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# LONG-TIME TUNNELING IN AMORPHOUS METALS AT HELIUM TEMPERATURES

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## 1. Introduction

Very-long-time heat relaxation at low temperatures was observed in several amorphous dielectrics, e.g., in vitreous silica<sup>/1-4/</sup>, PMMA <sup>/5,6/</sup>, and in various other organic materials <sup>/4/</sup>. Since such relaxation is understood in the terms of phenomenological tunneling model <sup>/7,8/</sup>, it may be a common feature of all amorphous materials, i.e., also of metallic glasses. Then we would be able - measuring the heat release - to determine the density of the two-level states even for metals in normal state, where the heat capacity measurements are of little use because of the electron term.

Concerning amorphous metals, heat release measurements have been performed with superconducting LaZn only  $^{/9/}$  up to now. Heat release observed was about a hundred times larger than in vitreous silica probably due to the ortho-para conversion of hydrogen admixtures, and with this thermal background, power due to the tunneling was not seen. Indeed, the heat capacity measurements with superconducting metals  $^{/10,11/}$  and with vitreous silica  $^{/12-14/}$  show that the densities of the tunneling states in those materials do not differ essentially; the heat release should therefore be of the sam order.

In this work, the results of the heat relaxation experiments with two metal glasses are presented. Some of the preliminary rosul have already been published in Ref. 15.

#### 2. Theory

Many low-temperature (T < 1K) features typical of amorphous solids in contrast to the crystalline materials may be explained with the phenomenological tunneling model /7,8/. According to this model, localized two-level systems characterized by quantum mochanical tunneling through the potential barrier between two wolls exist in glasses. The parameters of each two-level system are asymmetry energy  $\Delta$ , barrier energy  $V_E$ , well separation d, tunneling coupling energy  $\Delta_0 = \hbar \omega_e \exp(-\lambda)$ , where  $\hbar \omega_e$  is the zero point energy either well, and the tunneling parameter  $\lambda = d(2mV_E)^{1/2}/\hbar$  (m is the mass of the tunneling object). The energy splitting between the two lowest states in the two wells is  $E = (\Delta^2 + \Delta_2^2)^{1/2}$ . To explain the time-dependent specific heat term, approximately proportional to T, observed in glasses, in the framework of tunneling model, the distribution function of two-level systems  $P(\Delta, \lambda)$  does not need actually to depend on  $\Delta$  and  $\lambda$ . For small values of  $\Delta$  and  $\lambda$ , contributions of which manifest itself for T  $\leq$  1K and short measuring times, an assumption of uniform distribution is reasonable, namely

$$P(\Delta, \lambda) = \overline{P} = \text{const.}$$
(1)

This gives a time-dependent density of states /7,8,16,17/

$$n(E,t) = n_0(t) = (\overline{P}/2) \ln(4t/\tau_{min})$$
 (2)

and the corresponding contribution to the specific heat

$$c_t = (\pi^2 k_B^2/12) T \bar{P} \ln(4t/\tau_{min}),$$
 (3)

where  $k_B$  is the Boltzmann number, and  $\mathcal{T}_{\min}$  is the shortest relaxation time. As a result, heat release appears after cooling the system from the equilibrium temperature  $T_1$  to the temperature  $T_0$ ,

$$\dot{Q} = V \int_{T_0}^{1} (dc/dt) dT;$$
 (4)

with the uniform distribution (1), we have from (3)

$$\dot{Q}(T_1, T_0, t) = V(x^2 k_B^2/24t)(T_1^2 - T_0^2) \bar{P},$$
 (5)

where V is the volume of the specimen.

Equations (2), (3) and (5) hold for small values of E only. Because of the finite number of tunneling particles, the density of states n(E,t) should fall to zero for large E. To take this fact into account, calculations of  $c_{+}$  and  $\hat{Q}$  were performed using

$$n(E,t) = n_0(t)/(1 + exp((E - E_p)/k_B T_b)),$$
 (6)

where  $E_f = k_B T_f$  and  $T_b$  are constant;  $k_B T_b$  is the "width" of the transient region. For  $T_b/T_f \rightarrow 0$ , (6) transforms into

$$\begin{array}{ll} n(E,t) = n_0(t) & \text{for } E \leqslant E_f, \\ n(E,t) = 0 & \text{for } E > E_f. \end{array}$$
(7)

Usually, maximum value of B has been connected with maximum value of barrier height  $V_{max}$ , and  $V_{max} \simeq k_B^T g \simeq 0.1 \ eV$  (Tg is the glass temperature) was assumed  $^{7,17}$ . Then (1) should hold well at helium temperatures. We shall see this is not true for our specimen, where  $E_f \ll k_B^T g$ .

With distribution (6), we get - instead of (3) - $(\pi^2 k^2/12) \overline{\nu} \pi (m/m - m) \pi (4+/m - )$ 

$$c_t = (\pi^2 k_B^2 / 12) \widetilde{PI}_1 (T/T_f, T_b) \ln(4t/\tau_{min})$$
, (8)



$$I_{1}(T/T_{f},T_{b}) = (6/\pi^{2}) \int_{0} \frac{x^{2} \exp(-x) dx}{(1-\exp(-x))^{2}(1+\exp((xT/T_{f}-1)/(T_{b}T_{f})))}$$
(9)

00

m /m

and - instead of (5) -

$$\dot{Q}(T_1, T_0, t) = (\pi^2 k_B^2 / 24t) P V(I_2(T_1 / T_f, T_b) T_1^2 - I_2(T_0 / T_f, T_b) T_0^2) , \qquad (10)$$

where

$$I_{2}(T/T_{f},T_{b})=2(T_{f}/T)^{2}\int_{0}^{T/T_{f}}(T/T_{f})I_{1}(T/T_{f},T_{b})d(T/T_{f}).$$
(11)

Finite number of tunneling particles makes us also introduce the maximum tunneling parameter  $\lambda_{\max}$ , and a corresponding maximum relaxation time  $\mathcal{T}_{\max}$ ; then for  $t \ge \mathcal{T}_{\max}$  (2), (3) and (5) are incorrect.

After cooling the specimen sufficiently fast from T to  $T_0=0$ , excited tunneling particles relax and the total energy  $\mathcal{E}$  of the system decreases according to

$$\xi(T,0,t) = \sum_{i=1}^{n} \xi_{i}(T,0) \exp(-t/\tau_{i}), \qquad (12)$$

where  $\mathcal{E}_{i}(T,0)$  is the sum of the excitation energies at T of all levels with relaxation time  $\tau_{i}$ ; N is the total number of various relaxation-time values. Transition from the sum of the integral gives

$$\mathcal{E}(\mathbf{T},\mathbf{0},\mathbf{t}) = \int_{\mathbf{min}}^{\mathbf{max}} f(\mathbf{T},\mathbf{0},\mathbf{\tau}) \exp(-\mathbf{t}/\mathbf{\tau}) d\mathbf{\tau}, \qquad (13)$$

where  $f(T,0,\tau)$  is proportional to the relaxation time distribution function  $P(\tau)$ . Since  $\tau \sim \exp(2\lambda)$ ,  $P(\tau) = (P/2\tau)$  follows from  $P(\lambda) = \overline{P}$ . Writting

$$f(T,0,\tau) = a(T)/\tau$$
, (14)

we get from (13), (14)

$$\dot{Q} = \partial \xi / \partial t = a(T) \cdot t^{-1} (exp(-t/\tau_{max}) - exp(-t/\tau_{min})) .$$
(15)

Expression (15) really yields a usual  $t^{-1}$  dependence of  $\dot{Q}(t)$  for  $t \ll \tau_{max}$ . For  $t > \tau_{max}$ , this dependence transforms into an exponential one. Comparing (15) with (10), we obtain

$$a(T) = (\nabla_{\pi}^{2} k_{B}^{2} / 24) \overline{P} I_{2} (T/T_{f}, T_{b}) T^{2} .$$
 (16)

Then in a more general case, the heat release after rapid temperature variation from  $T_1$  to  $T_0$  (cooling when  $T_1 > T_0$ , heating when  $T_1 < T_0$ ;

$$T_{o}, T_{1} > 0$$
, equals (for  $t \gg \tau_{min}$ )  
 $\dot{Q}(T_{1}, T_{o}, t) = (a(T_{1}) - a(T_{o})) t^{-1} exp(-t/\tau_{max})$ . (17)

All expression we have written for  $\dot{Q}(T_1,T_0,t)$  are valid, if the thermal equilibrium was established before the cooling (heating) at  $T_1$ . Let us see what power is to be released when, after relaxation is completed at  $T_0$ , the specimen is heated up to the temperature  $T_{H^2}$ , and after the time  $t_H$  cooled to  $T_0$  again. The corresponding heat release will be  $\tau_{max}$ 

$$\dot{Q}(T_{\rm H}, T_{\rm o}t_{\rm H}, t) = \int_{\tau_{\rm min}} (a(T_{\rm H}) - a(T_{\rm o})) \tau^{-2} (1 - \exp(-t_{\rm H}/\tau) \exp(-t/\tau)) d\tau. \quad (18)$$

Usually,  $au_{\min} \ll t \ll au_{\max}$ , and

$$\dot{Q}(T_{\rm H}, T_{\rm o}, t_{\rm H}, t) = (a(T_{\rm H}) - a(T_{\rm o}))t^{-1}(1 + t/t_{\rm H})^{-1}$$
 (19)

Using (19), one can determine, how long  $t_H$  must be for reaching the "equilibrium" heat release (theoretically,  $t_H \rightarrow \infty$ ). As a rule,  $t_H = 20$  h in our experiments; the heat release 1 h after cooling differs from the equilibrium one by no more than 5 per cent.

It is interesting that the ratio of the power released for two different  $t_H$  and the same  $T_o$  does not depend on  $T_H$ ; this is not difficult to prove experimentally.

# 3. Specimens and experiment

Two specimens were studied. Specimen I was a strip of amorphous ferromagnet  $Fe_{80}B_{14}Si_6$  (produced in the Central Institute for Solid State Physics and Material Research of Acad.Sci., Dresden, GDR). Its length was 43.3 m, width 31 mm, thickness 40  $\mu$ m. The strip was wound up into the form of a cylinder, 50 mm in diameter. Strips of copper foil (thickness 30  $\mu$ m) were fixed at various places between the windings of  $Fe_{80}B_{14}Si_6$  (total contact area ~600 cm<sup>2</sup>); a thermometer (germanium resistor), a heater and a contact for the heat switch were mounted on this copper foil. The mass of  $Fe_{80}B_{14}Si_6$  was 288.18 g, that of the copper and resistors with negligible amount of the solder (no glue was used) equals 15.97 g. In such system, thermal equilibrium sets fairly fast throughout the specimen. Even under very unsuitable conditions, equilibrium was set in several tens of seconds.

Specimen II consisted of a strip of amorphous ferromagnet  $^{Co}_{69}^{Fe}_{4.5}^{Cr}_{2}^{Si}_{2.5}^{B}_{22}$  (of the same origin) with the length of 77.6 m, width 14.2 mm, and thickness 35 µm. The construction was almost the same as of specimen I, only specimen II consisted of two "floors"

because of the small width of the strip. The mass of  $Co_{69}Fe_{4.5}Cr_2Si_{2.5}B_{22}$  was 250.3 g (124.4 g + 125.9 g), that of the copper 16.1 g.

The experimental arrangement was the same as in Ref. 19, 20. Specimen I (II) with the thermometer and the heater hangs in the calorimeter on 12 (8) kapron threads (0.13 mm in diameter, 31 mm long). The coupling constant A between specimen I (II) and the body of the calorimeter with the heat switch off was slightly temperature dependent, A=122 pW/mK (72 pW/mK) - i.e. about 10 pW/mK per one kapron thread - at 1.3K. The heat resistance of the closed switch was determined as  $10^4$  K/W at the same temperature.

The efficiency of the switch and all the contacts is demonstrated in Fig. 1, where time necessary for cooling the specimen from the temperature  $T_1$  to 1.3K is shown.

The value of the thermal background power  $\dot{Q}_{\rm B} = (1150 \pm 50) \ {\rm pW}$  was somewhat larger than in previous experiments. Since it increased after changing the radiation shields in the calorimeter central tube, we suppose  $\dot{Q}_{\rm B}$  be largely due to the radiation along the suspension system. On the other hand, maximum variation of  $\dot{Q}_{\rm B}$  in time, which limits the accuracy of measurement, was reduced to  $\dot{Q}_{\rm R} \lesssim 100 \ {\rm pW}$ .

During the measurements, heat capacities of both specimens were determined in the temperature range somewhat larger than necessary for the heat release calculations.

The heat release  $\dot{Q}$  and the specific heat release  $\dot{q} = \dot{Q}/m$  (m is the mass of the amorphous metal) were calculated, as usual  $^{/19,20/}$ , from the drift of the specimen temperature with the heat switch off, corrected for the heat background  $\dot{Q}_{\rm B}$  and heat leak  $\dot{Q}_{\rm A}$ :

where

$$\mathbf{A}_{\mathbf{A}} = \mathbf{A}(\mathbf{T}_{\mathbf{K}} - \mathbf{T}) \cdot$$
(22)

Q is the measured power, R is the germanium thermometer resistance drift, C is the heat capacity of the

specimen,  $\partial R / \partial T$  is the sensitivity of the thermometer; as a rule,  $T_{K} \simeq T$ .

 $\dot{\mathbf{Q}} = \dot{\mathbf{Q}}_{\mathrm{m}} - \dot{\mathbf{Q}}_{\mathrm{h}} - \dot{\mathbf{Q}}_{\mathrm{m}},$ 

Fig.1. The time necessary for cooling the specimen in the calorimeter from  $T_1$  to  $T_0 = 1.3K$ .  $1 - Fe_{80}B_{14}Si_6$ ,  $2 - Co_{69}Fe_{4.5}Cr_2Si_{2.5}B_{22}$ .



(20)



Fig. 2. The specific power released in specimen I ( $Fe_{80}B_{14}Si_6$ ) after cooling from various  $T_1$  (3.12K  $\leq T_1 \leq 292K$ ) to  $T_0 = 1.3K$  as a function of the time. Straight lines:  $q \sim t^{-1}$ .

The results are presented as  $\dot{q} = \dot{Q}/m$  - the power released in 1 g of the material under study.

At the beginning, the specimen was cooled from room temperature to 1.3K and the long-time power release  $\dot{Q}(t)$  was measured, until it dropped to the level of background fluctuations (100 pW). Then the specimen was successively heated to  $T_1$  (3.12  $\leq T_1 \leq$  292K) and kept for  $t_H = 20$  hours at that temperature; after another cooling to 1.3K the time dependence of  $\dot{Q}(t)$  was measured again. For some values of  $T_1$  much less heating time was also used,  $t_H = 0.2$  h and/or  $t_H =$ 0.5 h.

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Fig. 3. The specific power released in specimen I 1 hour after cooling from  $T_1$  to  $T_0 = 1.3K$  as a function of  $T_1^2 - T_0^{21}$ o -  $t_H = 20$  h, • -  $t_H = 0.5$  h,  $\blacktriangle - t_{H^2} = 0.2$  h (see the text); 1 - standard tunneling theory (5) with  $\overline{P}_m = 2.3 \times 10^{37}$ /Jg, 2 - equation (10) with  $\overline{P}_m = 2.3^{10^{37}}$ /Jg,  $T_f = 20K$ ,  $T_b = 0$ .

Fig. 4. The specific power released in specimen II  $(Co_{69}Fe_{4.5}Cr_2Si_{2.5}B_{22})$  after cooling from various  $T_1$  (4.34K  $\leq T_1 \leq 40.0$ K) to  $T_0 = 1.3$ K as a function of the time. Straight lines  $\dot{q} \sim t^{-1}$ .



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# 4. Results

For both specimens, heat release after cooling from any "heating" temperature  $T_1$  is proportional to  $t^{-1}$  (Fig. 2,4). Deviations from the straight line just after the cooling for large  $T_1$  are evidently due to unsufficiently rapid cooling (relaxation of levels with small E begins later) and to unfinished process of reaching the thermal equilibrium throughout the specimen at the beginning of the measurements. This is the case of the specimen II and  $T_1 > 35K$  (see Fig. 4).

In Figs. 3,5 power release  $\dot{q}(1h) = \dot{Q}(1h)/m$  at t = 1h after the cooling is shown as a function of  $T_1^2 - T_0^2$  ( $T_0 = 1.3K$ ). For small  $T_1$ , long-time heat release increases with increasing  $T_1$ ; it is almost independent of  $T_1$  for large  $T_1$ . Measured values of  $\dot{Q}(1h)$  after short heating time  $t_H$  are also presented in Figs. 3,5.

# 5. Discussion

Ortho-para conversion in hydrogen bubbles, precipitated in the copper  $^{18-20'}$  or in amorphous LaZn  $^{9'}$ , is well known as a source of a long-time heat release. But such heat release is not proportional to t<sup>-1</sup> (the dependence is more complicated) and the dependence on T<sub>1</sub> is quite different: the heat release is about three



Fig. 5. The specific power released in specimen II 1 hour after cooling from various  $T_1$  to  $T_0 = 1.3$ K as a function of  $T_1^2 - T_0^2$ .  $o - t_H = 20$  h,  $o - t_H = 0.5$  h, (see the text); 1 - standard tunneling theory (5) with  $\overline{P}_m = 1.2^{\circ}10^{37}/Jg$ , 2 - equation (10) with  $\overline{P}_m = 1.2$  x  $10^{37}/Jg$ ,  $T_b = 0$ .

orders of magnitude more intensive after cooling from room temperature than that from 30K. In this experiments, the heat release after cooling from 30K does not differ significantly from the heat release after cooling from room temperature. Moreover, our measured heat release is of the same order as that in vitreous silica  $^{/4/}$ . Thus, the possible heat release due to the hydrogen ortho-para conversion in the copper and/or glass itself can be neglected.

Deviations from the t<sup>-1</sup> law were not found for any t until  $Q \lesssim Q_{\rm B}$ . Thus the relaxation time spectrum extends over 100 h ( $\tau_{\rm max} >$  100 h) for our specimens, regardless the essential difference between metals and dielectrics - the presence of conduction electrons. The absence of conduction-electrons influence may be due to a rather high measuring temperature,  $T_{\rm c} = 1.3$ K.\*

The proportionality  $\dot{Q}_{*}(T_{1}^{2}-T_{0}^{2})$  for small  $T_{1}$  enables to determine the parameter  $\overline{P}_{m} = V\overline{P}/m$  from (5):  $\overline{P}_{m} (2.3\pm0.2)10^{37}/Jg$  for the specimen I and  $\overline{P}_{m} = (1.2\pm0.1)10^{37}/Jg$  for the specimen II. Analogous measurements with vitreous silica yielded  $\overline{P}_{m} = 4.5^{\circ}10^{37}/Jg^{-4/4}$  and  $1.5^{\circ}10^{38}/Jg^{-2},3^{-3/4}$  in good agreement with the results from heat capacity (2.4\*10<sup>38</sup>/Jg^{-12-14/4}, heat conductivity (1.7\*10<sup>38</sup>/Jg^{-13},22,23/4)) and ultra-sound (9.5\*10<sup>37</sup>/Jg^{-24/4}) measurements. Our slightly reduced values of  $\overline{P}_{m}$  seem reasonable taking into account lower than in vitreous silica tunneling contribution to the heat capacity in the case of amorphous superconductors (ZrCu - 11/4).

Thus, the heat release studies enable one to find the two-level system's distribution function  $P(a,\lambda)$  even for metals in normal state; it is so far the only method to fix  $P_m$  directly without any other experimental data.

Our results for higher initial temperatures  $T_1$  can hardly be explained with the standard tunneling model with  $P(\Delta, \lambda) = \overline{P}$ ; the same was found for vitreous silica /4/. On the other hand, the data calculated from distribution (7) are in good agreement with our experimental results if we take  $\overline{P}_m = 2.3 \cdot 10^{37}/Jg$ ,  $T_f = 20K$  and  $T_b = 0$  for specimen I (Fig. 3), and  $\overline{P}_m = 1.2 \cdot 10^{37}/Jg$ ,  $T_f = 24K$  and  $T_b = 0$  for specimen II. Assuming distribution (7) for vitreous silica,

values  $\overline{P}_{m} = 4.5 \cdot 10^{37} / \text{Jg}$ ,  $T_{f} = 13$ K,  $T_{b} = 0$  well agree with experiments<sup>3</sup>, 4/. \*

The experimental values of  $E_f$  are surprisingly much smaller, than  $k_B T_g$  where the glass temperature  $T_g$  is probably near to the recrystalization temperature in metal, ~640K ( $\geq$ 690K) for specimen I (II). Indeed,  $T_f \simeq T_g/30$  for both our specimens. Maybe, even the maximum barrier height is much smaller than the characteristic glass energy  $k_B T_g$ ? If this is the case, the tunneling parameter  $\lambda$  may not be temperature independent except for  $T_0 \ll T_f$ ; for higher temperatures, the dependence  $\lambda$  on  $T_0$  and t may be more complicated than according to (10) and (19).

Because of large heat capacity of metallic glasses, the measurements at higher temperatures were not performed. But deviations from (19) were actually observed.

In Fig. 6 the ratio  $\dot{q}(t_{\rm H}, 1 \, {\rm h})/\dot{q}(1 \, {\rm h})$  is shown as a function of  $T_{\rm H}/T_{\rm f}$ ;  $\dot{q}(t_{\rm H}, 1 \, {\rm h})$  is specific power released 1 hour after the cooling from  $T_{\rm H}$ , where the specimen (preliminary relaxed at  $T_{\rm o}$ ) stayed for the time  $t_{\rm H}$ , and  $\dot{q}(1 \, {\rm h})$  is the specific power released 1 hours after



Fig. 6. The dependence of the value  $\dot{q}(t_{\rm H}, 1 \text{ h})/\dot{q}(1 \text{ h})$  on  $T_{\rm H}/T_{\rm f}$ , where  $\dot{q}(t_{\rm H}, 1 \text{ h})$  is the specific power released 1 hour after cooling down from  $T_{\rm H}$  for short heating times ( $t_{\rm H} = 0.2 \text{ h}$  or 0.5 h) and  $\dot{q}(1 \text{ h})$  is the same for long heating times ( $t_{\rm H} = 20 \text{ h}$ ,  $T_{\rm H} = T_{\rm 1}$ ). Dashed lines - equation (19), full curves - equation (25) with t=1 h,  $\propto =6$ ,  $T_{\rm H}=20$ K (24K) for specimen I (II),  $t_{\rm H} = 0.2$  h (curve 1),  $t_{\rm H}=0.5$  h (curve 2).

If we assume that the relaxation time due to the interaction with the conduction electrons at 10 mK  $\tau_e \simeq 10^{-4} \tau_p /^{21/}$ , where  $\tau_p$  is the relaxation time due to photon interaction, and  $\tau_e / \tau_p \sim E^{2/16,17}$ ,  $^{21/}$ , then  $\tau_e > \tau_p$  at T = 1.3K, and in relaxation of the levels with  $E/k_B > 1.3K$  the influence of the conduction electrons is probably negligible.

<sup>\*</sup> Calculations in  $^{/3/}$ , resulting in  $T_f = (4\pm 2)K$  and  $T_b \simeq 10K$ , are somewhat mysterious: using such values, even the condition  $n(E,t) = n_o(t)$  for  $E \ll E_f$  is not fulfilled.

the cooling from "equilibrium"  $T_H = T_1$  (the specimen stayed at  $T_H$  for 20 hours). The dashed curves correspond to (19) with  $t_H = 0.2$  h and  $t_H = 0.5$  h. For larger  $T_{H}/T_f$  the ratio  $q(t_H, 1 h)/q(1 h)$  increases for both specimen, which may be due to the drift of the time relaxation  $\tau_i$  spectrum to shorter  $\tau$ , since the heat relaxation at elevated temperatures is faster, than according to the standard theory.

If we assume the tunneling parameter  $\lambda'$  temperature dependent as

$$\lambda' = \lambda - (\alpha/2) \cdot T/T_{f}, \qquad (23)$$

we get temperature dependence of the relaxation time (  $\tau^{\prime} \sim \exp(2\;\lambda^{\prime})$  /16,17/

$$\tau' = \tau \cdot \exp(-\alpha \tau/\tau_{\varphi}) \cdot (24)^{\prime}$$

Then, according to (18) and for  $au_{\min} \ll t \ll au_{\max}$ 

$$\dot{q}(T_{H}, T_{o}, t_{H}, t)/\dot{q}(T_{H}, T_{o}, t) = 1/(1 + (t/t_{H})\exp(- \propto T_{H}/T_{f})/\exp(- \propto T_{o}/T_{f}))$$
(25)

The agreement between the model and experiment is surprisingly good, when taking t=1 h and  $\propto =6$  for both  $t_{\rm H} = 0.2$  h (curve 4) and  $t_{\rm H} = 0.5$  h (curve 3).

Thus, the parameter  $T_f$  seems to control both the energy distribution of the two-level systems and the change of the relaxation time spectrum; maybe,  $T_f$  has a deeper physical meaning. It would be interesting to check the existence of such deviation from (19) in another glasses and possible degree of universality of (10) and (25) as functions of  $T_0/T_f$  and  $T_H/T_f$ . At higher  $T_0$  (10) probably does not hold. Up to now, experiments with various  $T_0$  have been performed for vitreous silica only, and only for  $T_0 \ll T_f \simeq 13K$  (0.05K  $\leqslant T_0 \ll 1.08K$ )/1,2,4/; here the results agree well with (10). We suppose that dielectrics are more convenient for possible measurements at higher  $T_0$ .

#### 6. Conclusions

Very-long time heat release observed in metallic glasses is similar to that in dielectrics; such heat release is probably a common feature of all amorphous materials. Experimental values of  $\overline{P}_{m}$ , calculated from measurements at sufficiently low temperatures, do not differ essentially both for our metallic specimens and vitreous silica /4/.

Standard tunneling model assumption  $n(E,t) = n_0(t)$ , i.e.  $P(\Delta, \lambda) = \overline{P} = \text{const}$  is compatible with measured values for rather small values of E only. For higher E, long-time heat release in our specimens may

be explained by assuming  $n(E \le E_f, t) = n_o(t)$  and  $n(E > E_f, t) = 0$ , temperature  $T_f = E_f/k_B$  being about thirty times lower than the recrystallization temperature.

At elevated temperatures, viz.  $T_0 \ge T_f/10$ , the relaxation time in the two-level systems probably depends on the temperature  $T_0$ (higher  $T_0$ , shorter relaxation time) in contrast to the standard tunneling model.

Because of small value of  $T_f$ , if would be not difficult to separate the tunneling and ortho-para conversion terms in the total power released, if necessary.

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Колач М. и др. Медленное туннелирование в аморфных металлах при гелиевых температурах

Измерялось медленно релаксирующее тепловыделение в аморфных  $Co_69Fe_{4,5}Cr_2Si_{2,5}B_{22}$  и  $Fe_{80}B_{14}Si_{6}$  после охлаждения от  $T_1/3,12K \leq T_1 \leq 292K/$  до  $T_0 = 1,3K$ . Выделяемая мощность строго пропорциональна  $t^{-1}$  /0,5 ч  $\leq t \leq 60$  ч/. При низких  $T_1$  результаты эксперимента хорошо согласуются со стандартной теорией туннелирования. Полученные плотности состояний двухуровневых систем очень близки плотности этих систем в кварцевом стекле. Для более высоких  $T_1$  экспериментальное тепловыделение можно объяснить предположением о существовании максимальной энергии  $E_f$  в функции распределения.

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Koláč M. et al. Long-Time Tunneling in Amorphous Metals at Helium Temperatures

Long-time heat release in amorphous  $Co_{69}Fe_{4.5}Cr_{2}Si_{2.5}B_{22}$ and  $Fe_{80}B_{14}Si_{6}$  after cooling from  $T_{1}$  (3.12K $\leq T_{1} \leq 292K$ ) to  $T_{0} = 1.3K$  was measured. The power released is proportional to t<sup>-1</sup> (0.5 h  $\leq$  t  $\leq$  60 h). At low  $T_{1}$ , the experimental results are in good agreement with the standard tunneling theory. The resulting densities of states of two-level systems are close to those in vitreous silica. For higher  $T_{1}$ , observed heat release may be explained assuming the existence of a maximum energy  $E_{f}$  in the distribution function.

The investigation has been performed at the Laboratory of Nuclear Problems, JINR.

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