

С 346.6

G-60

7.2

ОБЪЕДИНЕННЫЙ
ИНСТИТУТ
ЯДЕРНЫХ
ИССЛЕДОВАНИЙ

Дубна

R-2945



МАТЕРИАЛЫ
XIII МЕЖДУНАРОДНОЙ КОНФЕРЕНЦИИ
ПО ФИЗИКЕ ВЫСОКИХ ЭНЕРГИЙ

Беркли 1966 г.

G. Goldhaber

G. Goldhaber
September 5, 1966

PICTORIAL ATLAS OF BOSON RESONANCES

SUPPLEMENT TO THE RAPPORTEUR TALK

ON "BOSON RESONANCES".

G. Goldhaber Rapporteur

B. C. Shen Secretary

NON STRANGE BOSONS (7a)

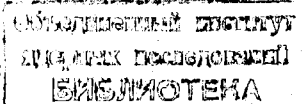
N. P. Samios Discussion Leader

A. R. Clark Secretary

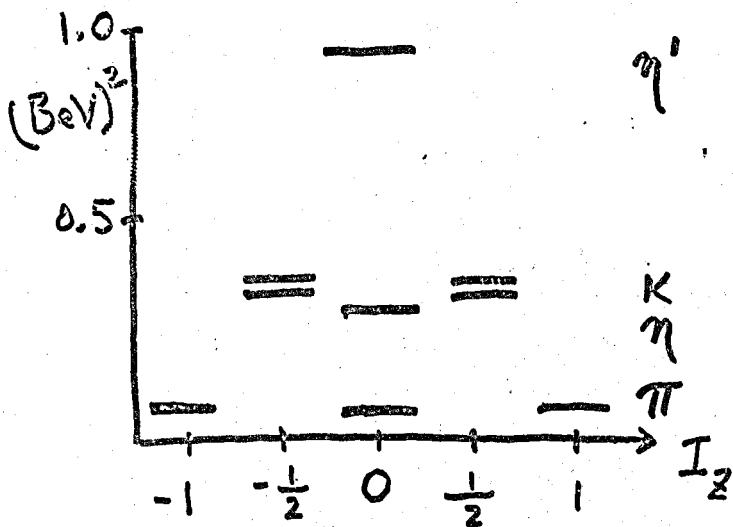
STRANGE BOSONS (7b)

A. Astier Discussion Leader

K. W. Lai Secretary



$J^P = 0^-$ NONET



η' $C = +1$
' $S_0(99)$ '

$K \eta$ $\theta_0 = 10^\circ$

π

Is $X^0 \stackrel{?}{=} \eta'$ $M = 959$

$E(1420) \rightarrow K \bar{K} \pi$

$C = +1$

CONCLUDED FROM:

$E \rightarrow K_1^0 K_1^0 \pi^0$

$\rightarrow K_1^0 K_2^0 \pi^0$

PREFERRED

SPIN : 0^-

1^+ (POSSIBLE)

83 ± 21 events

20 ± 25 events (limit)

$m' \stackrel{?}{=} X^0$ CAN THE X^0 BE
AN $I = 1$ OBJECT?

COMPARE RATES

$K^- p \rightarrow \Lambda X^0$	I=0 1	I=1 1
$K^- n \rightarrow \Lambda X^-$	0	2

Two K^- d Bubble Chamb. Expts.

① MARTIN et al (INDIANA)

FROM KNOWN X^0 PRODUCTION RATE,
IF $I = 1$

PREDICT	FIND
19 ± 6	5 ± 4

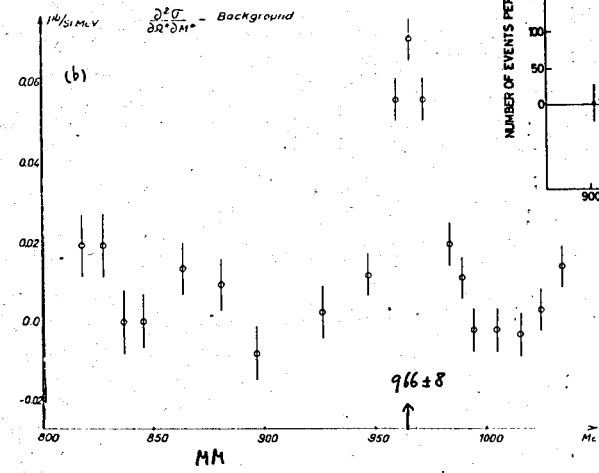
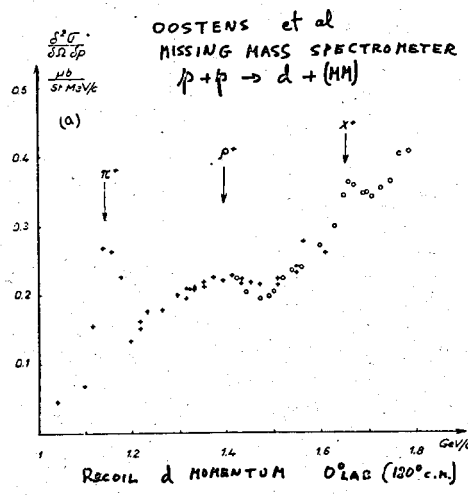
② RITTENBERG (LRL)

19 ± 6	0
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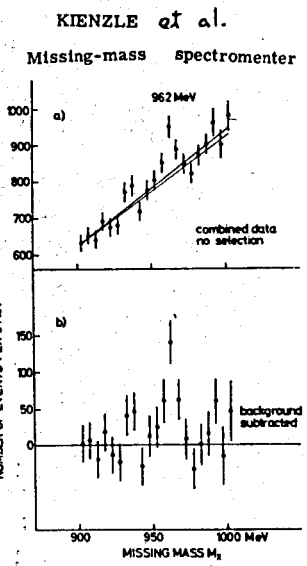
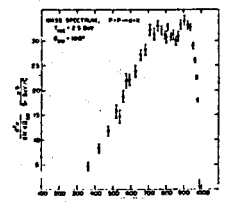
∴ $I = 1$ For X^0 Very Unlikely

$$\begin{array}{l}
 M(\delta^-) = 963 \pm 5 \quad P < 5 \\
 M(\delta^+) = 966 \pm 8 \quad P \sim 0 \\
 M(X^0) = 959 \quad P < 3
 \end{array}
 \left. \vphantom{\begin{array}{l} M(\delta^-) \\ M(\delta^+) \\ M(X^0) \end{array}} \right\} M(\delta^\pm) = 964$$

EVIDENCE FOR δ^+ and δ^-



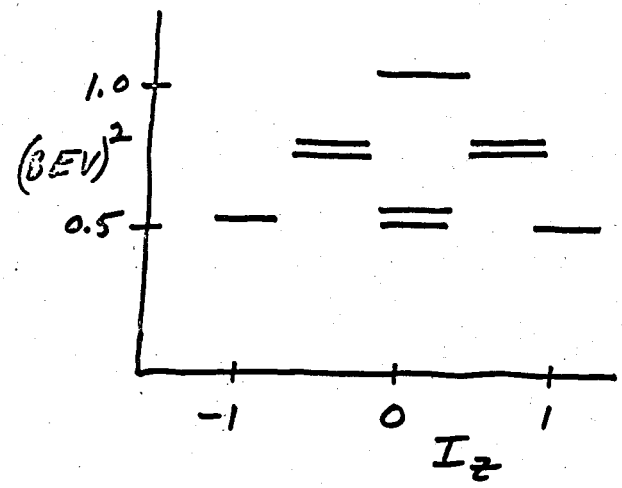
TURKOT et al.
 $p+p \rightarrow d + X^+$



δ^-

VECTOR

$J^P = 1^-$ $C = -1$ NONET
 $3S_1(\rho\bar{\rho})$



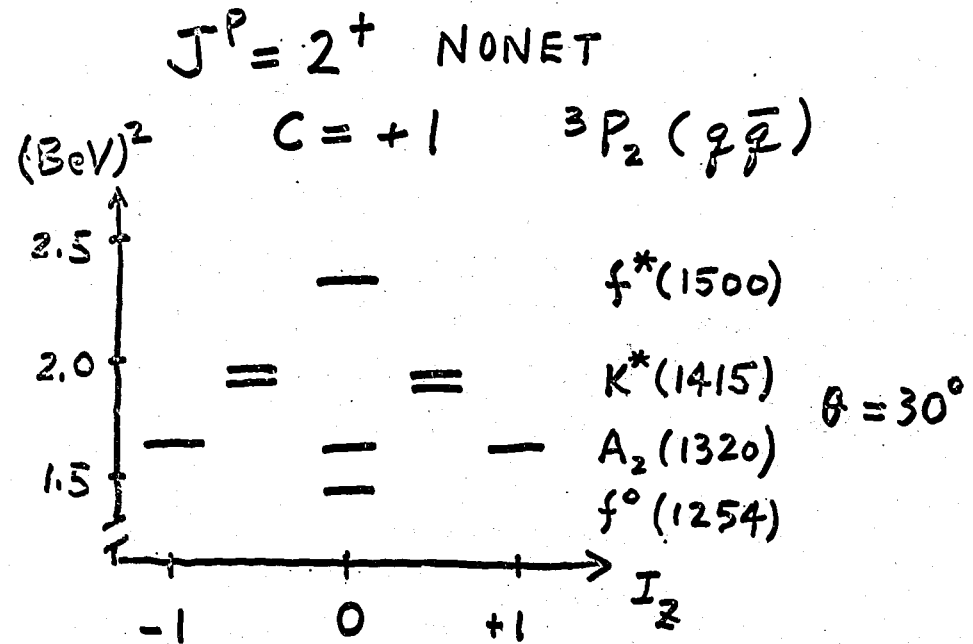
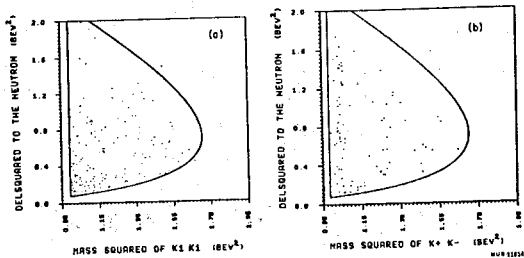
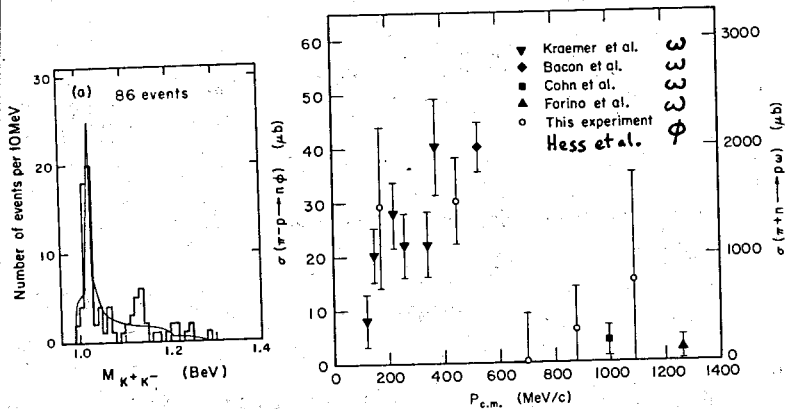
ϕ
 K^*
 ω
 ρ
 $\theta_1 = 40^\circ$

- ① ϕ SPIN $\bar{p}d \rightarrow \phi$
- ② $\pi^- p \rightarrow \phi n$
 $\quad \quad \quad \hookrightarrow K^+ K^-$

$\sigma(\phi) / \sigma(\omega) \approx 1/50$
Non-Peripheral ϕ .

- ③ $\omega - \rho$ Interference ?

Hess et al. $\pi^- p$



① A_2 SPIN — DEBATED

$A_2 \rightarrow K\bar{K}$ $J^P = 2^+$ CLEAR CUT (IGNORING 4^+)

$A_2 \rightarrow \rho\pi$ SPIN DETERMINATION STRONGLY
BACKGROUND DEPENDENT $1^+ ? 2^- ?$

A_2 MASS: 1280 MeV FOR 8 GeV/c DATA
1320 MeV " 3-4 " "

SPLITTING — DOUBTFUL

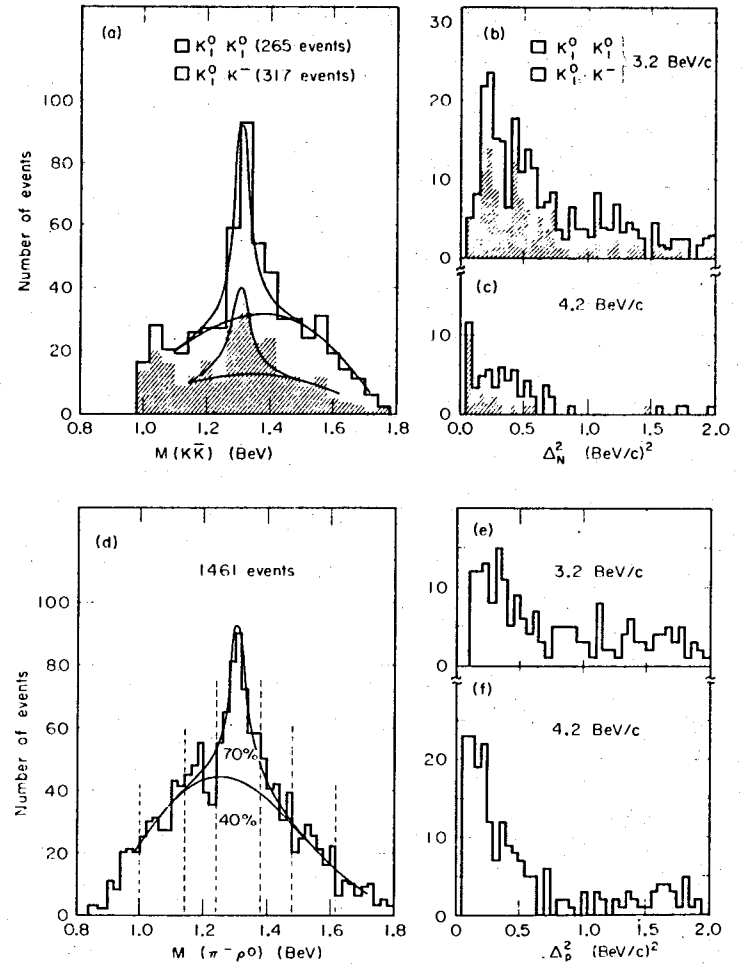
② f^0 SPIN 2^+ CONFIRMATION, $f^0 \rightarrow \pi^0\pi^0$

③ $f^* \rightarrow K\bar{K}^*$ LESS INTENSE, INTERFERENCE
WITH \underline{E} , SPIN 2^+ CONFIRMATION

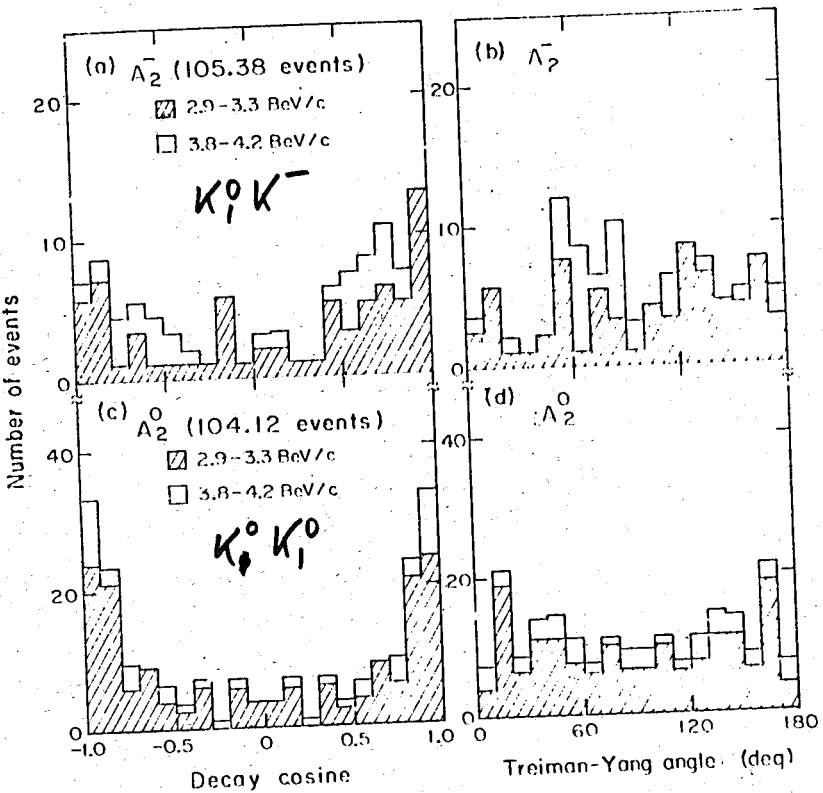
④ $K^*(1415) \begin{cases} \rightarrow K^*\pi \\ \rightarrow K\pi \end{cases} \sim 0.6$

CONSISTENT WITH GLASHOW SOCOLOW

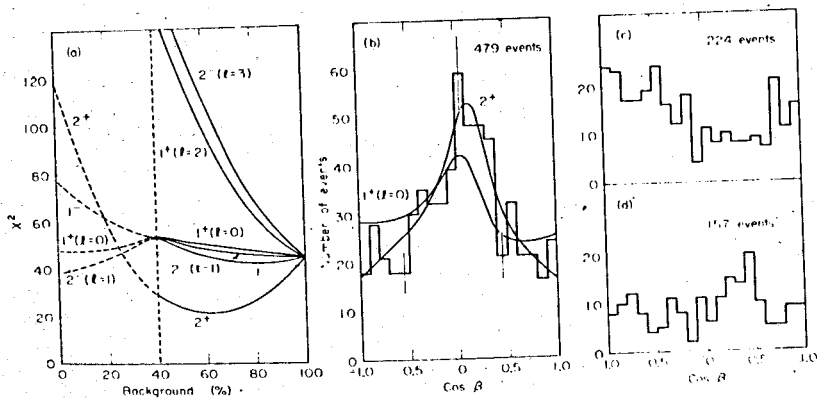
CHUNG et al. π^-p



CHUNG et al. $\pi^- p$

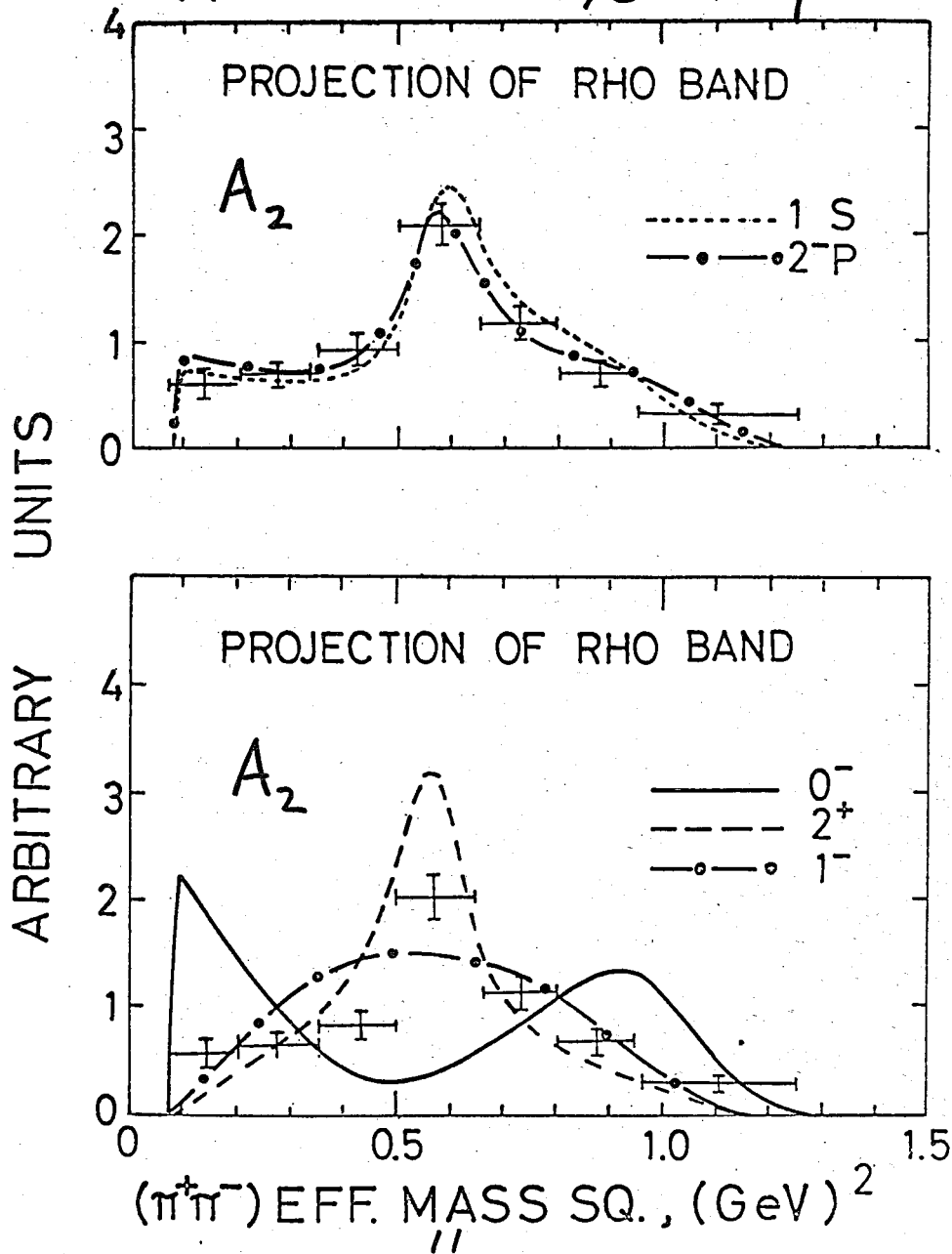


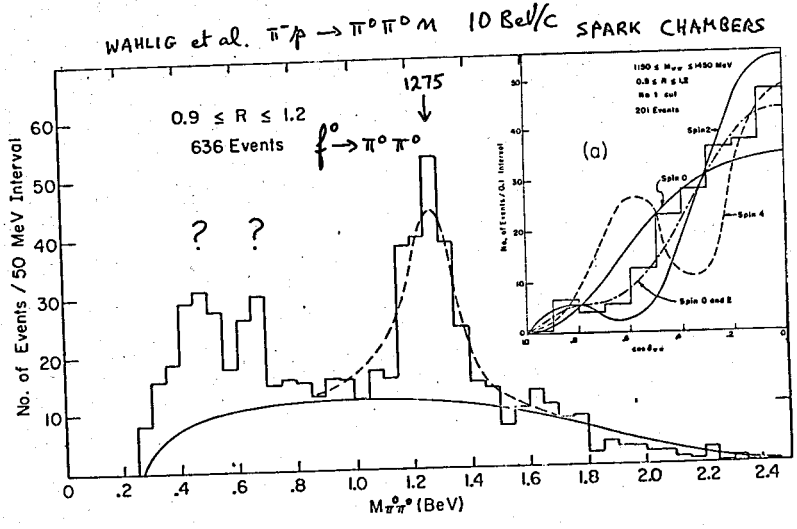
SPIN ANALYSIS FOR $A_2 \rightarrow p \pi$



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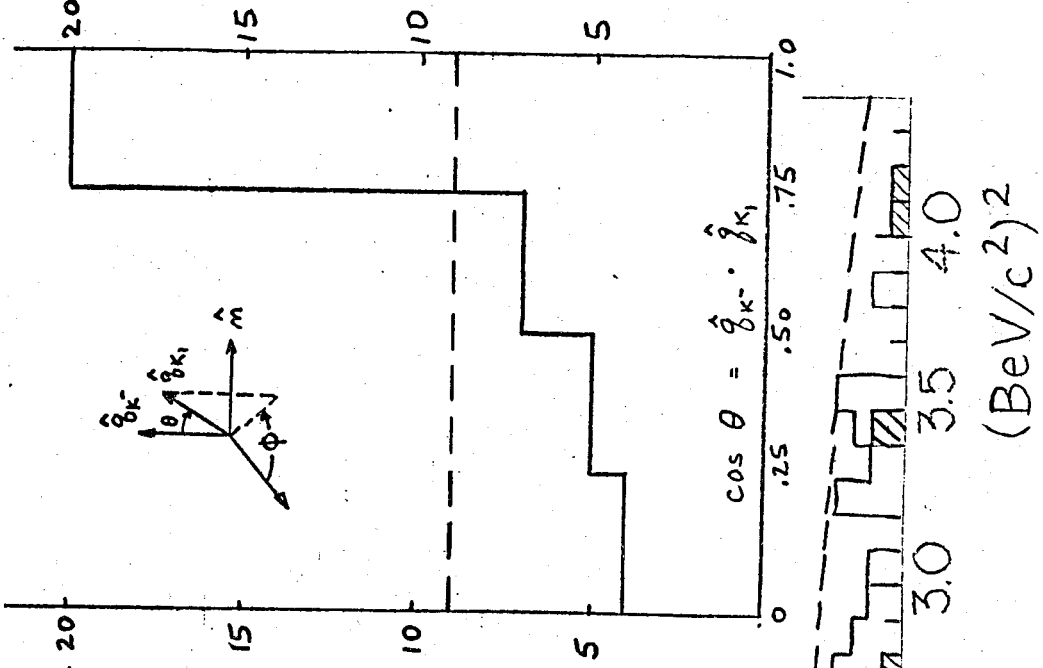
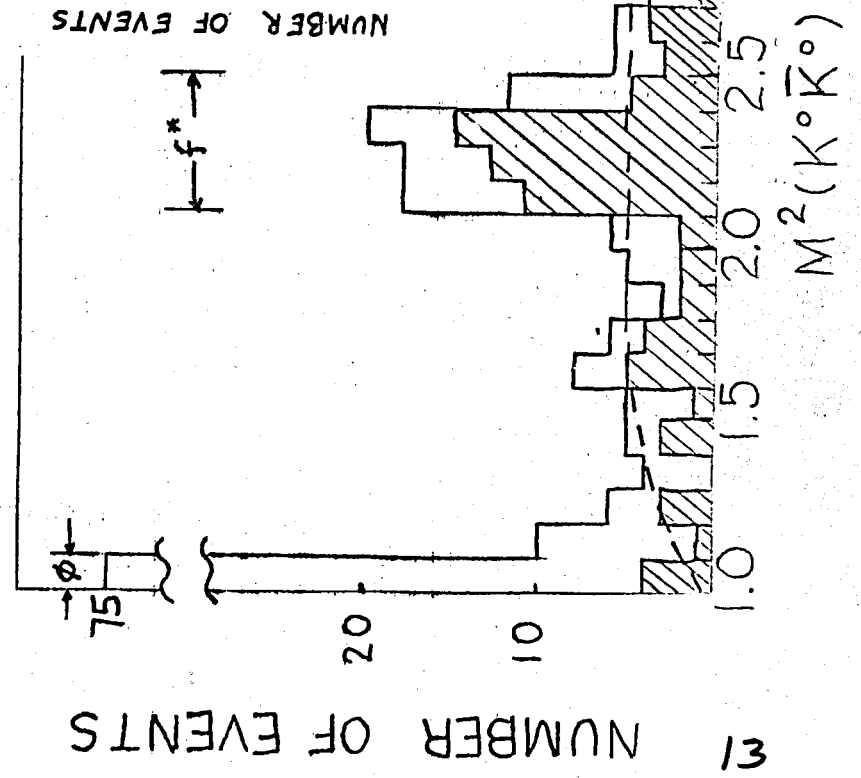
ABC 8 GeV/c $\pi^+ p$



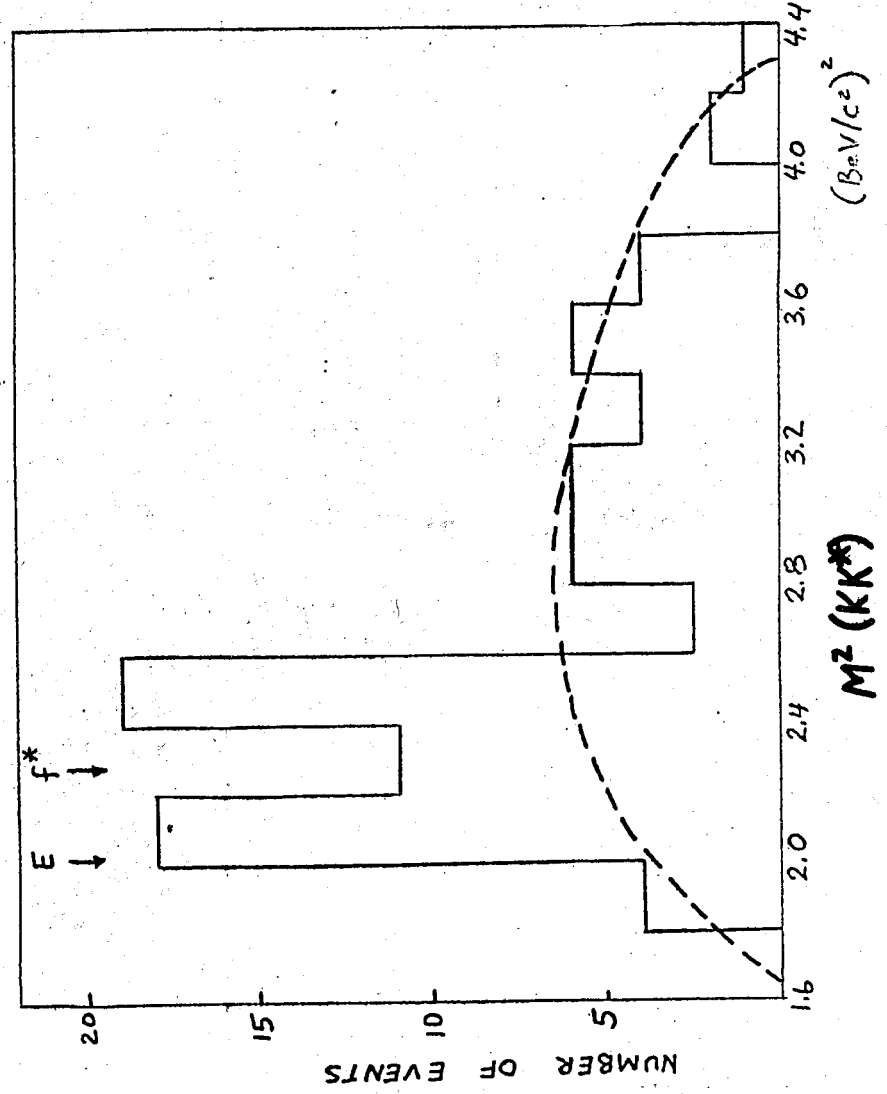


BARNES et al.

K^-p 4.6, 5.0 BeV/c



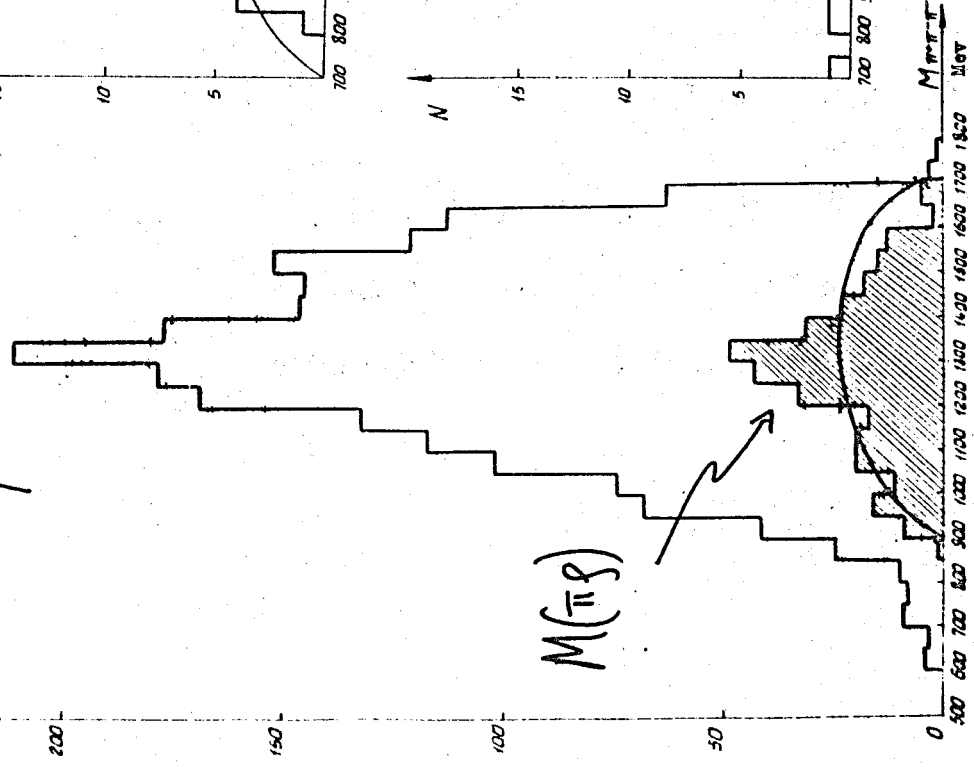
BARNES et al. $K^- p$ 4.6, 5.0 BeV/c



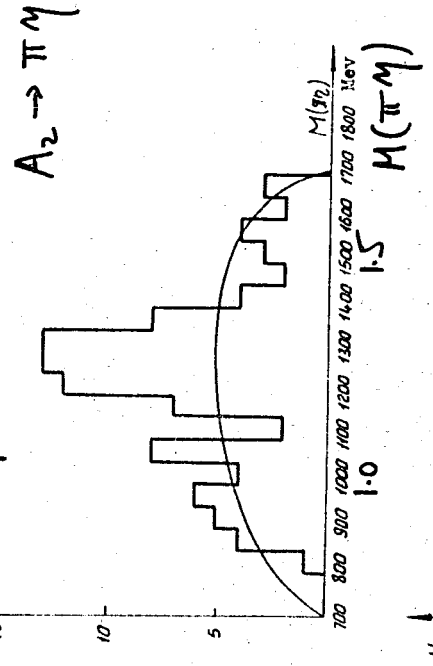
14

ADDITIONAL EVIDENCE ON THE $\pi\eta$ DECAY MODE

DUBOVIKOV et al (MOSCOW)
 $\pi^- p$ 3.25 GeV/c

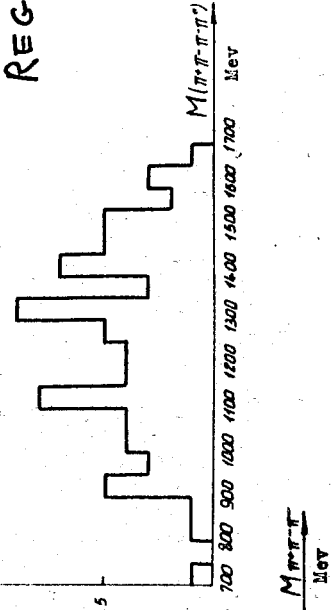


15

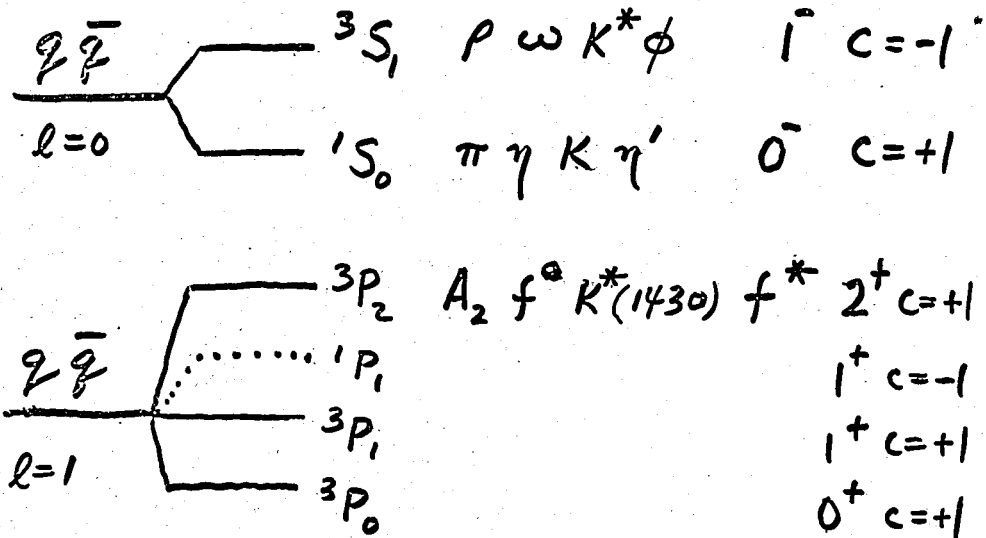


$A_2 \rightarrow \pi\eta$

CONTROL REGION



$q\bar{q}$ MODEL

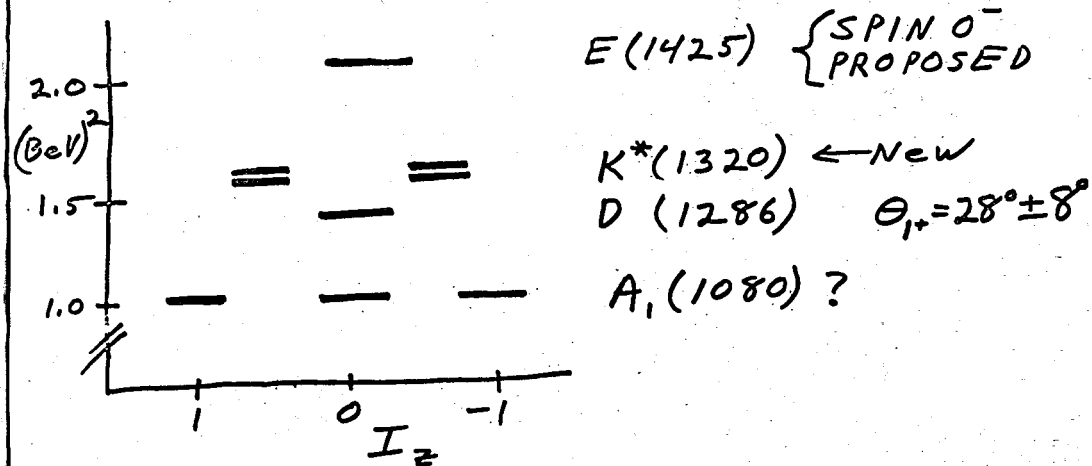


TO GET 2^- WE NEED $l=2\ q\bar{q}$
 OR "ABNORMAL MODES"
 i.e. $qq\bar{q}\bar{q}$ SYSTEMS

!! SPECULATIVE !!

$J^P = 1^+$ NONET(?)

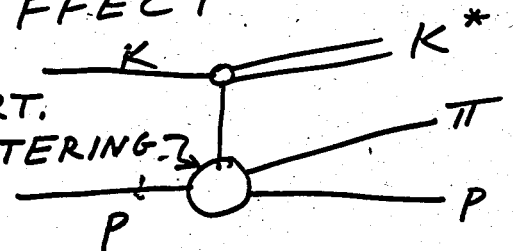
$C = +1$ $3P_1(8\bar{8})$



- ① $K^*(1320) \rightarrow K^*(890) + \pi$] INTERFERENCE
 $\rightarrow \rho K$
 $\rightarrow \omega K$
 $\rightarrow K\pi$

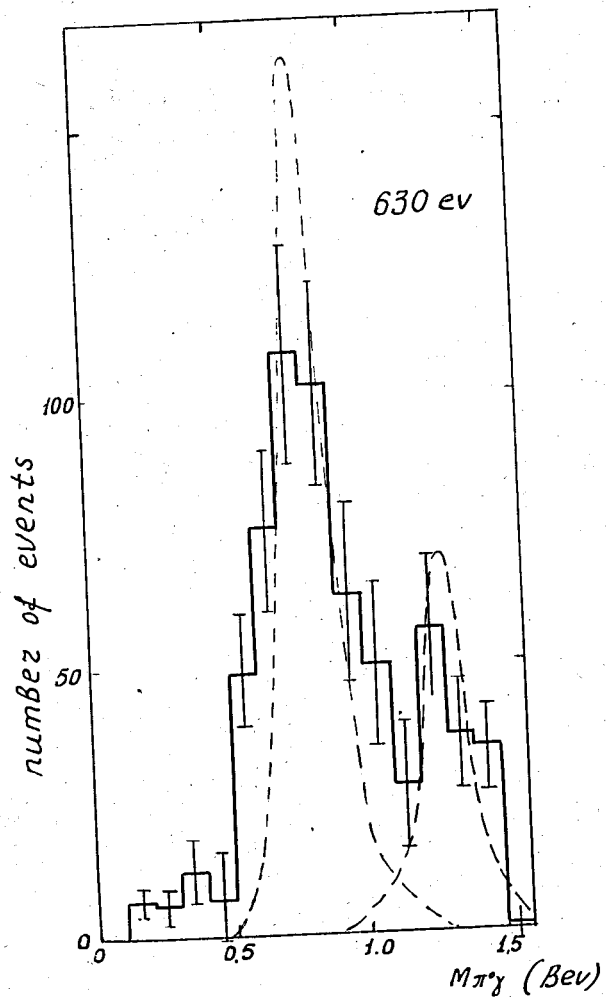
② DECK EFFECT

DRELL-VIRT.
 PION SCATTERING

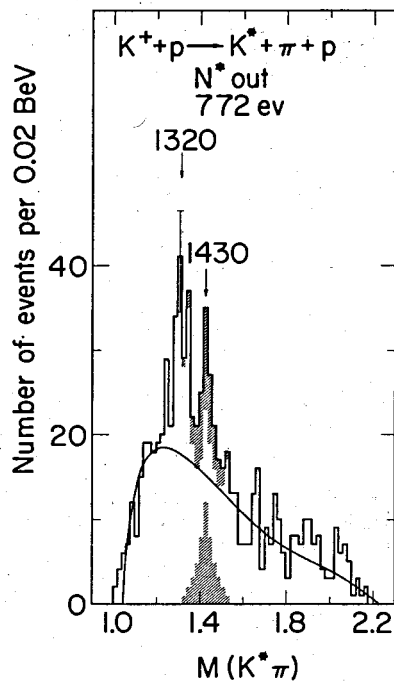


Barmin et al.

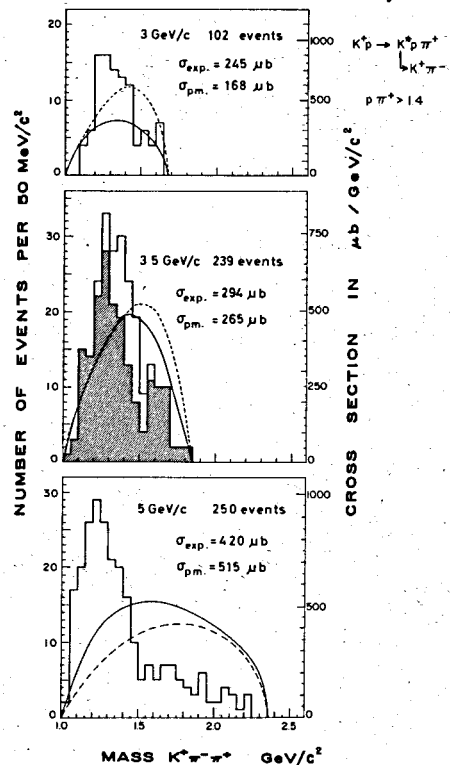
$\pi^- p \rightarrow n + \pi^0 \gamma$ at 2.8 GeV/c
(Propane-Xenon B.C.)



SHEN et al. $K^+ p$ 4.6 BeV/c



de BAERE et al. $K^+ p$



K* (1320) and K* (1430) PRODUCTION

An interesting phenomenon has been observed relating to K* (1320) and K* (1430) production in the K⁻p reaction.

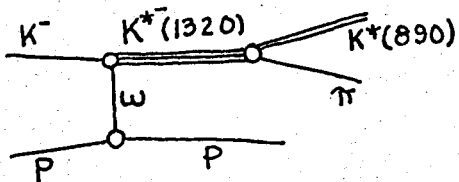


There is evidence for K* (1430) production in all of these but K* (1320) is not produced in the charge exchange reaction (3).

There are two possible explanations:

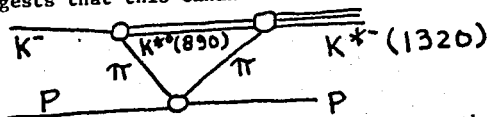
A. K* (1320) production proceeds predominantly via isoscalar (ω) exchange.

exchange.



This is not available in charge exchange

B. A proposal by Morrison suggests a diagram involving the Drell process, i.e., virtual pion scattering at the nucleon vertex. He suggests that this enhances resonance formation.



This is suppressed for charge exchange at the lower vertex.

Evidence for this effect comes from DORNAN et al, K⁻p 4.6 BeV/c,

B, G, IC(L), M, O, R L

6 GeV/c,

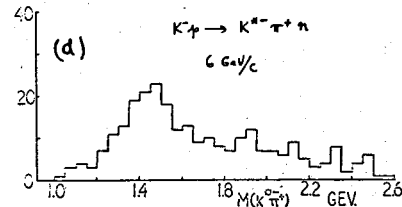
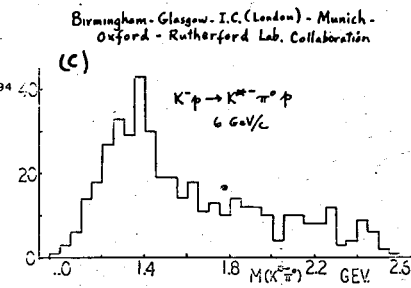
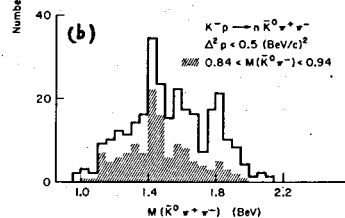
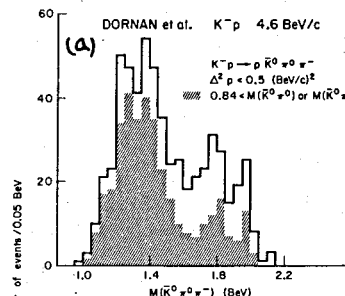
Argonne

4 + 5 GeV/c,

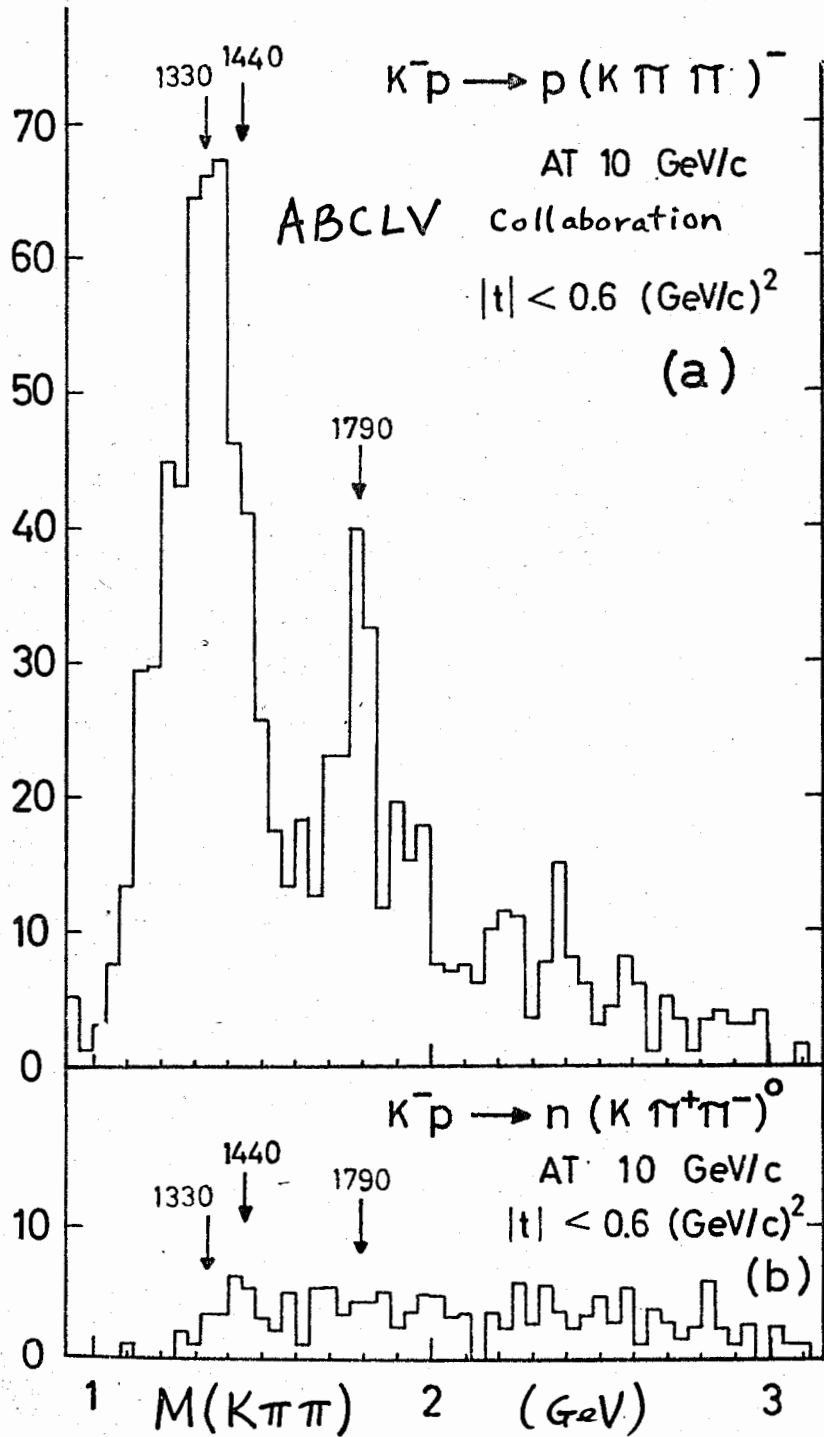
and particularly clear cut from

ABCLV

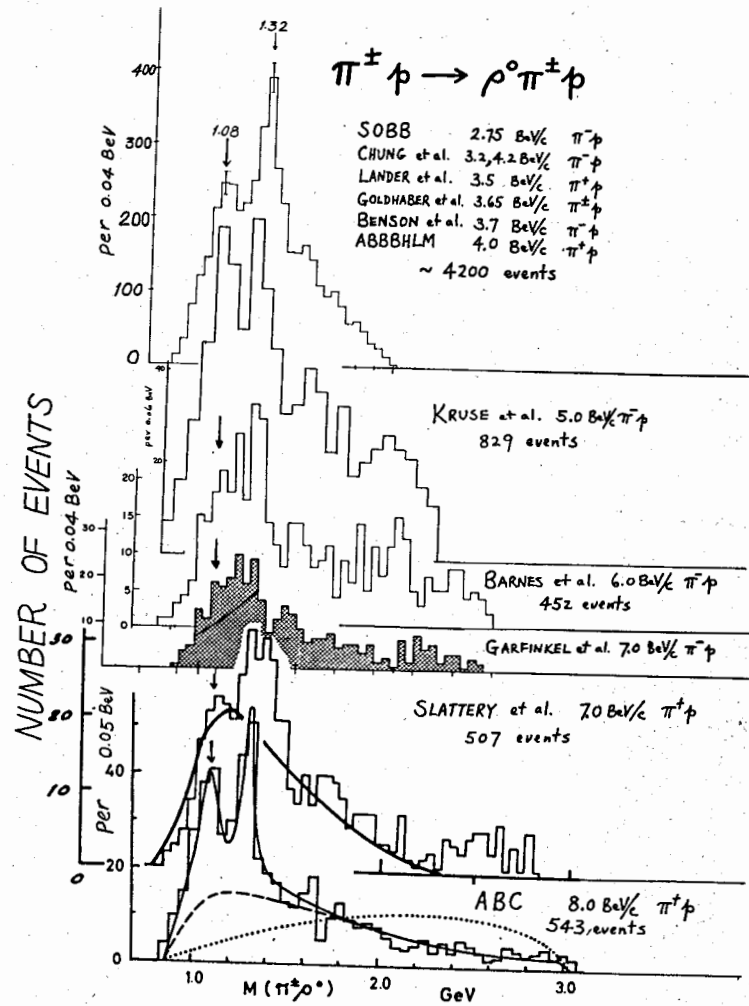
10 GeV/c



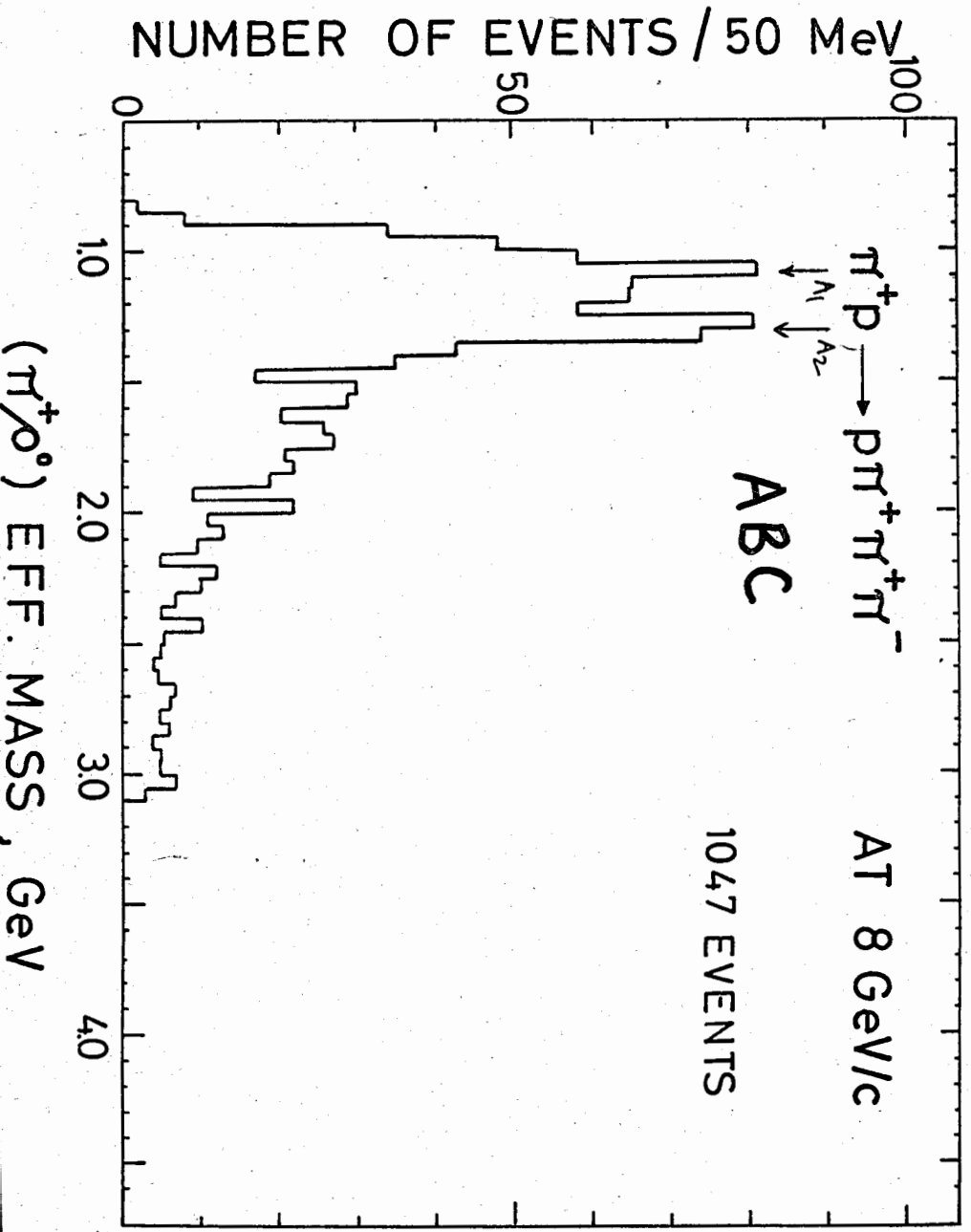
NUMBER OF EVENTS / 40 MeV



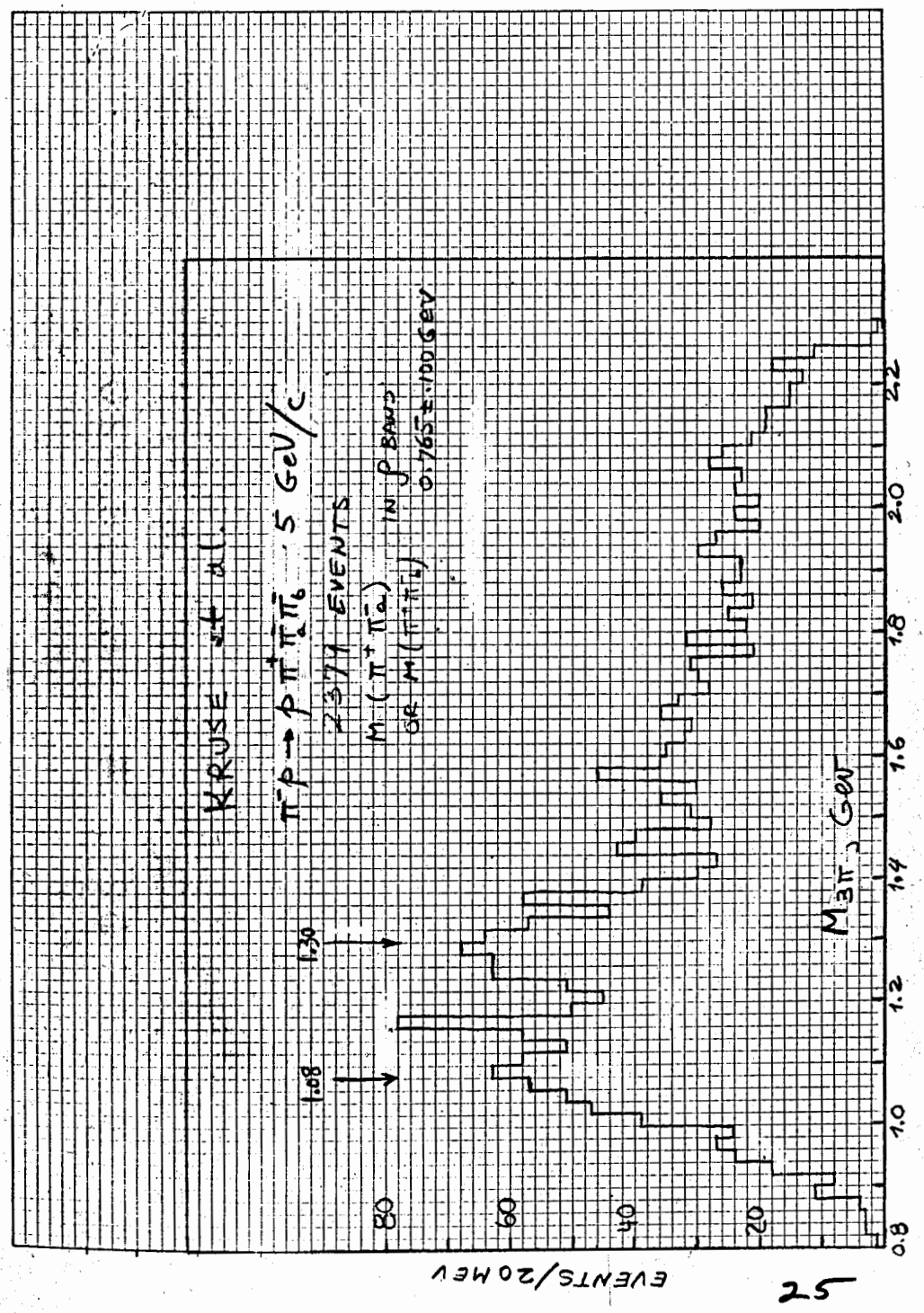
22



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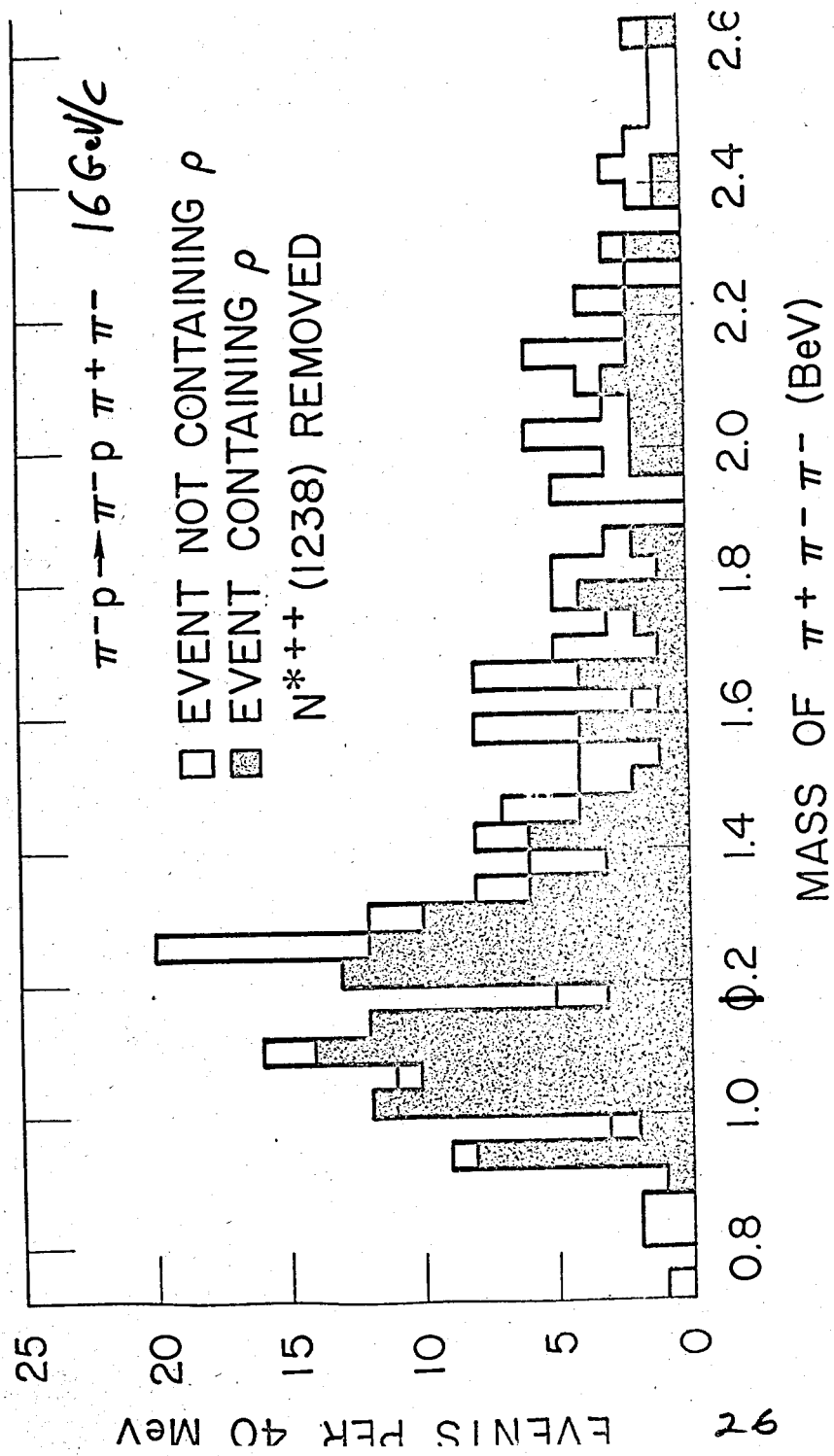


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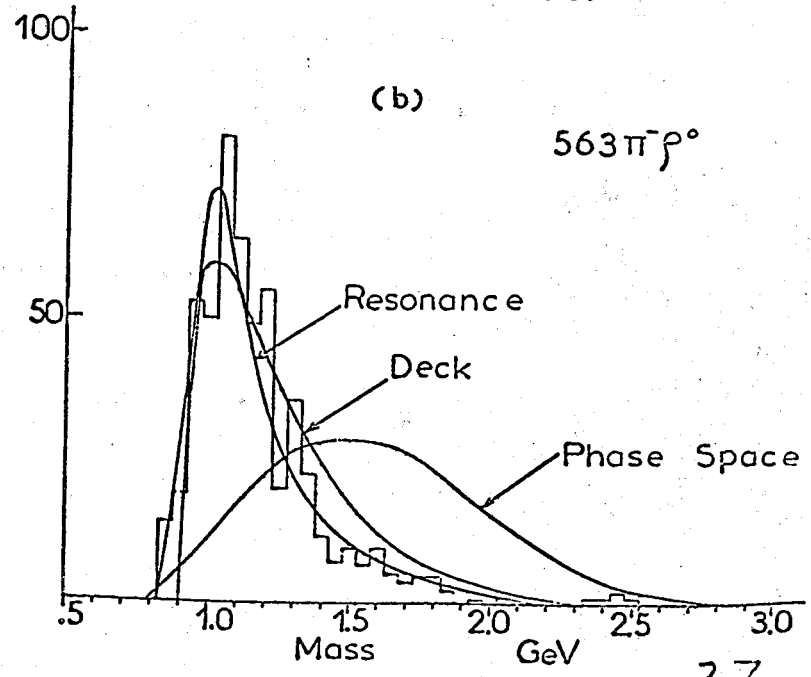
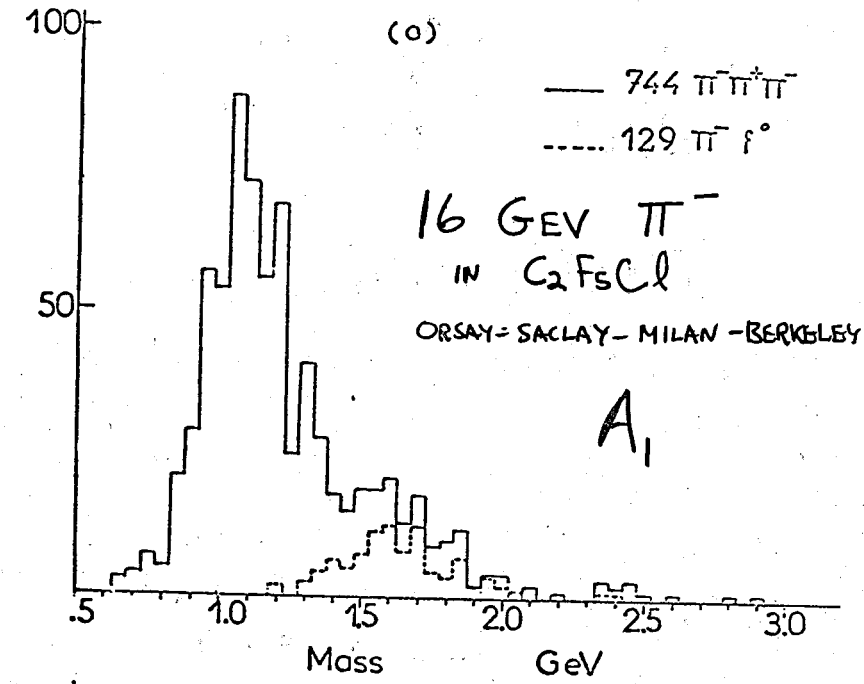


25

BALLAM et al.



no of events / .05 GeV



$$J^P = 0^+$$

$$C = +1 \quad {}^3P_0 (\eta \bar{\eta})$$

WHERE IS IT?

① $S^*(1068) \rightarrow K, K, \quad I=0, J^{PC} = 0^{++}$

RESONANCE OR SCAT LENGTH?

$$M = 1068$$

$$P = 80$$

$$Q = 2 + i0.2 \text{ F}$$

$$T \rightarrow 3.3 + i0.2$$

② $S_0(720)$ NOT CONVINCINGLY CONFIRMED YET

③ $K \neq K, (\sim 1000) \quad I=1, J^{PC} = 0^{+-} ?$
SCAT LENGTH?

④ $\kappa(720)$ SHARP κ ($P < 20$)

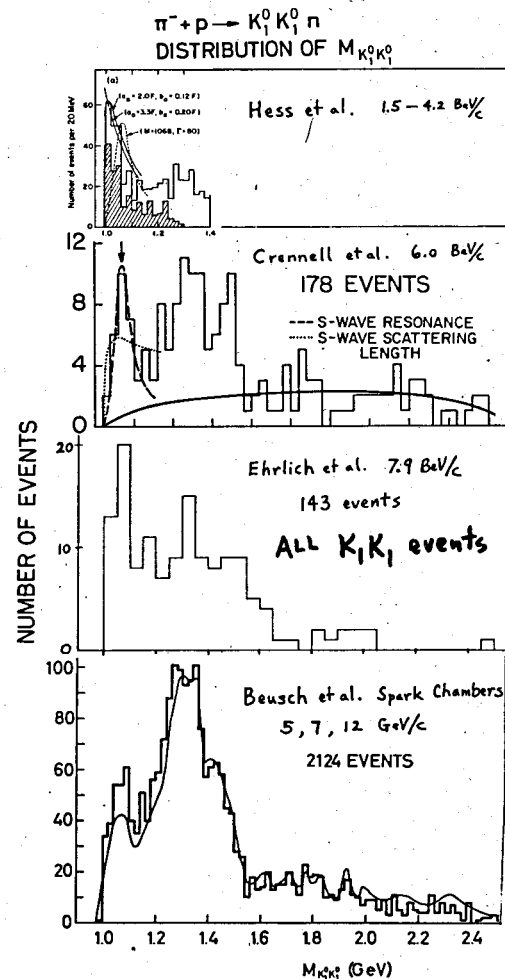
DISPROVED. WIDE EFFECT

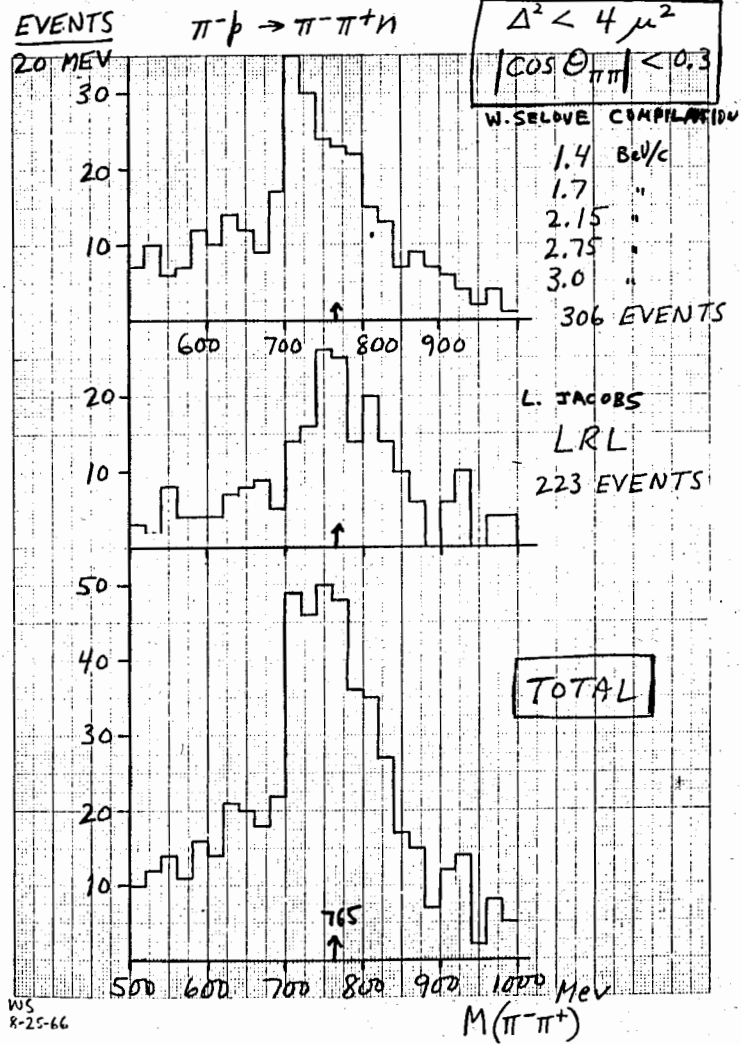
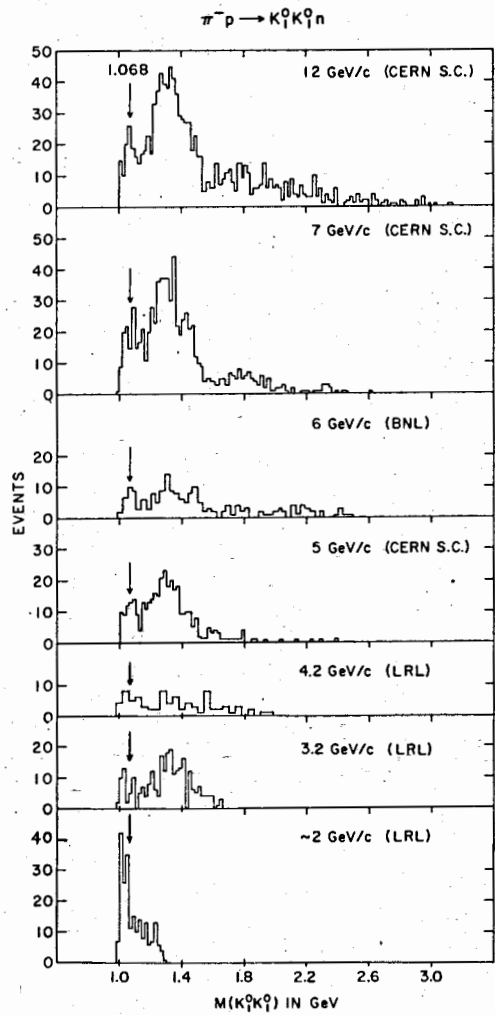
$P \sim 50 \text{ MEV}$ MAY BE PRESENT

COULD BE INTERFERENCE

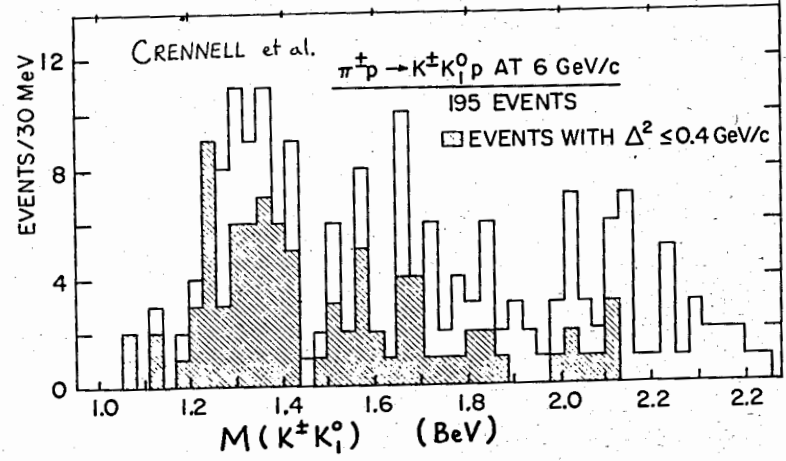
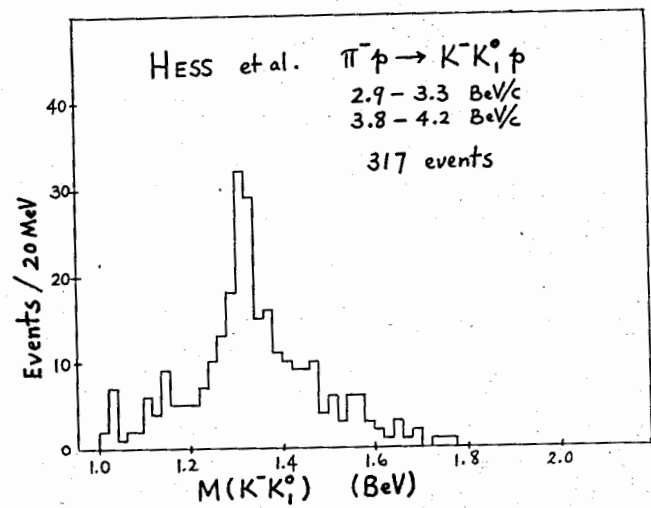
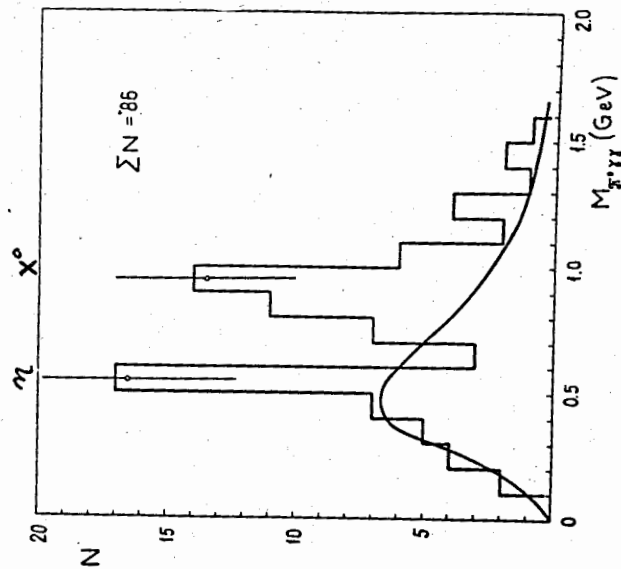
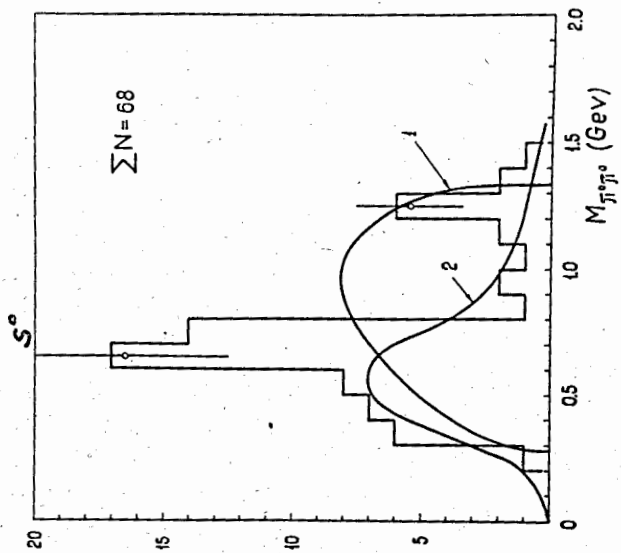
$K\pi$ WITH $N\pi$ BAND

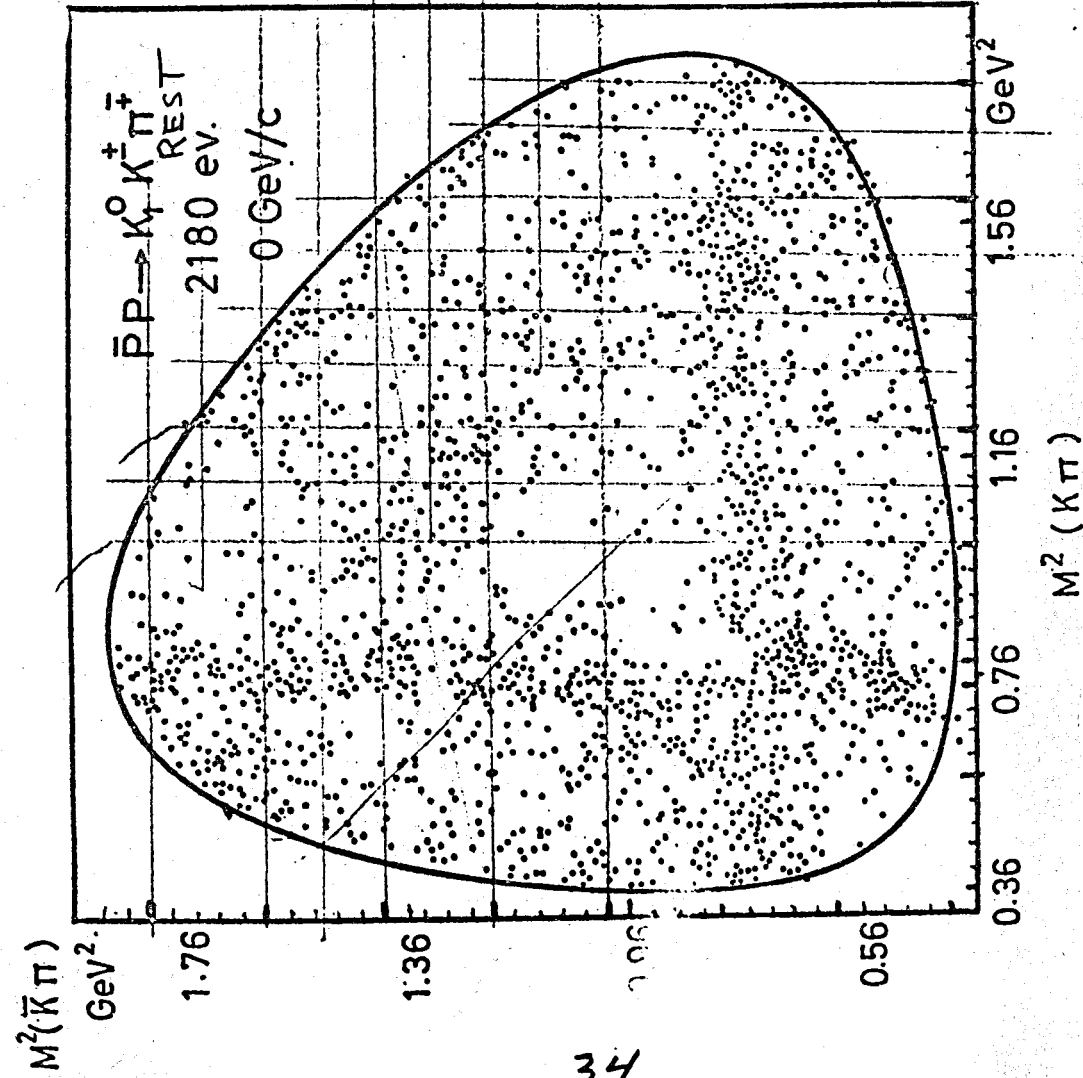
SAME GOES FOR $\sigma(400)$



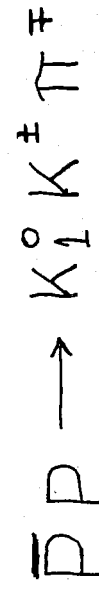


STRUGALSKI et al (Dubna)
Xenon Bubble Chamber



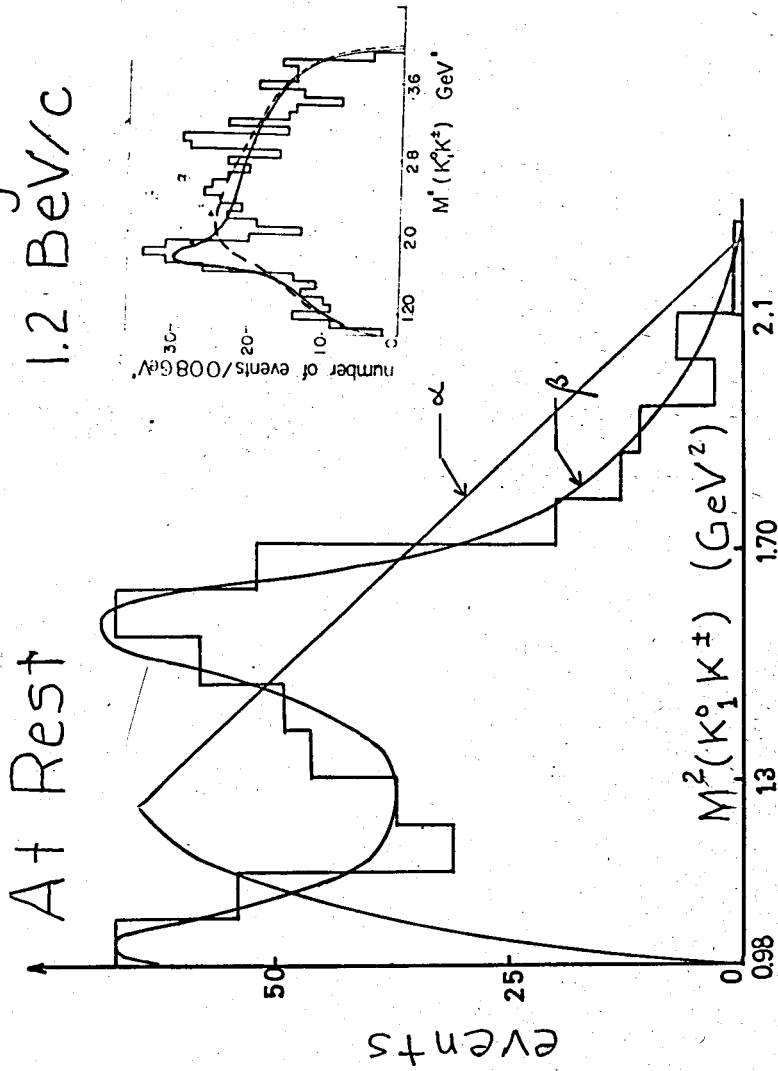


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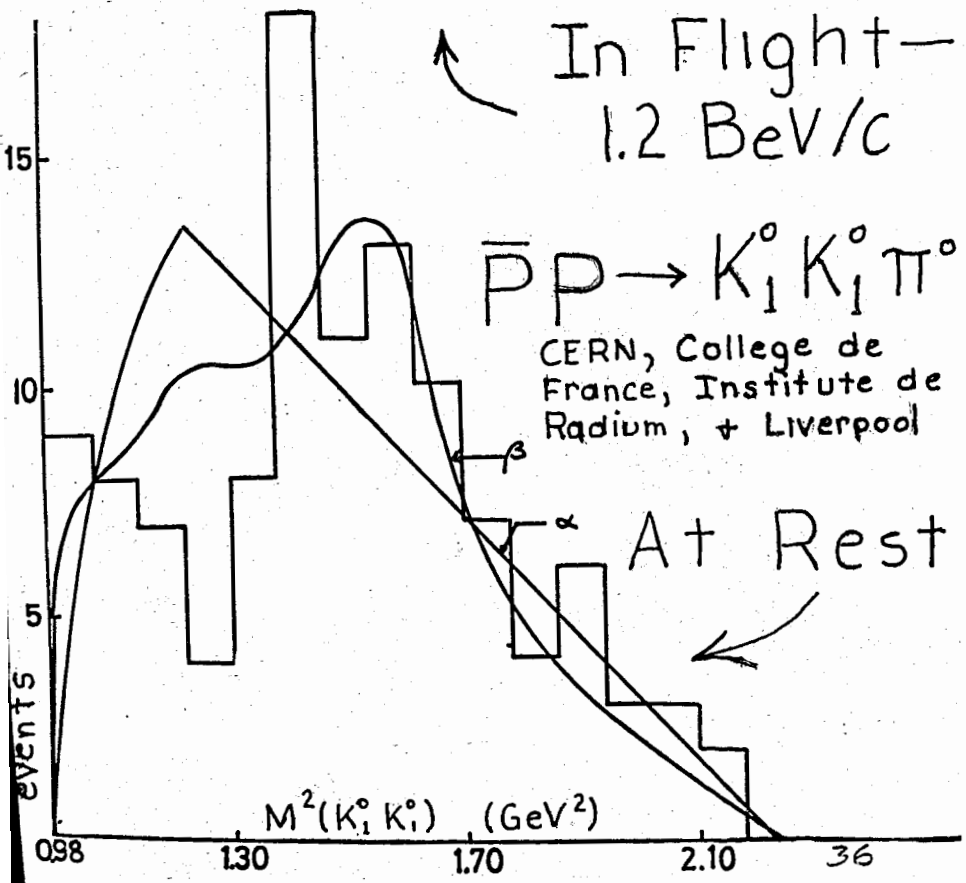
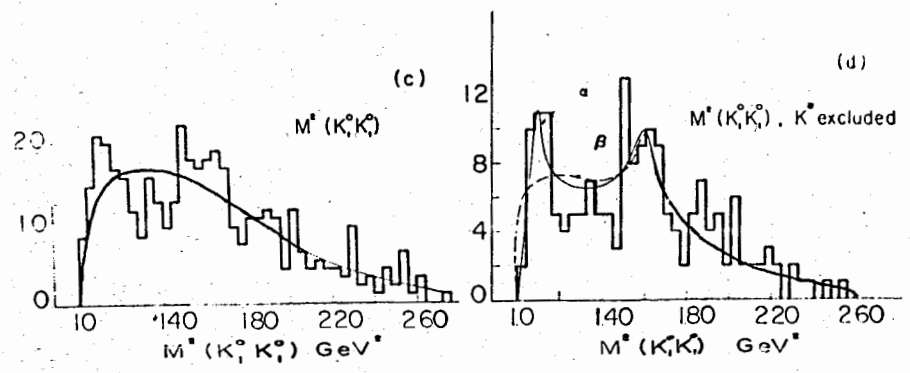
CERN, College de France, Institute de Radium, & Liverpool

At Rest
In Flight -
1.2 BeV/c



35

events / 0.04 GeV²

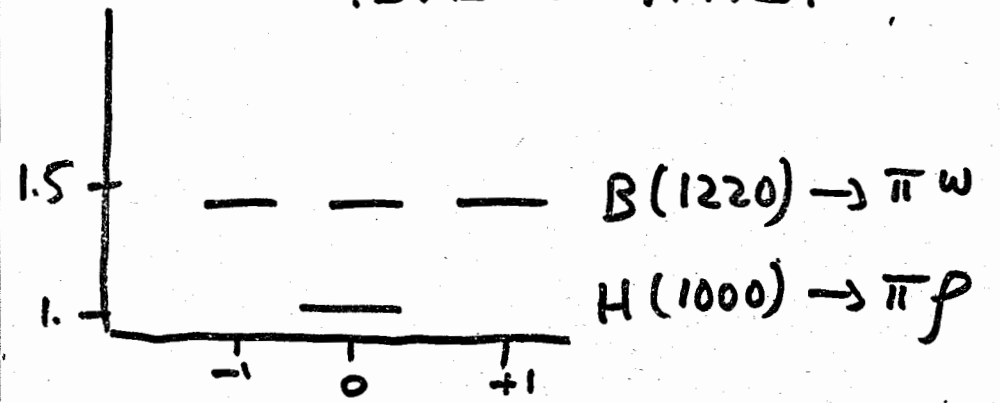


In Flight -
1.2 BeV/c

$\bar{P}P \rightarrow K^0_1 K^0_1 \pi^0$
CERN, College de
France, Institute de
Radium, + Liverpool

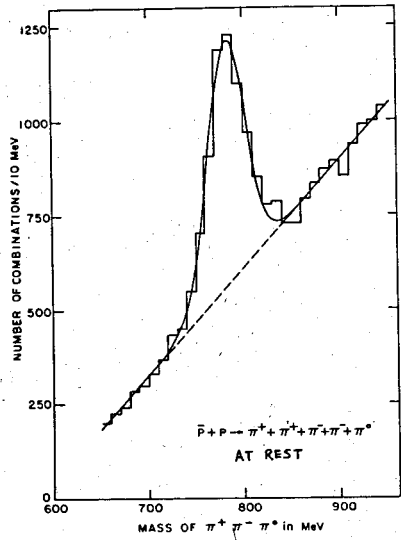
At Rest

$J^P = 1^+$
 $C = -1$ $^1P_1(q\bar{q})$ } $J^P = 2^-$ $^3D_2(q\bar{q})$
! SPECULATIVE!

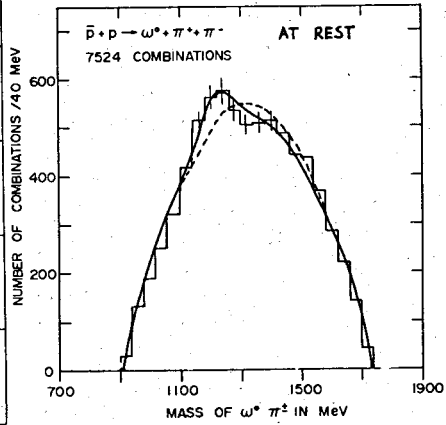


- ① B REVIVED $\bar{p}p \rightarrow B^\pm + \pi^\mp$
- ② H CONFIRMED $\pi^+ d \rightarrow H^0 p p$
Seen at 3.65 BeV/c
NOT at 5.1 BeV/c

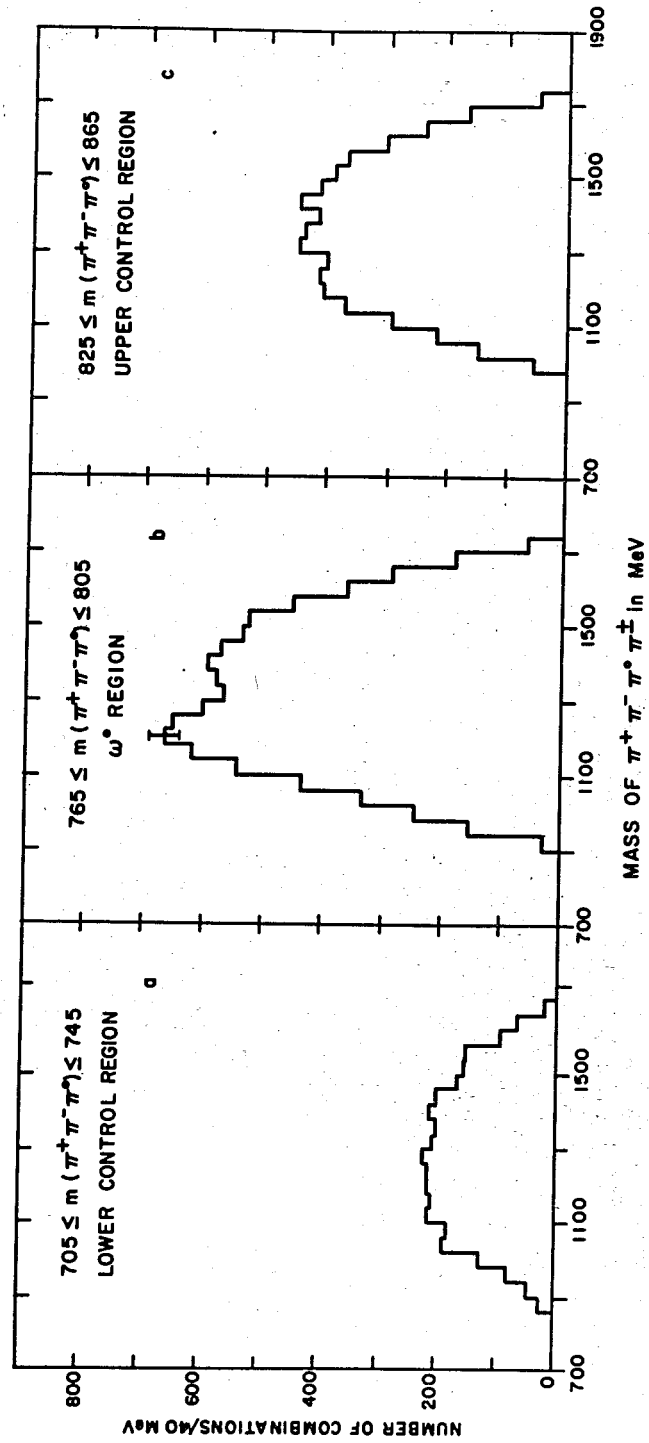
IF NO MIXING G-M=0
REQUIRES $M(K^*) = 1060$ MeV

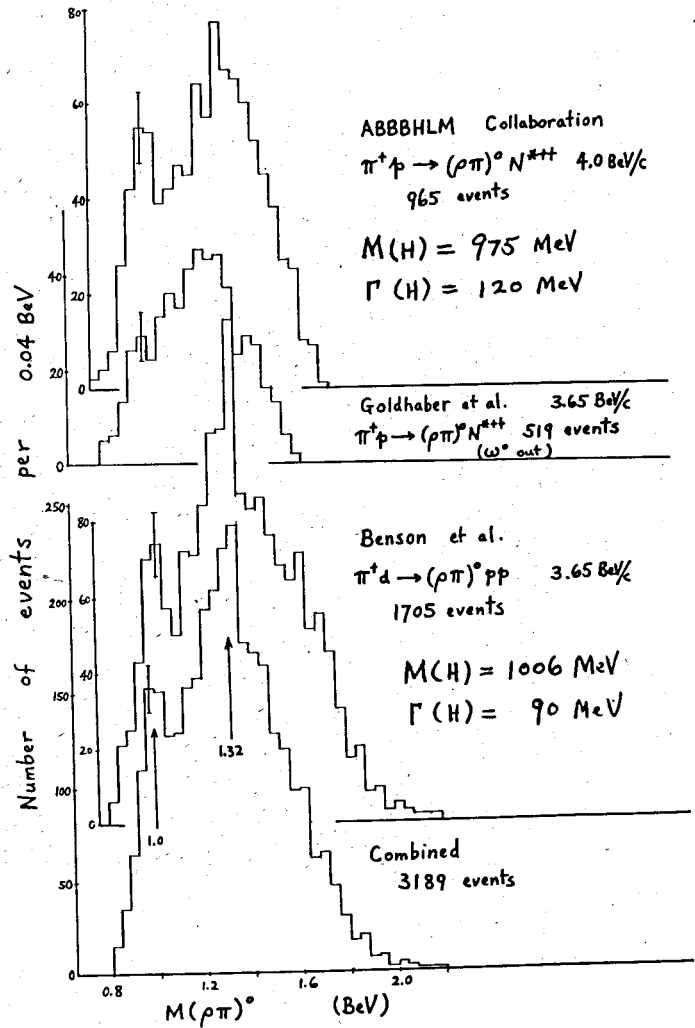


BALTAY et al.

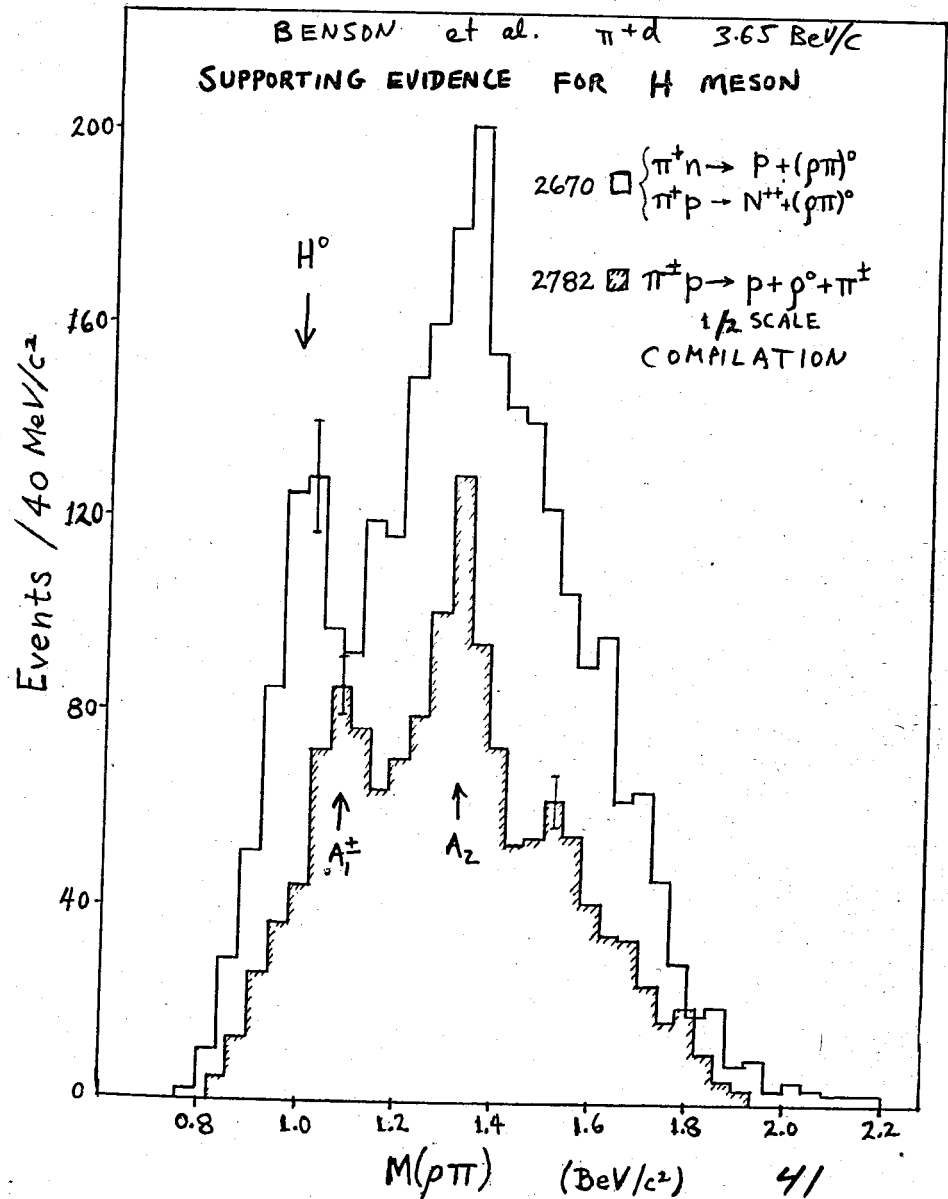


BALTAY et al. $\bar{p}p$ at REST





40



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BARI-BOLOGNE - FLORENCE

$\pi^+ d \rightarrow p, p, \pi^+ \pi^+ \pi^0$ 5.1 GeV/c

ρ selected, N^* 's removed

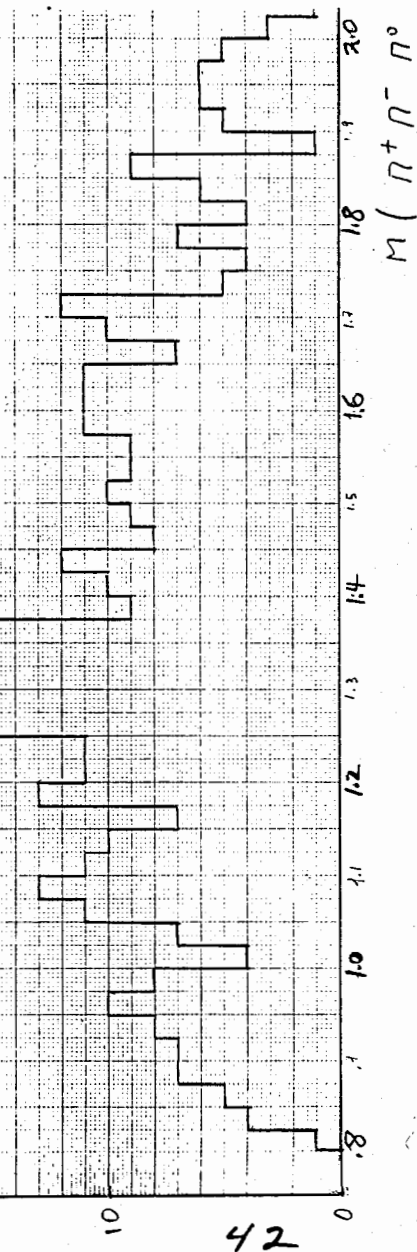
501 events

$A_2^0 \rightarrow \pi f$

No evidence for

H

1640 MeV
0.25 GeV



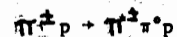
The $M = 1650$ MeV Region, $S = 0$

It has become clear at this conference that there are two or more objects located at this general mass region.

1. The g meson $G = +1$ $I \geq 0$

a. There is overwhelming evidence that in the $\pi^+ \pi^-$ mass spectrum there exists a structure beyond the very prominent ρ and f^0 peaks. This comes from $\pi^- p \rightarrow \pi^+ \pi^- n$ and $\pi^+ d \rightarrow \pi^+ \pi^- p$ at a series of energies.

b. From the reactions



there is evidence (not 100% established) for an enhancement at ~ 1620 MeV. This would be $G = +1, I \geq 1$

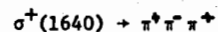
c. Some evidence has been presented for $(1680)^- \rightarrow \pi \pi \pi \pi$

Conte et al.

$\rightarrow \rho \pi \pi$ 75%

$\rightarrow \rho \rho$? <40%

2. The σ (1640) "meson," $G = -1, I \geq 1$. A compilation of 3 sets of data on $\pi^+ p \rightarrow \pi^+ \pi^- \pi^+ p$ from 7 - 8.5 GeV/c shows an enhancement 1640 MeV.

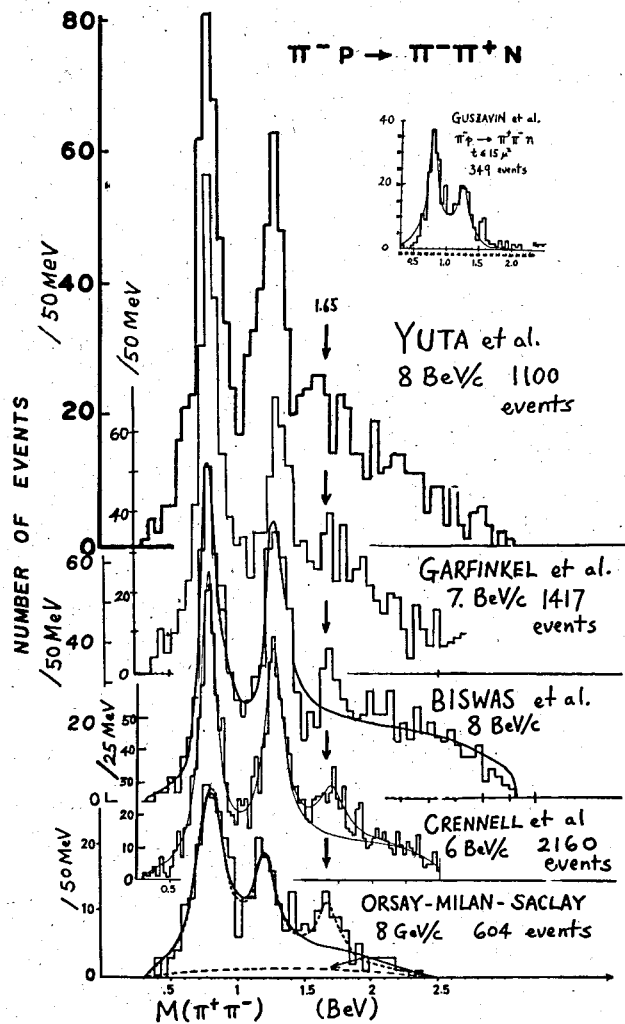


$\rightarrow \rho^0 \pi^+$ (very little)

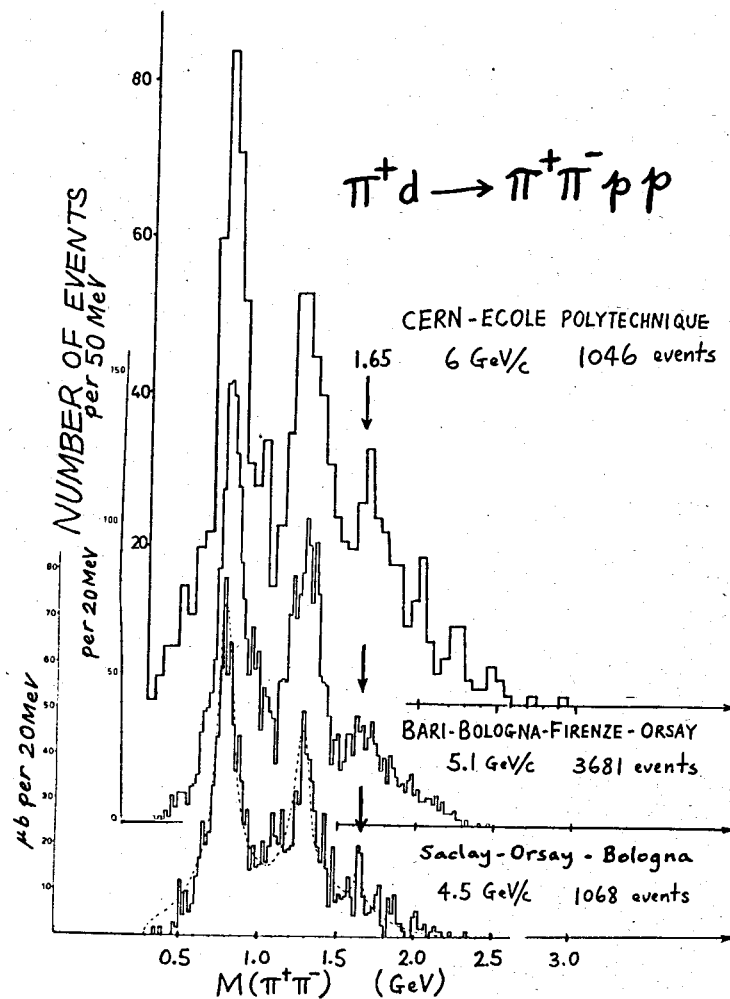
$\rightarrow f^0 \pi^+$

$$M(\sigma) = 1640 \pm 15, \Gamma(\sigma) \approx 100$$

A very similar result is also presented by Guzavin from 4.7 GeV/c $\bar{W} p$. As always the suggestion comes to mind that this is related to the Deck effect with f^0 production this time. In fact, a suggestion of such an enhancement was observed in the 16 GeV/c \bar{W} nucleus data in the E.P. heavy liquid chamber.

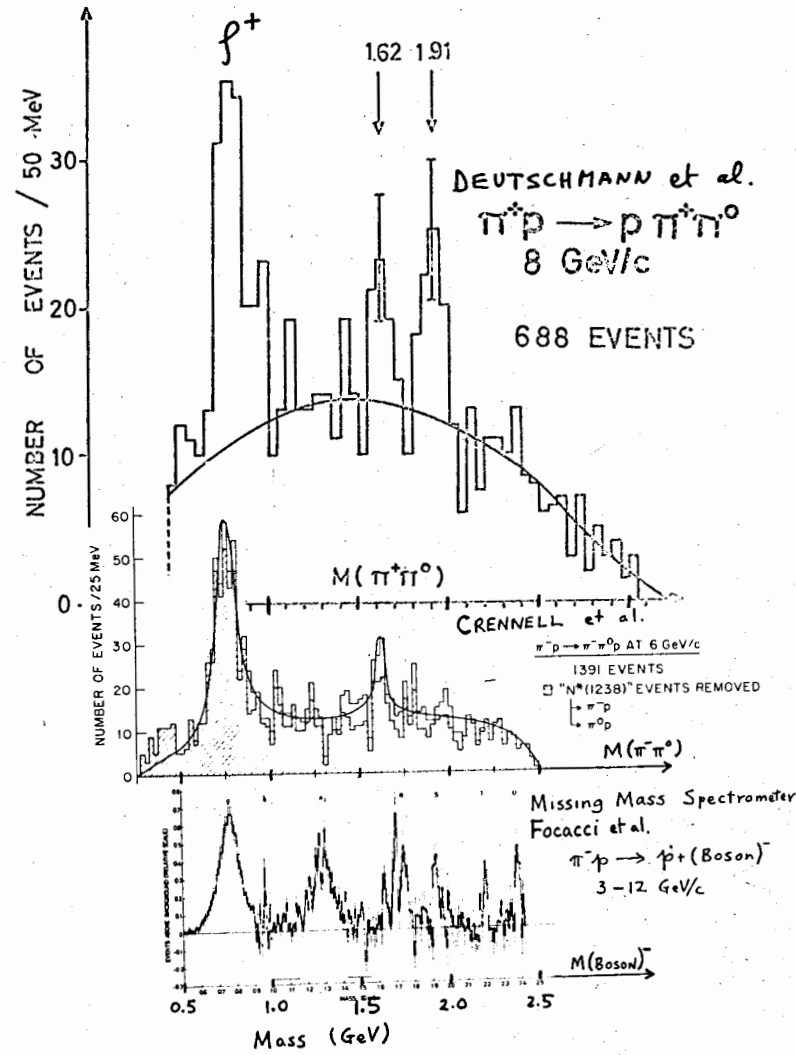
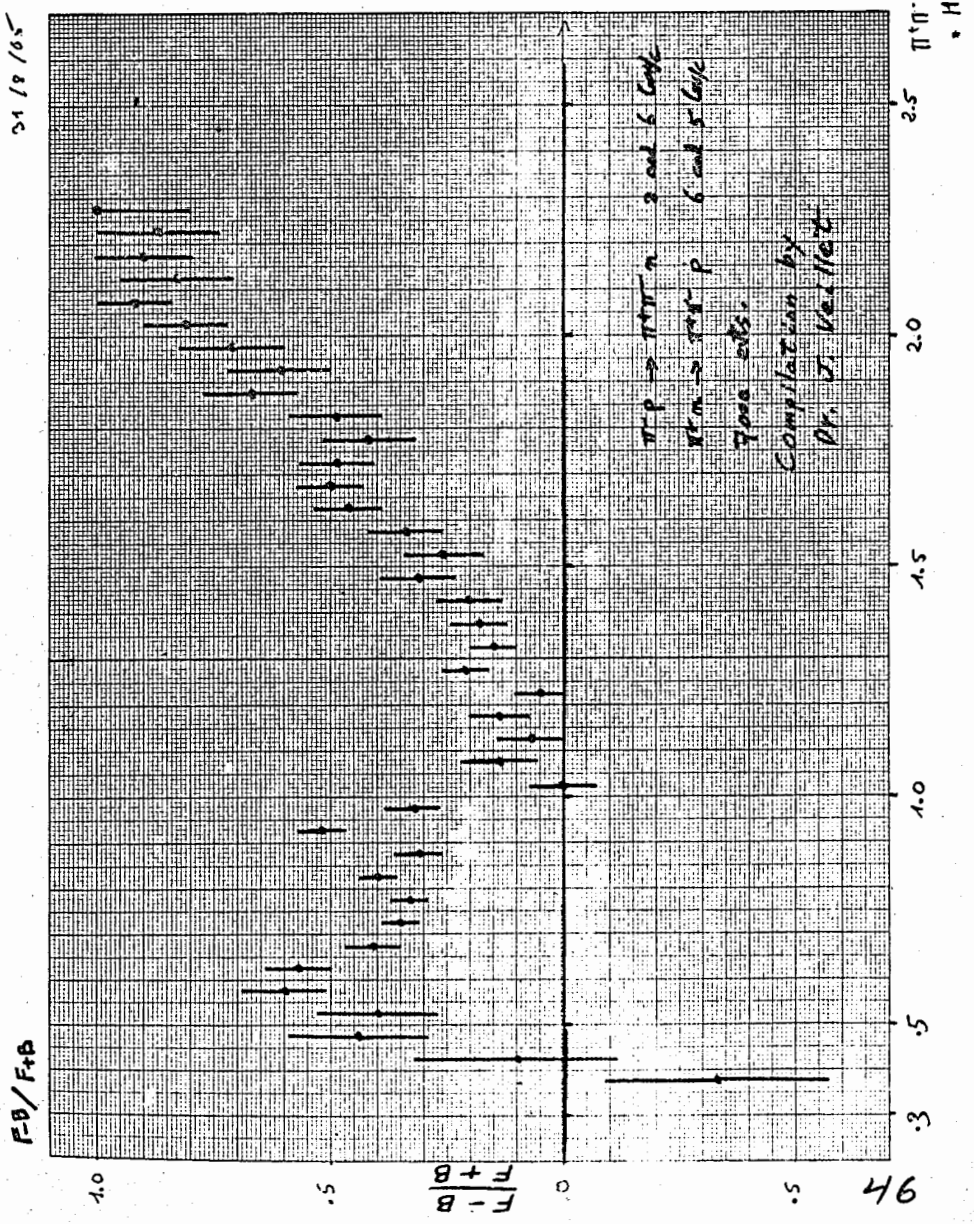


44



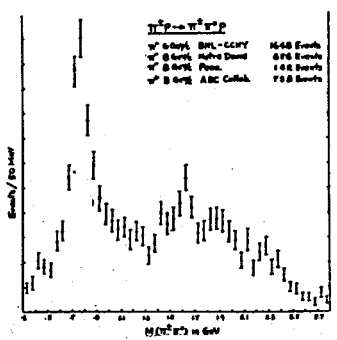
45

31/10/65



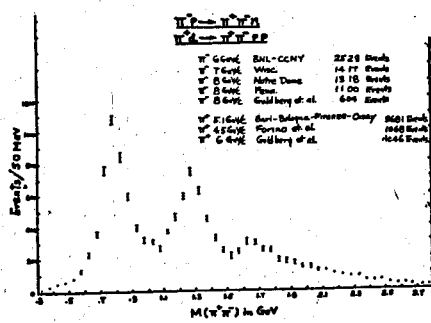
COMPILATION

$\pi^{\pm}\pi^0$

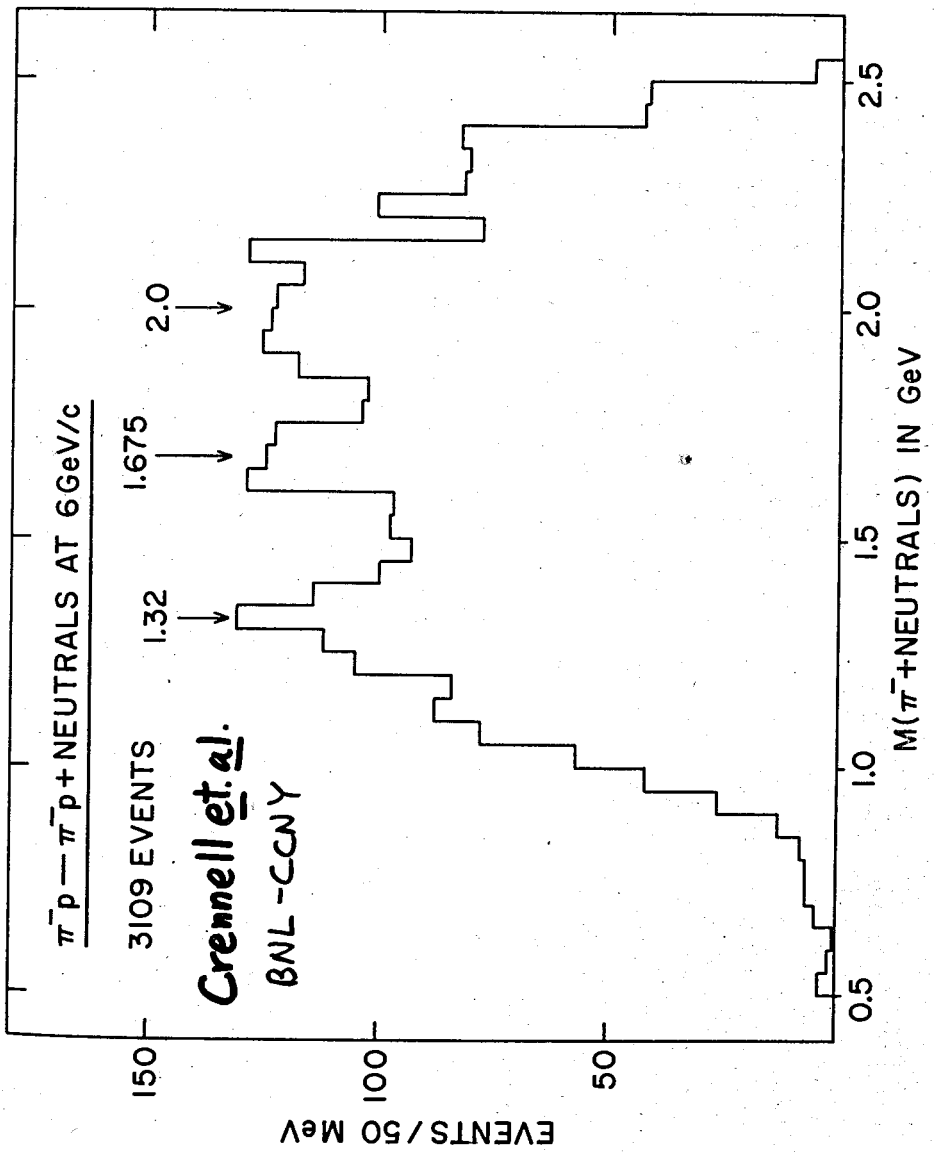


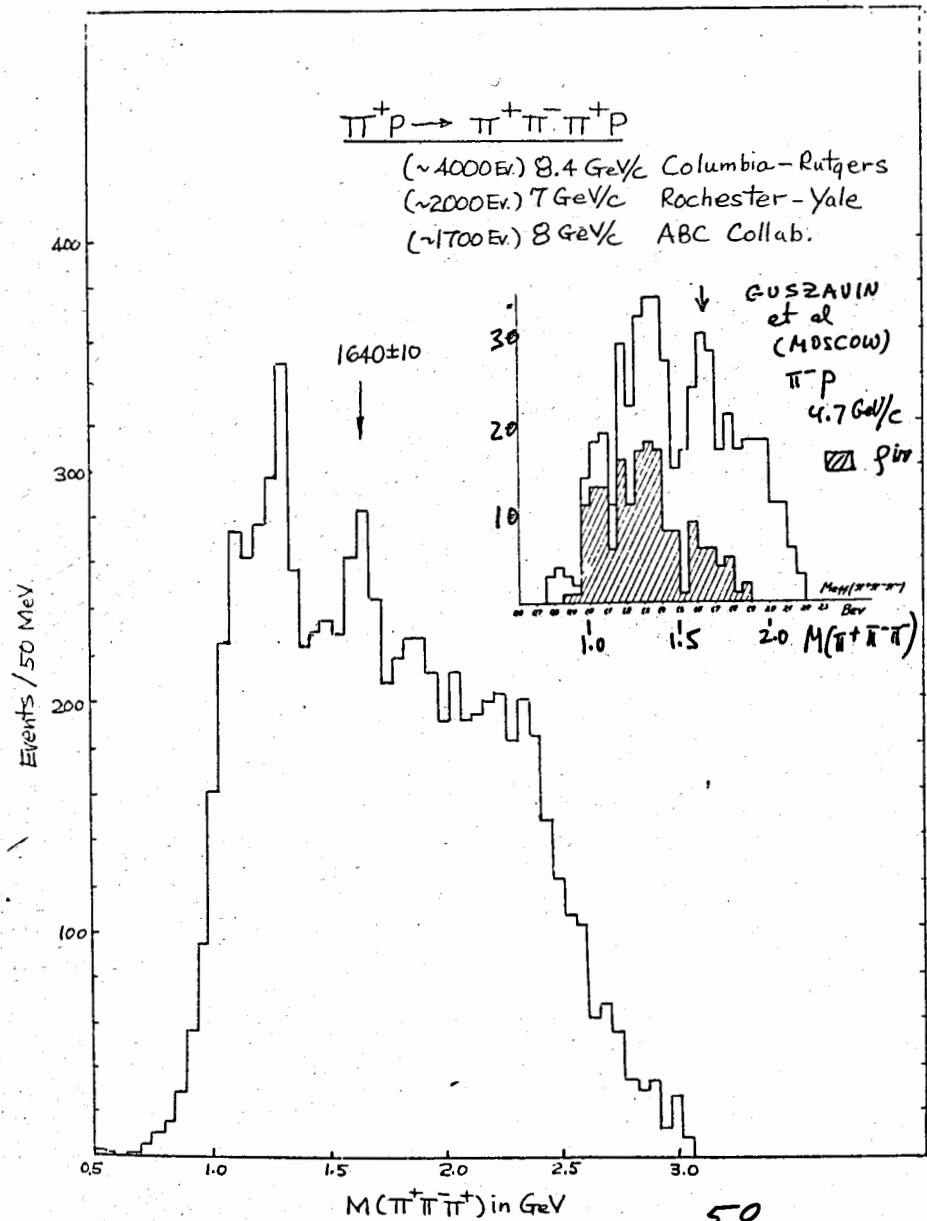
ρ^{\pm} ↑

$\pi^+\pi^-$



↑ f^0
↑ f^0
↑ g^0





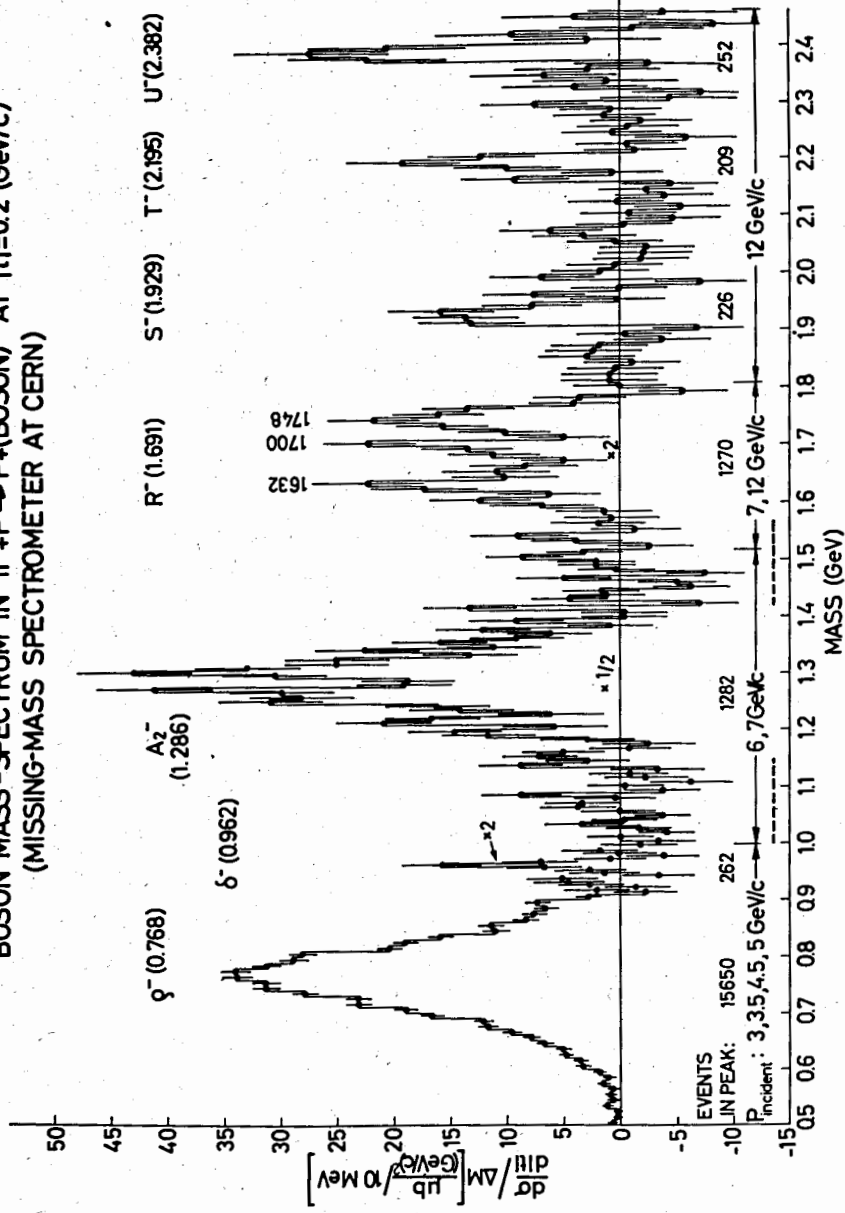
50

$S=0$ Pion Resonances
 in the Mass Region of 1.65 GeV

$G = +1$		$G = -1$		$G = \text{Unknown}$	
$I \geq 0$	$I \geq 1$	$I \geq 1$	$I \geq 1$	m	Γ
m	Γ	m	Γ	m	Γ
1675 ± 30 (Goldberg et al.)	200 ± 50 (Crennell et al.)	1640 ± 10 (ABC, Columbia-Rutgers, Rochester-Yale)	100 ± 10	1632 ± 10	34 ± 3
1650 (BBFO)	1620 (Deutschmann et al.)	1630 ± 30 ~ 100 (Guszevin et al.)	~ 100	1699 ± 10	30 ± 3
1700 ~ 200 (Crennell et al.)	1680			1748 ± 10	28 ± 3
1670 ± 20 (Biswas et al.)	160 (Conte et al.)				
1610 ± 40 (Kernan et al.)	155 ± 85 (Kernan et al.)				
				1675	~ 200 (Crennell et al.)

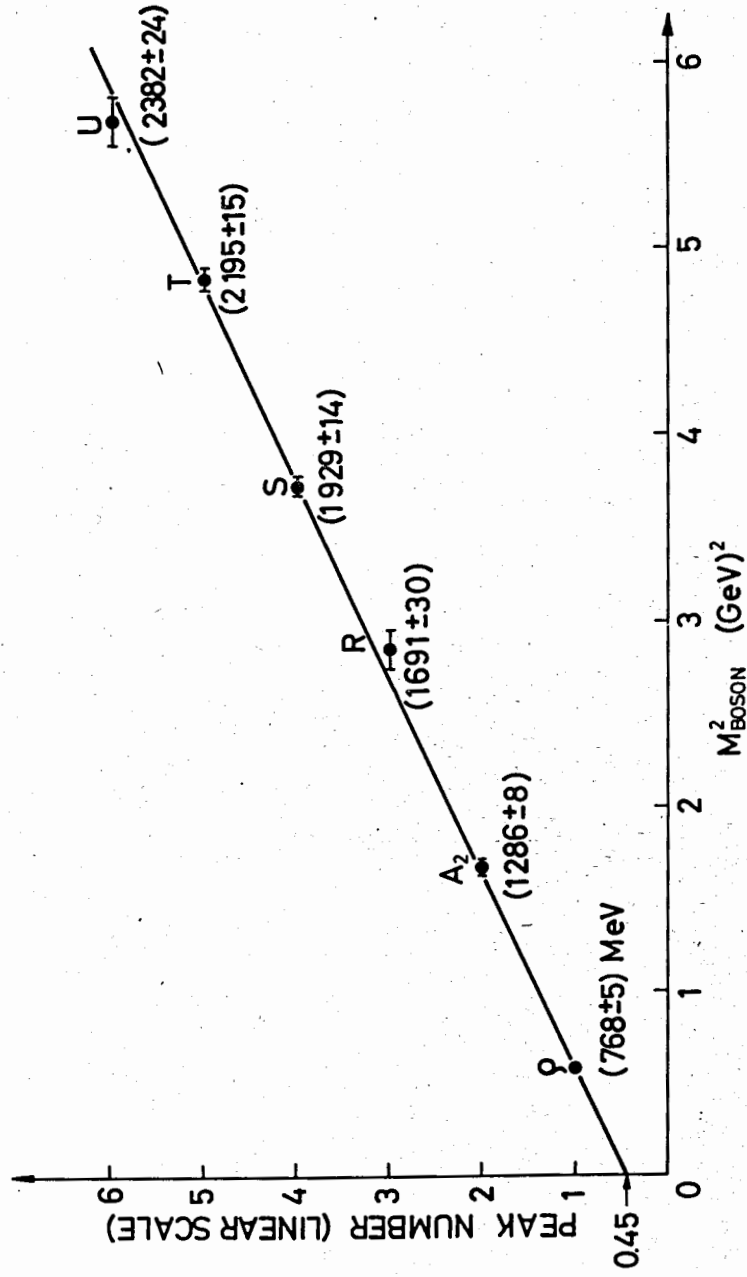
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BOSON MASS - SPECTRUM IN $\pi^+P \rightarrow P^+(\text{BOSON})\pi^-$ AT $\langle t \rangle = 0.2$ (GeV/c)²
(MISSING-MASS SPECTROMETER AT CERN)



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FOCACCI et al.



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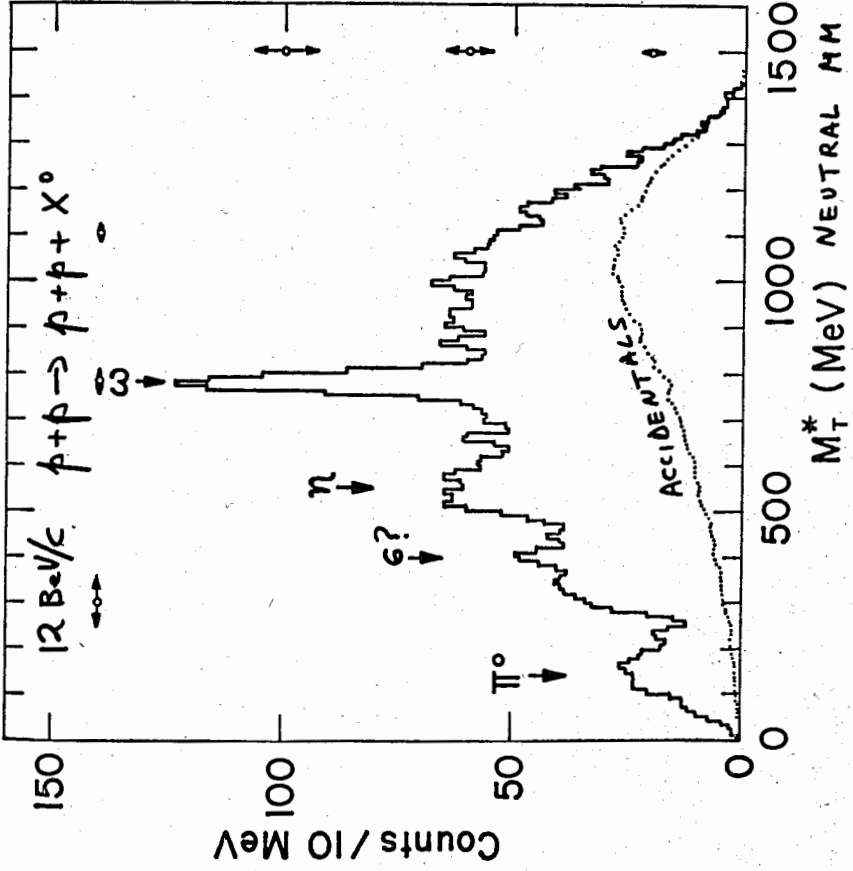
BOSON MISSING MASS SPECTROMETER CERN

Mass	Mass M (MeV)	Exp. resolution (MeV)	Physical width Γ (MeV)	F_1 ($\pm 1\%$)	Statistical significance (standard deviations)	No. of events in peak in Fig. 1	Signal/background***	t limits (GeV/c) ²	t limits in the t limits $s^{1/2}/(\text{GeV}/c)^2$	Beam mode	Reference
ρ^-	768 ± 5	20 ± 5	127 ± 5	3.0 3.5 4.5 5.0		$15,600 \pm 170$	1.6 ± 1.1	$0.10 - 0.14$ $0.14 - 0.17$ $0.17 - 0.22$ $0.22 - 0.28$	770 ± 150 770 ± 170 80 ± 110 370 ± 110	$10 > 97.4\%$	1,2
ρ^+	962.5 ± 5	24 ± 4	6.5	3.0 3.5 4.5 5.0	5.0	262 ± 52	1.1 ± 1.5	$0.11 < t < 0.21$	$6.9 \pm 3^{**}$	$\frac{10}{36} = 1.5 \pm 0.9$ $\frac{36}{30} = 1.05 \pm 0.1$	4,5
A_2^+	1286 ± 8	36 ± 4	90 ± 5	6.0 7.0	17	1282 ± 65	1.1 ± 1.5	$0.31 < t < 0.39$	400 ± 120	$\frac{10}{30}$	5
A_2^-	1300 ± 10 1312 ± 10			6.0 7.0	1 peak and 2 parameters $p = 5\% - 10\%$	A_2^+ $A_2^- = 11$	1.1 ± 1.6 1.1 ± 1.6			$\frac{10}{30} = 1$	9
π^-	1691 ± 15	31 ± 3	116 ± 3	7.0 12.0	13.5 1 peak; $p = 1\%$ $2 = 1\%$ $3 = 1\%$ $p = 20-60\%$ (31, 21, 3)	1270 ± 94	1.1 ± 1.6	$0.23 < t < 0.28$	195 ± 30	$\frac{10}{30} = 0.30 \pm 0.05$ $\frac{30}{30} = 0.67 \pm 0.10$ $\frac{30}{30} = 0.95 \pm 0.05$	7,9
π_1	1632 ± 15	34 ± 3	≤ 21		5	360 ± 70 485 ± 70 425 ± 70	1.1 ± 1.7 1.1 ± 1.3 1.1 ± 1.5		35 ± 10 43 47	$\frac{10}{30} = 0.37 \pm 0.13$ $\frac{30}{30} = 0.62 \pm 0.04$ $\frac{10}{30} = 0.42 \pm 0.11$ $\frac{30}{30} = 0.56 \pm 0.14$ $\frac{30}{30} = 0.61 \pm 0.01$ $\frac{10}{30} = 0.14 \pm 0.06$ $\frac{30}{30} = 0.80 \pm 0.18$ $\frac{30}{30} = 0.95 \pm 0.05$	9
π^+	1700 ± 15	30 ± 3	≤ 30	7.0 12.0	6.6						9
π_3	1760 ± 15	20 ± 3	≤ 38		6.1						9
ω	1929 ± 14	22 ± 2	5.35	12.0	5.5	226 ± 41	1.1 ± 1.7	$0.22 < t < 0.26$	35 ± 12	$\frac{10}{30} = 0.06 \pm 0.15$ $\frac{30}{30} = 0.27 \pm 0.06$ $\frac{30}{30} = 0.92 \pm 0.20$ $\frac{30}{30} = 0.13 \pm 0.13$ $\frac{30}{30} = 0.02 \pm 0.02$	8
π^0	2195 ± 15	39 ± 4	5.13	12.0	5.1	209 ± 41	1.1 ± 1.7	$0.22 < t < 0.26$	29 ± 10	$\frac{10}{30} = 0.04 \pm 0.11$ $\frac{30}{30} = 0.94 \pm 0.06$ $\frac{30}{30} = 0.94 \pm 0.19$ $\frac{30}{30} = 0.02 \pm 0.13$ $\frac{30}{30} = 0.02 \pm 0.02$	8
η^0	2382 ± 24	62 ± 6	5.30	12.0	5.9	252 ± 45	1.1 ± 1.6	$0.20 < t < 0.26$	42 ± 14	$\frac{10}{30} = 0.30 \pm 0.10$ $\frac{30}{30} = 0.45 \pm 0.10$ $\frac{30}{30} = 0.25 \pm 0.10$	8

* $d\sigma/dt$ normalized to 4 GeV/c (average momentum)

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ANDERSON et al. DOUBLE ARM M M SPECTROMETER

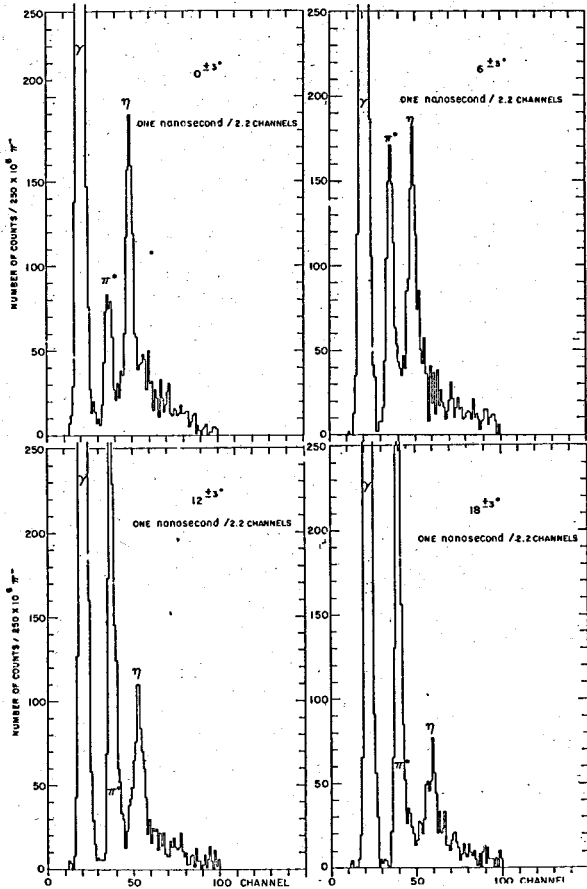


NEW TECHNIQUES

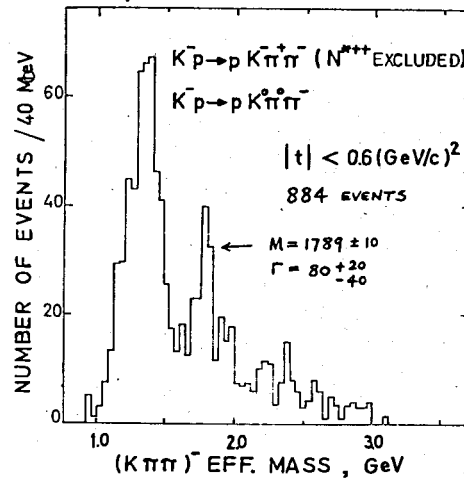
55

NEW TECHNIQUE

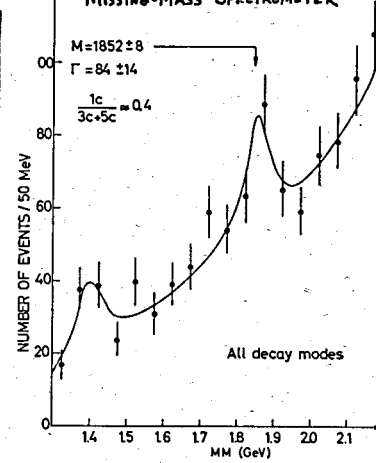
HYMAN et al. $\pi^- p$ 805 MeV/c
NEUTRON-TIME-OF-FLIGHT SPECTROMETER



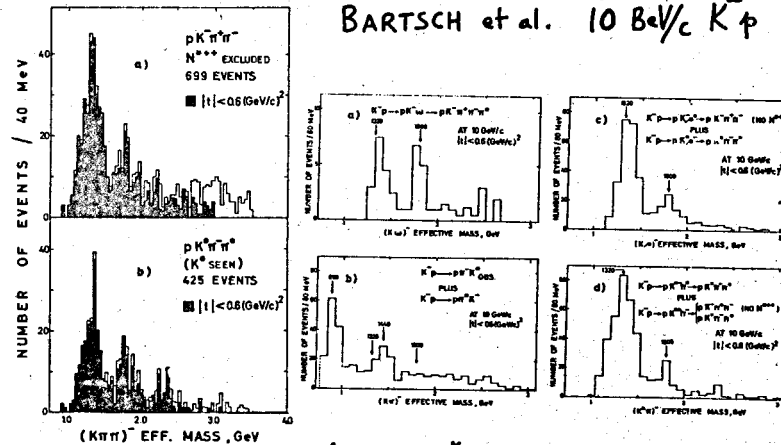
$K^- p$ 10 GeV/c BARTSCH et al.



DUBAL et al $K^- p$ 12 GeV/c
MISSING-MASS SPECTROMETER

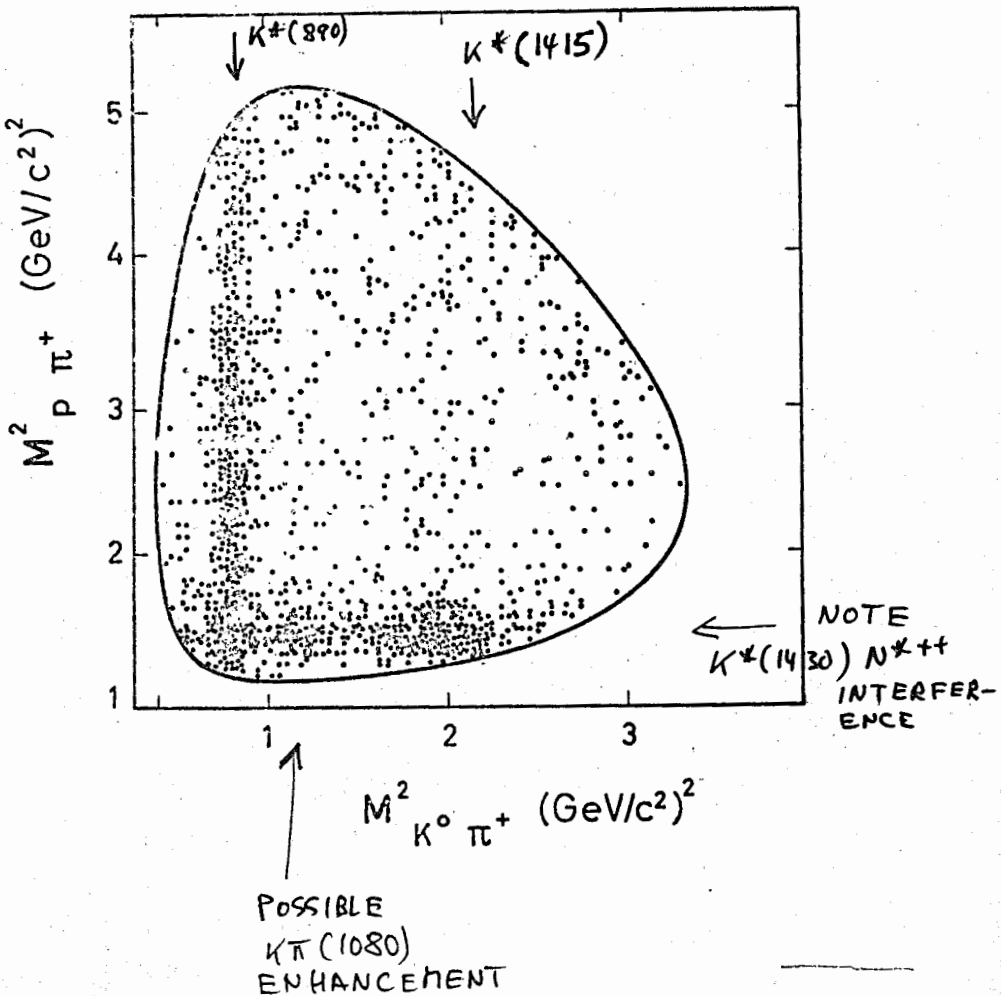


BARTSCH et al. 10 BeV/c $K^- p$

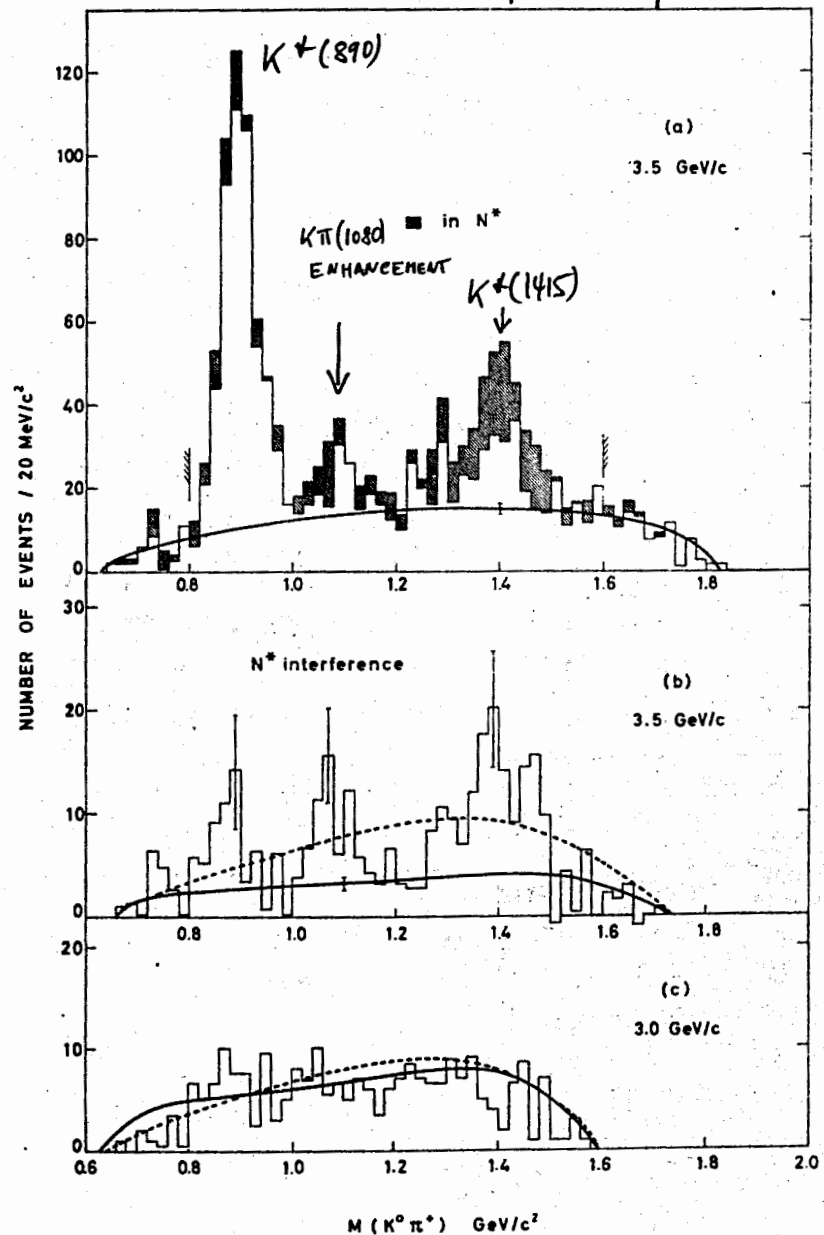


$L \rightarrow K^*(890) \pi$	$35 \pm 12 \%$
$K^*(1400) \pi$	$85 \pm 5 \%$
$K p$	$7.5 \pm 5 \%$
$K \omega$	$10 \pm 6 \%$
$K \pi \pi$	$40 \pm 15 \%$

De BAERE et al. $K^+p \rightarrow K^0\pi^+p$
3.5 GeV/c



De BAERE et al. $K^+p \rightarrow K^0\pi^+p$



qq̄ STATES			
STATE	C	J ^P	CANDIDATES NAME
1S ₀	+	0 ⁻	π η K η' (?) PSEUDO SCALAR
3S ₁	-	1 ⁻	ρ ω K* φ VECTOR
3P ₀	+	0 ⁺	S*(?) , S ₀ (770)(?) SCALAR
3P ₁	+	1 ⁺	A ₁ , K*(1320), D, E[?] AXIAL VECTOR
1P ₁	-	1 ⁺	B, H ... [?] IRRED. TENSOR
3P ₂	+	2 ⁺	A ₂ , f ₀ , K*(1430), f ₁ TENSOR
1D ₂	+	2 ⁻	
3D ₂	-	2 ⁻	B, H, ... [?]
ABNORMAL MODES ^a	qq̄ STATES		
0 ⁻	-	0 ⁻	} NO DEFINITE CANDIDATES
0 ⁺	-	0 ⁺	
1 ⁻	+	1 ⁻	
2 ⁺	-	2 ⁺	

$$\omega(783) \rightarrow \frac{\pi^0 \sigma}{\pi^+ \pi^- \pi^0} = (1.5 \pm 0.6)\% \quad \text{Baqin et al. (E.P.-Bergen)}$$

$$\rightarrow \frac{\pi^+ \pi^-}{\pi^+ \pi^- \pi^0} = (0.04 \pm 0.10)^2 \quad \text{Button-Shafer (LRL)}$$

$$\rightarrow \frac{e^+ e^-}{\pi^+ \pi^- \pi^0} = (0.5-6) \times 10^{-4} \quad 95\% \text{ C.L.}$$

Binnie et al. (I.C. London Manchester)

$$\rightarrow \frac{e^+ e^-}{\pi^+ \pi^- \pi^0} = (1.1 \pm 0.3) \times 10^{-4} \quad \text{Azimov et al. (Dubna)}$$

$$\sigma(\psi \rightarrow e^+ e^-) \leq (0.12 \pm 0.08) \times 10^{-4} \text{ mb}$$

$$\text{Assume } \sigma(\psi \rightarrow K \bar{K}) \approx 10 \mu\text{b},$$

$$\psi(1020) \rightarrow \frac{e^+ e^-}{K \bar{K}} \leq (0.12 \pm 0.08) \times 10^{-2}$$

Azimov et al.
(Dubna)

$$\eta(549) \rightarrow \frac{\pi^0 \gamma \gamma}{\gamma \gamma} < 0.5 \text{ (90\% C.L.)}$$

Wahlig et al
(MIT - PISA)

$$\rightarrow \frac{\pi^0 \gamma \gamma}{\gamma \gamma} = 0.86 \pm 0.4$$

Strugalski et al
(Dubna)

$$\rightarrow \frac{\pi^0 \pi^0 \pi^0}{\gamma \gamma} < 0.42 \quad "$$

$$\rightarrow \frac{\pi^0 e^+ e^-}{\text{All } \eta} < 0.0023 \text{ (90\% C.L.)}$$

Baglin
(EP - Berkeley)

SHEN et al. SPECULATIVE

Decay rates via vector plus pseudoscalar mesons for the
 A_1 nonet hypothesized in the text.

Resonance	Decay mode	Experimental decay rate, Γ (MeV)	Matrix element	P/M^2	Predicted Γ
$A_1(1080)$	$\rho\pi$	$\sim 125^a$	$4H^2$	0.205	<u>125</u> input
$K^*(1320)$	$K^*\pi$	80 ± 20^b	$1.5H^2$	0.193	44
	ρK		$1.5H^2$	0.11	26
	ωK	6 ± 6^b	$1.5 \sin^2 \theta_1 H^2^c$	0.089	9
$D(1286)$	$K^* \bar{K}^0 d$	40 ± 10^a	$6 \sin^2 \theta H^2$		d
$E(1420)$	$K^* \bar{K}$	60 ± 10^a	$6 \cos^2 \theta H^2$	0.076	56^e

- From compilation by Rosenfeld et al., reference 18.
- This experiment.
- The ω - ϕ mixing angle, θ_1 , is taken to be 40 deg.
- The D mass lies below threshold for $K^* \bar{K}$ production. The simple phase-space estimate is thus not applicable.
- A mixing angle of ~ 20 deg is obtained by using the Gell-Mann-Okubo formula linear in mass. This value of the mixing angle predicts a decay rate of 60 MeV for $E \rightarrow K^* \bar{K}$.

Alexander Lipkin and Scheck

$$R = \frac{\langle \pi^+ \rho^- | \pi^+ \pi^- \rangle}{\langle \pi^+ \rho^- | \pi^+ \pi^- \rangle} = \frac{\langle \pi^+ \rho^- | \pi^+ \pi^- \rangle}{\langle \pi^+ \rho^- | \pi^+ \pi^- \rangle} = \frac{\cos \nu - \sqrt{2} \sin \nu}{\sin \nu + \sqrt{2} \cos \nu}$$

MIXING ANGLES FOR MESON NONETS

Benson et al.

J ^P	QUARK MODEL USING CROSS SECTION RELATIONSHIP		SU(3) MASS FORMULA †		Quark Model Using Cross Section Relationship Positive R Negative R
	Positive R	Negative R	Linear	Quadratic	
0 ⁻	+9° -28° -6°	+5° -81° -10°	±23.4°	±10.4°	-19° ± 7° -31° ± 5° -28° ± 9°
1 ⁻	35° ± 7° (Re=0)		±37.5°	±40.2°	27° ± 4° 43° ± 4°
2 ⁺	26° ± 2.5°	47° ± 3°	±29.9°	±31.3°	

LAI and Schumm

GOLDBERG et al. SU₃ COMPARISONS

J ^P	Decay	SU ₃ Factor	Predicted Rate	Experimental Rate
1 ⁻ + 0 ⁻ + 0 ⁻	K*(890) → Kπ	1/4	Input	49 ± 3
	ρ(765) + 2π	1/3	171 ± 8	125 ± 25
	φ(1020) → K \bar{K}	1/2 cos ² θ ₁	3.1 ± .5	3.3 ± .5
2 ⁺ + 0 ⁻ + 0 ⁻	A ₂ (1320) + K \bar{K}	12	Input	4.5 ± 1.5
	f ⁰ (1250) + ππ	3(2sinθ ₂ + acosθ ₂) ²	Input	118 ± 20
	f ⁰ (1250) + K \bar{K}	4(sinθ ₂ - acosθ ₂) ²	6 ± 4	2 ± 2
	f ⁰ (1250) + n ⁰ n ⁰	(2sinθ ₂ - acosθ ₂) ²	0.3 ± 0.3	small
	A ₂ (1320) + n ⁰ π	8	8 ± 3	3 ± 2
	K**(1410) + Kπ	18	30 ± 11	39 ± 20
	K**(1410) + Kη ⁰	2	0.9 ± 0.3	2 ± 2
	f*(1500) + ππ	3(2cosθ ₂ - asinθ ₂) ²	2 ± 4	0 ± 6
f*(1500) + K \bar{K}	4(cosθ ₂ + asinθ ₂) ²	33 ± 18	51 ± 25	
f*(1500) + n ⁰ n ⁰	(2cosθ ₂ + asinθ ₂) ²	9 ± 4	small	
2 ⁺ + 1 ⁻ + 0 ⁻	A ₂ (1320) + ρπ	4	Input	80 ± 14
	K**(1410) → K*π	3/2	20 ± 4	43 ± 15
	K**(1410) → ρK	3/2	5.0 ± 1.4	14 ± 5
	K**(1410) → ω ⁰ K	3/2(sin ² θ ₁)	1.5 ± 0.5	7 ± 4
	f*(1500) + K*K	6cos ² θ ₂	7 ± 4	< 34 ± 15 *NEW

2⁺ + 0⁻ + 0⁻
α = 3.9 ± 1
GLASHOW
& SOCOLOW
USED
α = 2√2

MASS OF THE $K^*(400)$

Group	K π decay			K $^*\pi$ decay			Remarks
	Experiment	# evts peak/bkgd	Mass	# evts pl. backgd.	Mass	Remarks	
British Coll.	3.5 GeV/c K $^-$	35/15	1400 \pm 10	?	?	N* scanty	N* scanty
British Coll.	6 GeV/c K $^-$?	1402 \pm 8	?	1430 \pm ?	N* scanty	N* without influence
EP + S + A	3 GeV/c K $^-$	60/110	1404 \pm 15	120/180	1400 \pm 20	N* removed	N* without influence
AML + N	4.1 and 5.5 GeV/c K $^-$	170/200	1392 \pm 10	60/90	1450 \pm ?	N* removed	N* without influence
CERN (M)	7 and 12 GeV/c K $^-$	15/?	1400 \pm 10	from K π and K $^*\pi$ decay together (using mass spectrometer)			
IRL (M)	4 GeV/c K $^-$	35/0	1430 \pm 20			Y* scanty	
BNL	6 GeV/c π^+	45/20	1407 \pm 10			Y* scanty	
Wisconsin	3.54 GeV/c K $^+$?	1425 \pm 10			Global fit of K π and K $^*\pi$ events	
CERN-Brussels	3.5 GeV/c K $^+$	90/?	1399 \pm ?			N* removed	
CERN-Brussels	3.5 GeV/c K $^+$	90/?	1428 \pm 17			N* scanty	
CERN-Brussels	5 GeV/c K $^+$	70/30	1430 \pm 20			K $^*\pi$ production	
IRL (G)	4.6 GeV/c K $^+$	20/10	1390 \pm 30	50/180	1430 \pm 10	N* removed	N* removed

BRANCHING RATIOS OF THE $K^*(400)$

Group	Experiment	K $^*\pi$ /K π	K ρ /K π	K ω /K π	K η /K π
EP + S + A	3 GeV/c K $^-$	1.1 \pm 0.7	0.35 \pm 0.25	0.2 \pm 0.2	0.05 \pm 0.05
ANL + N	4.1 GeV/c K $^-$	0.47 \pm 0.15	0.34 \pm 0.25		
ANL + N	5.5 GeV/c K $^-$	0.65 \pm 0.15	0.36 \pm 0.30		
Wisconsin	3.54 GeV/c K $^+$	1.7 \pm 0.55	0.3 \pm 0.2	0.03 \pm 0.03	0.06 \pm 0.06
IRL (G)	4.6 GeV/c K $^+$	0.63 \pm 0.20		0.05 \pm 0.03	
IRL (G)	4.6 GeV/c K $^+$	0.65 \pm 0.20		-0.05	

SPIN AND PARITY OF THE $K^*(1400)$

Group	Experiment	Results
EP + S + A	3 GeV/c K^-	$\chi^2 / \langle \chi^2 \rangle$ for 2^+ ; 1^- ; 3^- = 6/6; 19/7; 15/4
BNL	6 GeV/c \bar{K}^-	$\chi^2 / \langle \chi^2 \rangle$ for 2^+ ; 1^- = 2/4; 9/4
ANL + N	4.1 and 5.5 GeV/c K^-	1^- and 2^+ almost equally favored. (1^- a little bit more)

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I-SPIN OF THE $K^*(1400)$

Group:	Experiment	Argument
BNL Wisconsin LRL	6 GeV/c π^\pm	$\pi^+ p \rightarrow \Lambda^0 K^+ \pi^+ / \pi^- p \rightarrow \Lambda^0 K^+ \pi^- = 9/1$ if $I = 3/2$ Experimentally: 3 events seen/80 expected
	3.54 GeV/c K^+	$K^+ p \rightarrow (K^0 \pi^+) \pi^+ n$ Exp. no enhancement in $(K^+ \pi^+)$ mass distribution.
	4.6 GeV/c K^+	$(K \pi)^0 N^{*++} / (K \pi)^+ N^{*++} / (K \pi)^+ N^{*0} = \begin{cases} 63/16/27 & \text{if } I = 3/2 \\ 9/1/0 & \text{if } I = 1/2 \end{cases}$ Experimental results consistent with the last ratios
EP + S + A ANL + N	3 GeV/c K^-	$(\bar{K}^0 \pi^- \pi^0) \rightarrow (\bar{K}^0 \pi^-) \pi^0 / (\bar{K}^0 \pi^- \pi^0) \rightarrow (\bar{K}^0 \pi^0) \pi^- = 1/1$ if $I = \frac{1}{2}$. Exp. 1.06 ± 0.7
	4.1 and 5.5 GeV/c K^-	$K^{*-} \rightarrow \bar{K}^0 \pi^- / K^{*-} \rightarrow \bar{K}^0 \pi^0 = 2/1$ if $I = \frac{1}{2}$. Exp. 1.84 ± 0.5

Production

Decay

$\bar{p}d$ at REST BETTINI et al.

TABLE I

Channel	percentage of all $\bar{p}n$ annihilations	Notes
$\bar{p}+d \rightarrow p_s p^+$		
1 prong	16.4 ± 0.5	
$\pi^- + \pi^0$	$\leq 0.7^{(1)}$	
3 prongs	59.7 ± 1.2	
$\pi^- + \pi^- + \pi^+$	1.57 ± 0.21	(40% $\rho^0 \pi^-$, 40% $f^0 \pi^-$, 20% $\pi^- \pi^- \pi^+$)
($\rho^0 + \pi^-$)	~ 0.63	
($f^0 + \pi^-$)	$\sim 0.94^{(2)}$	
$\pi^- + \pi^- + \pi^+ + \pi^0$	21.8 ± 2.2	(40% $\rho^0 \pi\pi$, $\sim 60\%$ 4π)
($\rho^0 \pi^- \pi^0 + \rho^0 \pi^+ \pi^- + \rho^0 \pi^+ \pi^-$)	~ 8.7	
($A_2^0 + \pi^-$)	$\leq 3.3^{(1)}$	
($\omega^0 + \pi^-$)	$0.41 \pm 0.08^{(2)}$	
($\eta^0 + \pi^-$)	$\leq 0.25^{(1),(2)}$	
5 prongs	23.4 ± 0.7	
$\pi^- + \pi^- + \pi^- + \pi^+ + \pi^+$	$5.15 \pm 0.47^{(3)}$	
$\pi^- + \pi^- + \pi^- + \pi^+ + \pi^+ + \pi^0$	15.1 ± 1.0	($\sim 70\%$ $\omega 3\pi$, 30% 6π)
$\omega^0 + \pi^- + \pi^- + \pi^+$	$12.0 \pm 3.0^{(2)}$	
7 prongs	0.39 ± 0.07	

(1) At a 90% confidence level.
 (2) Corrected for neutral decay
 (3) Dominated by a strong $\rho^0 \rho^0$ interaction (See Ref. 4).

$\pi\pi$ Phase Shifts or Resonance Parameters

Phase shift	$M(\pi\pi)$ (MeV)	Γ (MeV)	Source	Interpretation
$\sim 0^\circ$	700-750		Walker et al.	Resonance?
	720	< 50	Selove	Resonance
$35^\circ \sim 55^\circ$	400-500		Jacobs + Selove	Phase shift
$\sim 20^\circ$	300-325		Jones	Phase shift
$\sim 57^\circ$	600-625			
	430 ± 70	400^{+400} -150	Lovelace	Resonance
Decreasing δ_{00} from 2π at threshold			Cook	phase shift
$I=0 \quad L=2$ $\pi\pi$ Resonance	785	$\sim 5-20$	Desai	Resonance
$\delta_{00} - \delta_{11} = 27^\circ \pm 18^\circ$	280-350		Birge et al.	phase shift

$\delta_{L=0}$
 $I=0$