740
<i>Jackiw, Roman</i> Massachusetts Institute of Technology MIT, Bldg. 6, room 320, 77 Massachusetts Ave, 02139-4307, Cambridge, MA, USA	jackiw@lns.mit.edu Fax: 617 253 8674 Phone (office): 617 253 4830
<i>Jaramillo, Jose Luis</i> Instituto de Astrofisica de Andalucia (CSIC) Apartado Postal 3004, 18080, Granada, Spain	E-mail: jarama@iaa.es Fax: +34 958814530 Phone: +34 958121311
<i>Hakioglu, Tugrul</i> Physics Department, Bilkent University, 6533, Ankara, Turkey	E-mail: hakioglu@fen.bilkent.edu.tr Fax: 90 312 266 4579 Phone: 90 312 290 2109
<i>Harutyunyan, Gohar</i> Yerevan State University, Alec Manougian, 1, 375049, Yerevan, Armenia	
<i>Hairapetyan M.</i> Yerevan State University, Alex Manoogian st. 1, 375025 Yerevan, Armenia	
<i>Hietarinta, Jarmo Niilo</i> Department of Physics, University of Turku, FIN-20014 Turku, Finland	E-mail: hietarin@utu.fi Fax: (358-21) 333 59 93 Phone: (358-21) 333 56 85
<i>Hovanisyan, Arthur</i> Yerevan State University, Alex Manoogian st. 1, 375025 Yerevan, Armenia	
<i>Hussin, Veronique</i> CRM, Universite' de Montreal, CP 6128-A, Montreal, Quebec, H3C 3J7, Canada	E-mail: hussin@dms.umontreal.ca Fax: (1-514) 343-2254 Phone: (1-514) 343-7814
<i>Isaev, Alerei</i> Bogoliubov Laboratory of Theoretical Physics, Joint Insitute for Nuclear Research, 141980 Dubna, Russia	E-mail: isaevap@thsun1.jinr.dubna.su Fax: +(7 09621) 65 084 Phone: +(7 09621) 63 024 <b>3.A</b>
<i>Ivanov, Evgenyi</i> Bogoliubov Laboratory of Theoretical Physics, Joint Insitute for Nuclear Research, 141980 Dubna, Russia	E-mail: eivanov@thsun1.jinr.ru Fax: +(7 09621) 65 084 Phone: +(7 09621) 63352
<i>Kalnins, Ernie G.</i> Mathematics Department, University of Waikato, Hamilton, New Zealand	E-mail: math0236@waikato.ac.nz Fax: 64 07 838 4666 Phone: +(64 07) 586 2889 ext833
<i>Karayan, Khajak</i> Yerevan State University, Alec Manougian St., 1, 375049, Yerevan, Armenia	
<i>Kerner, Richard</i> Laboratoire GCR, Boite 142, Universite Paris VI, Boite 142, 4 Place Jussieu, 75005, Paris, France	E-mail: RK@ccr.jussieu.fr Fax: +(33 1) 4427 7287 Phone: +(33 1) 4427 7298
<i>Kibler, Maurice</i> Institut de physique Nucleaire de Lyon, IN2P3-CNRS et Universite,' Claude Bernard, F-69622, Villeurbanne Cedex, France	E-mail: m.kibler@ipnl.in2p3.fr Fax: 33 4 72 44 80 04 Phone: 33 4 72 44 84 39
<i>Khvedelidze, Arsen</i> Bogoliubov Laboratory of Theoretical Physics, Joint Institute for Nuclear Research, Dubna, Russia	E-mail: khved@thsun1.jinr.ru Fax: +(7 09621) 65 084 Phone: +(7 09621) 63 720

<i>Komarov, Igor</i> University of St.Petersburg, St.Petersburg 198904, Russia	E-mail: igor.komarov@pobox.spbu.ru E-mail: komarov@mph.phys.spbu.ru
<i>Korepin, Vladimir</i> State University of New York Nicolls road, Stony Brook, NY 11794-3840, USA	E-mail: korepin@insti.physics.sunysb.edu Fax: +1 (516) 632-7954 Phone: +1 (516) 632-7981
<i>Korkhmazyan, Natan</i> Armenian Pedagogical Institute Khanjyan St. 5, 375010, Yerevan, Armenia	E-mail: norayrk@yahoo.com Phone: +374-1-523754
<i>Kostyakov, Igor</i> Department of Mathematics, Syktyvkar Branch of IMM, Syktyvkar, Russia	E-mail: kostyakov@dm.komisc.ru Phone/Fax: +(7 8212) 215 740
<i>Kozlov, Guennadi</i> Bogoliubov Laboratory of Theoretical Physics, Joint Institute for Nuclear Research, Moscow Region, 141980, Russia	E-mail: kozlov@thsun1.jinr.ru Fax: +(7 09621) 65 084 Phone: +(7 09621) 62 163
<i>Kryuchyan, Gagik</i> Istitute for Physical Research, National Academy of Sciences, 378410, Ashtarak-2, Armenia	E-mail: kry@ipr.sci.am Fax: +(374 43) 31 172 Phone: +(374 2) 288 150
<i>Lukierski, Jerzy</i> Institute of Theoretical Physics, University of Wroclaw; Poland	E-mail: lukier@ift.uni.wroc.pl Fax: +(48 71) 320 1409 Phone: +(48 71) 201 411
<i>Lusanna, Luca</i> Direttore di Ricerca Istituto Nazionale Fisica Nucleare Sezione di Firenze, Largo E. Fermi 2 (Arcetri) Firenze, 0125,Italy	E-mail: Luca.Lusanna@fi.infn.imt Fax: +39 055 229330 Phone: +39 055 2307788
<i>Lutsenko, Alexei</i> Laboratory of Information Technologies, Joint Institute for Nuclear Research, Dubna, Moscow Region, 141980, Russia	E-mail: lutsenko@cv.jinr.ru Fax: +(7 09621) 65 084 Phone: +(7 09621) 64 875
<i>Mardoyan, Levon</i> International Center for Advanced Studies, Yerevan State University, Alex Manoogian st. 1, 375025 Yerevan, Armenia	E-mail: mardoyan@icas.yasu.am Fax: (+3741) 151 087 Phone: (+3741) 570 370
<i>Martirosian, Radick</i> Yerevan State University, Alex Manoogian st. 1, 375025 Yerevan, Armenia	
<i>Milosević, Ivanka</i> Faculty of Physics University of Belgrade, P.O. Box 368, YU-11000 Belgrade, Yugoslavia	E-mail: ivag@afrodita.rcub.bg.ac.yu Fax: +(381 11) 328 2619 Phone: +(381 11) 630 152
<i>Ruben Mkrtchyan</i> Yerevan Physics Institute, Alikhanian Brothers St. 2, Yerevan, 375036, Armenia	E-mail: mrl@amsun.yerphi.am Fax: +3741 35-00-30 Phone: +3741 34-15-00
<i>Nersessian, Armen</i> Bogoliubov Laboratory of Theoretical Physics, Joint Institute for Nuclear Research, Dubna, Moscow Region, 141980, Russia	E-mail: nerses@thsun1.jinr.ru Fax: +(7 09621) 65 084 Phone: +(7 09621) 63 636
<i>Niederle, Jiri</i> Institute of Physics, ASCR, 182 21 Prague 8, Czech Republic	E-mail: niederle@fzu.cz Fax: 420-2-688 2948 Phone: 420-2-6605 2667 or 2610
<i>Nikolic, Bozidar</i> Faculty of Physics, University of Belgrade, Studentski trg 10-12, P.O.Box 368, 11001, Belgrade, Yugoslavia	E-mail: boza@ff.bg.ac.yu Fax: +(381 11) 328 2619 Phone: +(381 11) 630 152

<i>Olver, Peter</i> School of Mathematics, University of Minnesota, Minneapolis, MN 55455, USA	E-mail: olver@ima.umn.edu Fax: (1-612) 626 2017 Phone: (1-612) 624 5534
<i>Papoyan, Vladimir</i> Yerevan State University, A. Manougian str. 1, 375025 Yerevan, Armenia	E-mail: vpap@www.physdep.r.am Phone: +(88 52) 570370
<i>Patera, Jan</i> Czech Technical University, KM FJFI, Trojanova 13, 120 00, Praha 2, Czech Republic	E-mail: patera@km1.fjfi.cvut.cz Fax: +420-2-24918643 Phone: +420-2-24318631
<i>Patera, Jiri</i> Centre de Recherches Mathematiques, Universite' de Montreal, CP 6128-A, Montreal, Quebec, H3C 3J7, Canada	E-mail: patera@crm.umontreal.ca Fax: +(1-514) 343 2254 Phone: +(1-514) 343 6419
<i>Pogosyan, George</i> BLTP and ICAS, Joint Institute for Nuclear Research, Dubna, Moscow Region, 141980, Russia	E-mail: pogosyan@thsun1.jinr.ru Fax: +(7 09621) 65 084 Phone: +(7 09621) 63 153
<i>Popowicz, Ziemowit</i> Institute of Theoretical Physics, University of Wroclaw, 50-205 Wroclaw, Poland	E-mail: ziemek@ift.uni.wroc.pl (04871) 321 44 54 Phone: +(48 711) 320 14 03
<i>Proskurin, Denis</i> Bogoliubov Laboratory of Theoretical Physics, Joint Institute for Nuclear Research, Dubna, Moscow Region, 141980, Russia	E-mail: proskur@thsun1.jinr.ru Fax: +(7 09621) 65 084 Phone: +(7 09621) 63 348
<i>Salamo, Sebastian</i> Departamento de Fisica, Universidad Simon Bolivar, Apartado Postal 89000, Caracas, Venezuela	E-mail: ssalamo@fis.usb.ve Fax: +(58 2) 906 3601 Phone: +(58 2) 906 3618
<i>Saharian, Aram</i> Yerevan State University A. Manoogyan St. 1, 375025, Yerevan, Armenia	E-mail: saharyan@server.physdep.r.am
<i>Samsonov, Boris</i> Quantum Field Theory Department Tomsk State University, Tomsk, Russia	E-mail: samsonov@phys.tsu.ru Fax: (7 382) 426 195 Phone: +(7 3832) 913 019 634050
<i>Silagadze, Zurab</i> Budker institute of Nuclear Physics, Acad.Lavrentiev prospect 11, 630090 Novosibirsk, Russia	E-mail: silagadze@inp.nsk.su Fax: +7 (3832) 342163 Phone: +7 (3832) 394205
<i>Sissakian, Alexei</i> Joint Institute for Nuclear Research, Dubna, Moscow Region, 141980, Russia	E-mail: sisakian@jinr.ru Phone: +(7 09621) 62 268
<i>Sitenko, Yuri</i> Bogolyubov Institute for theoretical Physics, Metrologichna str. 14b, Kyiv, Ukraine	E-mail: yusitenko@bitp.kiev.ua Fax: (38-044) 266 59 98 Phone: (38-044) 266 91 48
<i>Shirkov, Dmitri</i> Bogoliubov Laboratory of Theoretical Physics, Joint Institute for Nuclear Research, Dubna, Moscow Region, 141980, Russia	E-mail: shirkov@thsun1.jinr.ru Fax: +(7 09621) 65 084 Phone: +(7 09621) 65 088
<i>Smorodinskaya, Noemi</i> Institute of Theoretical and Experimental Physics, Bolshaya Cheremushkinskaya ulitsa 25, 117218, Moscow, Russia	E-mail: naya@crdf.ru Fax: 7-095-7776559 Phone: 7-095-1299415
<i>Sorba, Paul</i> LAPTH (CNRS), Chemin de Bellevue, BP 110, 74941, Annecy-le-Vieux, France	E-mail: sorba@lapp.in2p3.fr Paul.Sorba@lapp.in2p3.fr Fax: 33 4 50 09 89 13 Phone: 33 4 50 09 16 85

<i>Sudbery, Antony</i> University of York, Heslington, YO10 5DD, York, UK	E-mail: as2@york.ac.uk Fax: +44 1904 433071 Phone: +44 1904 433081
<i>Suzko, Alina</i> Laboratory of Information Technologies, Joint Institute for Nuclear Research, Dubna, Moscow Region, 141980, Russia	E-mail: suzko@thsun1.jinr.ru Fax: +(7 09621) 65 084 Phone: +(7 09621) 62 473
<i>Tarlini, Marco</i> I.N.F.N. Sezione de Firenze, L. go E. Fermi 2, 50125 Firenze, Italy.	E-mail: Marco.Tarlini@fi.infn.it Fax: (39055) 229330 Phone: (39055) 2307828
<i>Twarock, Reidun</i> City University Northampton Square N1 2PB, London, England	E-mail: r.twarock@city.ac.uk Fax: 0044-207-477 8597 Phone: 0044-207-477 8952
<i>Varnashev, Konstantin</i> St. Petersburg Electronical University, Pr.Popov st. 5, St.Petersburg, 197376, Russia	E-mail: kvarnash@kv8100.spb.edu Fax: (7-812) 346 27 58 Phone: (7-812) 234-31-60
<i>Veselov, Alexander</i> Department of Mathematical Sciences, Loughborough University, Loughborough, Leicestershire LE11 3TU, UK	E-mail: A.P.Veselov@lboro.ac.uk Fax: +(44 1509) 223 969 Phone: +(44 1509) 222 866
<i>Winternitz, Pavel</i> Centre de Recherches Mathematiques, Universite' de Montreal, CP 6128-A, Montreal, Quebec, H3C 3J7, Canada	E-mail: wintern@crm.umontreal.ca Fax: +(1 514) 343 2254 Phone: +(1 514) 343 7271
<i>Wolf, Kurt Bernardo</i> IIMAS-UNAM, Universidad Nacional Autonoma de Mexico, Apartado postal 48-3, 62251 Cuernavaca, Morelos, Mexico	E-mail: bwolf@fis.unam.mx Phone/Fax: +(52 73) 173 388 Phone/Fax: +(52 73) 170 955
<i>Yarzhemsky, Victor</i> Institute of General & Inorganic Chemistry, Russian Academy of Sciences, Moscow, Russia	E-mail: vgyar@ionchran.rinet.ru Fax: +(7 095) 954 1279 Phone: +(7 095) 954 2230
<i>Yeranyan, Armen</i> International Center for Advanced Studies, Yerevan State University, Alex Manoogian st. 1, 375025 Yerevan, Armenia	E-mail: ayeran@icas.y-su.am Fax: (+3741) 151 087 Phone: (+3741) 570 370
<i>Vinitsky, Sergei</i> Bogoliubov Laboratory of Theoretical Physics, Joint Institute for Nuclear Research, Dubna, Moscow Region, 141980, Russia	E-mail: vinitsky@thsun1.jinr.ru Fax: +(7 09621) 65 084 Phone: +(7 09621) 63 348
<i>Zakhariev, Boris</i> Bogoliubov Laboratory of Theoretical Physics, Joint Institute for Nuclear Research, Dubna, Moscow Region, 141980, Russia	E-mail: zakharev@thsun1.jinr.ru Fax: +(7 09621) 65 084 Phone: +(7 09621) 64 747

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