

# объединенный <br> ИНСТитУт <br> ядерных <br> исследований <br> <br> дубна 

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C.L.Kathat

SECOND CLASS CURRENTS
IN THE $\mu^{-}$-CAPTURE
BY POLARIZED LIGHT NUCLEI

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The problem of second class currerit (SCC) has a significant value for our understanding of the weak interaction structure. Weinberg [1] classified the weak hadron currents by their transformation properties under the G-parity operation (where $G=C$ exp (ir $T_{2}$ )). The first class currents (FCC) which dominate in the weak interaction and form the basis of the Standard Model, behave under G-parity transformation as

$$
G V_{a}^{I} G^{-1}=+V_{a}^{I} \quad \text { and } \quad G A_{a}^{I} G^{-1}=-A_{a}^{I} .
$$

SCC, which are a serious problem (see, for example, [2,3]) for the renormalized gauge theories of the electroweak interaction, behave oppositly to FCC under the G-parity operation:

$$
G V_{a}^{I I} G^{-1}=-V_{a}^{I I} \quad \text { and } \quad G A_{a}^{I I} G^{-1}=+A_{a}^{I I} \text {. }
$$

Following this classification the Dirac ( $F_{1}$ ), Fauli ( $F_{2}$ ), axial-vector ( $F_{A}$ ) and pseudoscalar ( $F_{P}$ ) form factors belong to FCC, and the scalar ( $F_{s}$ ) and tensor ( $F_{T}$ ) form factors - to SCC.

From the investigation of the mirror asymmetry of f3-decay [4] the values of $F_{T}$ are found to be equal to the form factor $\mathrm{F}_{2}$ within the experimental accuracy. On the other hand, in a series of papers (see, for example, [5]) from•the data on the angular distribution of s-particles with respect to the nuclear spin it is concluded that the G-parity of the weak nuclear current is strongly conserved, i.e.

$F_{T}=0 . \operatorname{SCC}$ were also searched for in the
 not observed.

Recently the $\tau$-lepton decay channels taking place due to SCC have been observed at colliding
 the subsequent analysis of these data throws dpubt upon the conclusions of the SCC existence (see, for example, [9]).

Thus, at present there is a contradictory and uncertain experimental situation concerning the search for SCC. It seems that for the complete solution of the SCC problem it is necessary to search for new effects, induced by SCC, and to carry out a number of independent axperiments on measurement of various physical characteristics of electroweak processes.

Since the momentum transferred in the $\mu^{-}$-capture is much higher than in the f-decay, the search for SCC in the $\mu^{-}$-capture is preferable [10, 11], although the pure effects [12-14], induced by SCC, may be also observed in nuclear f-decay.

The present work, developing the $[10,14-17]$, is devoted to the study of the polarized muon capture by the polarized light nuclei

$$
\begin{equation*}
\mu^{-}+(A, Z) \rightarrow(A, Z-1)+{ }^{2 r} \tag{1}
\end{equation*}
$$

with allowance for the SCC and the muon neutrino mass.

The matrix element of process (1) in the tramework of the current-current theory of the weak

1nteraction may be written as

$$
\begin{equation*}
\left.\left\langle+; \vec{म}_{2,} S_{\nu}\right| \hat{H}_{W} \mid \text { म }_{\mu}, \vec{S}_{\mu} ; i\right\rangle=-\frac{G_{F}}{\sqrt{2}} 1_{a} J_{a} \text { (す), } \tag{2}
\end{equation*}
$$

where $J_{a}(\vec{q})=\int d \vec{r} e^{-\vec{q} \vec{r}}\langle f| \phi_{15}(\vec{r}) \hat{J}_{\alpha}(\vec{r})|i\rangle \quad i=$ the
 Fermi constant of the weak interaction (mp is the proton mass); $\mathrm{q}_{a}=\left(\mathrm{p}_{\mu}-\mathrm{p}_{\Delta}\right)_{\alpha}=\left(\vec{q}, \quad i E_{0}\right)^{p}$ is the 4-momentum transfer; $p_{\mu}^{a}$ and $p_{2}^{a}$ are the 4-momenta of the muon and muonic neutrino: $1_{\alpha}=1 \bar{u}_{\nu_{\mu}} \gamma_{\alpha}\left(1+\gamma_{5}\right)$ $u_{\mu} i s$ the muon current; $u_{i}\left(i={ }^{2 \mu} \mu, \mu\right)$ are the Dirac spinors.

Since the wave tunction of the muon $\phi_{15}{ }^{(\vec{r})}$ in the 15 Bohr orbit of the mesoatom is a slowly varying function within the nuclear volume, it will be a "good" approximation if one extracts it from the 1 nside of the matrix element (2) and use its average value [18]:

$$
\left|\phi_{15}\right|_{a v}^{2}=R\left|\phi_{15}(0)\right|^{2}=(R / \pi)\left[\operatorname{Zom}_{\mu} M_{A} /\left(m_{\mu}+M_{A}\right)\right]^{3}
$$

Here $k$ is a reduction factor taking into account the finite extent of the nuclear transition density; $M_{A}$ and $Z$ are the mass and the charge of the nucleus; a is the fine structure constant.

In order to calculate the nuclear matrix elements the multipole expansion method [18] of the nuclear weak current $\hat{J}_{o( }(\vec{q})$, is used.

The coordinate system (see Fig. 1) taking into account the nuclear polarization is defined as
follows: $\vec{e}_{z}=\vec{q}^{0}=\vec{q} / q$, the unit vectors $\vec{e}_{x}$ and $\vec{e}_{y}$ are parrallel to the vectors $\left(\vec{p}_{2} \times \vec{s}_{\mu}\right) x$ and ( $\vec{p}_{2}$, $x$ $\vec{\Xi}_{\mu}{ }^{\prime}$, respectively. The angles $\hat{\theta}^{*}$ and $\rho^{*}$ describe the direction of the quantization axis (Z--axis) with

$\vec{e}_{y} \| \vec{p}_{\nu} \times \vec{s}_{\mu}$
respect to the fixed Z-axis. Below the method of taking into account the nuclear polarization described in [14, 19, 20] 15 used. The order of the multipole operators, determining the expression for the differential rate of the transition $\left(J_{i}^{\pi_{i}} ; T_{i} M_{T_{i}} \rightarrow J_{f}^{\pi_{f}} T_{f} M_{T_{f}}\right)$, $i=$ defined bu the selection rule: $\left|J_{i}-J_{f}\right| \leq J \leq$ $\left|J_{i}-J_{f}\right|$. In the case of the pure Gamow-Teller transition $(J=1)$ the differential rate of process (1) with allowance for the muon and nuclear polarization and the longitudinal polarization of the neutrino (the mass of which is supposed to be not zerol, calculated using (2) in the lower order of the perturbation theory, is given bu
$d W=\frac{G_{F}^{2}}{(4 \pi)^{2}} d \Omega_{2+} E_{2} \rho_{2}\left|\phi_{1 S}\right|_{a v}^{2}\left[\begin{array}{c}T_{f} \\ -M_{f} \\ -1 \\ T_{i} \\ M_{T}\end{array}\right]^{2} F\left(\theta, \theta^{*}, \beta^{*}\right)$.

Here diz $=\sin (\theta) d \theta d p$ is the solid angle of the neutrino; $p_{n}=\left(E_{n_{2}}^{2}-m_{n}^{3} 1 / 2, E_{n}=E_{n}-\Delta E\right.$ (where $\Delta E$ $=E_{f}-E_{i}=E_{\mu}-E_{\omega}$ is the energu transfer), $m_{\nu \lambda}$ are the momentum, energu and mass of the neutrino; $E_{\mu}=$ $m_{\mu}-\varepsilon_{B}, m_{\mu}$ and $\varepsilon_{B}$ are the energy, mass and binding energy (in the is Bohr orbit of a mesoatom) of the muon; $E_{i}\left(E_{f}\right)$ is the energy of the initial (final) nucleus.

The function $F\left(\theta, \theta^{*}, F^{*}\right)$ has the form

$$
\begin{aligned}
& F\left(\theta, \theta^{*}, \alpha^{*}\right)=f_{1} \phi_{1}+2 f_{2} \phi_{2}+f_{3} \phi_{3}+f_{4} \phi_{4}+f_{5} \phi_{5}+ \\
& +\frac{A}{2} F_{2}\left(\cos ^{*} \theta^{*}\left[\mp_{1} \phi_{1}+2\left(f_{2} \phi_{2}-f_{3} \phi_{3}-f_{4} \phi_{4}-f_{5} \phi_{5}\right)\right]+\right. \\
& +A F_{2}^{1}\left(\operatorname{cog}^{*}\right) \operatorname{coSf}^{*}\left({ }_{6} F_{L 1}^{5} F_{E 1}^{5}+{ }_{7} F_{L 1}^{5} F_{M 1}+{ }_{8} F_{C 1}^{5} F_{E 1}^{5}+\right. \\
& \left.f_{q} F_{C 1}^{5} F_{M 1}\right)-\frac{A}{4} F_{2}^{2}\left(\cos \theta^{*}\right) \cos 2_{\phi}^{3} f_{10}\left[\left(F_{M 1}^{E_{1}}\right)^{2}-\left(F_{E 1}^{S_{E}}\right)^{2}\right]-
\end{aligned}
$$

$$
\begin{align*}
& \left.f_{9} F{\underset{C 1}{5}}_{5}^{F_{E 1}^{5}}\right)-\frac{3}{2} P P_{1}\left(\cos \theta^{*}\right)\left(2 f_{1} \phi_{2}+f_{2} \phi_{1}\right) . \tag{4}
\end{align*}
$$

Here $A$ and $F$ are the alignment and the polarization of the nuclei; $P_{L}^{M}$ (coso*) are the associated Legendre polynomials;

$$
\phi_{1}=\left(\left(F_{M 1}\right)^{2}+\left(F_{E 1}^{5}\right)^{2}\right), \quad \phi_{2}=F_{M 1} F_{E 1}^{5}
$$

$\phi_{3}=\left(F_{L 1}^{5}\right)^{2}, \quad \phi_{4}=F_{L 1}^{5} F_{C 1}^{5}, \quad \phi_{5}=\left(F_{C 1}^{5}\right)^{2}$,
where $F_{M 1}, F_{C 1}^{5}, F_{L 1}^{5}$ and $F_{E 1}^{5}$ are the matrix elements of the vector magnetic, axial-vector electric, Coulomb and longitudinal multipole operators.

The arbitrary polarization of muons and the longitudinal polarization of the muonic neutrino taken into account the leptonic functions $\boldsymbol{f}_{\mathrm{i}}$ (i=1, $2, \ldots, 10)$, entering into the differential rata (3), have the form:

$$
\begin{array}{ll}
\boldsymbol{f}_{1}=2 \delta\left(1-s_{v} \cos \theta\right), & \boldsymbol{f}_{2}=-2 \delta\left(s_{v}-\cos \theta\right), \\
\boldsymbol{f}_{3}=2 \delta\left(1+s_{2} \cos \theta\right), & \boldsymbol{f}_{4}=4 \delta\left(s_{2}+\cos \theta\right), \\
\boldsymbol{f}_{5}=2 \delta\left(1+s_{2} \cos \theta\right), & \boldsymbol{f}_{6}=\sqrt{2} s_{v} \sin \theta, \\
\boldsymbol{f}_{7}=-\sqrt{2} \delta \sin \theta, & \boldsymbol{f}_{8}=\sqrt{2} \delta \sin \theta, \\
\boldsymbol{f}_{7}=\sqrt{2} s_{2}, \sin \theta, & \boldsymbol{f}_{10}=0 .
\end{array}
$$

Here cose $=\left(\vec{s}_{\mu} \vec{p}_{2}\right)=-\left(t_{\mu}\right.$ 呮 $\left.^{\prime}\right)$, where $\vec{t}_{\mu}$ is the unit vector of the muon polarization and $\vec{p}_{2}=\vec{p}_{2} \quad / P_{2} \quad 15$ the unit vector in the direction of the neutrino momentum; $\delta=1-s_{\mu} \beta_{2}$, where $s_{2}= \pm 1$ and $\beta_{2}=\left|\vec{\beta}_{2}\right|$ $=P_{2} / E_{2}$ are the helicity and the velocity of the muonic neutrino.

After summing eq. (3) over. neutrino spin states, we obtain the following expressions for the functions $\boldsymbol{F}_{i}(i=1,2, \ldots, 10) \mathbf{I C}^{\circ}$

$$
f_{1}=4\left(1+\beta_{2} \cos \theta\right), \quad f_{2}=4\left(\beta_{2}+\cos \theta\right),
$$

$$
\begin{array}{ll}
\boldsymbol{f}_{3}=4\left(1-\beta_{2} \cos \theta\right), & \boldsymbol{f}_{4}=-8\left(\beta_{2}-\cos \theta\right), \\
\boldsymbol{f}_{5}=4\left(1-\beta_{2} \cos \theta\right), & \boldsymbol{f}_{6}=-2 \sqrt{2} \beta_{2} \sin \theta, \\
\boldsymbol{f}_{7}=-2 \sqrt{2} \sin \theta, & \boldsymbol{f}_{8}=2 \sqrt{2} \sin \theta, \\
\boldsymbol{f}_{7}=-2 \sqrt{2} \nu \sin \theta, & \boldsymbol{f}_{10}=0 .
\end{array}
$$

The further averaging of expression (3) over the muon spin states gives a simple form of the functions $\dot{f}_{1}$ :

$$
\begin{array}{lll}
\boldsymbol{f}_{1}=4, & f_{2}=4 / \xi_{2}, \quad f_{3}=4, & f_{4}=-8 \beta_{2}, \\
f_{5}=4, \quad f_{6}=-2 \sqrt{2} \beta_{2}, \quad f_{7}=-2 \sqrt{2}, & f_{8}=2 \sqrt{2}, \\
f_{7}=-2 \sqrt{2} \beta_{2}, \quad \quad f_{10}=0 . & \tag{8}
\end{array}
$$

In the case of unpolarized muons and for production of the longitudinally polarized neutrino the functins $f_{i}$ are given by

$$
\begin{align*}
& f_{1}=2 s, \quad f_{2}=-2 s_{2} \varepsilon_{0} \quad f_{3}=2 \varepsilon, \quad f_{4}=4 s_{2} \delta, \\
& f_{5}=2 \varepsilon, \quad f_{6}=\sqrt{25}{ }_{2} \delta, \quad f_{7}=-\sqrt{2} \delta, \quad f_{8}=\sqrt{2} \delta, \\
& f_{9}=\sqrt{2}_{5, \delta}, \quad f_{10}=0 . \tag{9}
\end{align*}
$$

For the polarized muon capture by the polarized ${ }^{6}$ Li nuclei in the framework of the shell model with the harmonic oscillator potential the matrix elements $F_{M 1}, F_{C 1}^{5}, F_{L 1}^{5}$ and $F_{E 1}^{5}$ have the form

$$
F_{M 1}=\frac{1}{\sqrt{\pi}} \frac{q}{M_{n}} e^{-y}\left[k_{1} F_{1}+\mu\left(k_{2}+k_{3} y\right)\right],
$$

$$
\begin{align*}
& F_{E 1}^{5}=\frac{2}{\sqrt{\pi}} e^{-y}\left(k_{2}+k_{3} y\right) F_{A}, \\
& F_{C 1}^{5}=\frac{1}{\sqrt{\pi}} \frac{q}{M_{n}} E^{-y}\left[k_{4} F_{A}+\left(k_{5}+k_{G} y\right)\left(q_{0} F_{F}+2 M_{n} F_{T}\right)\right] \text {, } \\
& F_{L_{1}}^{5}=-\frac{2}{\sqrt{\pi}} e^{-y}\left(k_{5}+k_{G^{y}}\right)\left(F_{A}-\frac{q^{2}}{2 M_{n}} F_{F}\right) .  \tag{10}\\
& \text { Here } k_{1}=0.178: k_{2}=0.561 ; k_{3}=-0.554 ; k_{4}= \\
& 8.6 \cdot 10^{-3} ; k_{5}=-0.397 ; k_{6}=0.295 ; y=(b q / 2)^{2} \text {, } \\
& \text { where } b \text { ( }=2.03 \text { fm [18]) is the oscillator } \\
& \text { parameter. } \\
& \text { In the long wave lenth limit }\left\langle q / M_{n} \approx \square, y \approx \square\right\rangle \\
& \text { the function determining the differential rate of } \\
& \text { the } \mu^{-} \text {-capture by the polarized nuclei, is given by } \\
& F\left(\Theta, \Theta^{*}, \phi^{*}\right)=F_{A}\left(2 f_{1}+f_{3}\right)+4 q \mp_{2} F_{2}-q f_{4} F_{T}+ \\
& +A F_{2}\left(\cos \theta^{*}\right)\left[F_{A}\left(f_{1}-f_{3}\right)+2 q f_{2} F_{2}+q f_{4} F_{T}\right]+ \\
& +A P_{2}^{1}\left(\cos ^{*}\right) \cos _{4}^{*} \sqrt{ } / 2\left(f_{6} F_{A}+q f_{7} F_{2}-q f_{B} F_{T}\right)+ \\
& +\frac{A}{2} P_{2}^{2}\left(\cos \theta^{*}\right) \cos 2 \theta^{*} f_{10} F_{A}+3 F_{1}\left(\cos \theta^{*}\right)\left(f_{2} F_{A}+\right. \\
& \left.+2 \mathrm{qf}{ }_{1} \mathrm{~F}_{2}\right)+3 \sqrt{2} \mathrm{FF}_{1}{ }^{1}\left(\cos \theta^{*}\right) \cos _{4}^{*}\left(\mathrm{f}_{7} \mathrm{~F}_{\mathrm{A}}+\mathrm{qf}_{6} \mathrm{~F}_{2}-\right. \\
& \left.-q f_{q} F_{T}\right)= \tag{11}
\end{align*}
$$

The angular distribution of the neutrino with respect to the muon spin orientation is described bu the asymmetry coefficient, defined by

$$
\begin{equation*}
a_{\mu \nu}=\frac{d W\left(\vec{s}_{\mu} \uparrow \uparrow \vec{p}_{2}^{O}\right)-d W\left(\vec{s}_{\mu} \uparrow \downarrow \vec{p}_{2}^{O}\right)}{d W\left(\vec{s}_{\mu} \uparrow \vec{p}_{2}^{0}\right)+d W\left(\vec{s}_{\mu} \uparrow \downarrow \vec{p}_{\nu}^{O}\right)} \tag{12}
\end{equation*}
$$

Ety neglecting the terms proportional to $\mathrm{q}_{\mathrm{g}} / \mathrm{M}_{\mathrm{N}}$ and $q^{2} / M_{N}^{2}$ in the case of unpolarized nuclei and neutrino, we obtain a simple expression for the coefficient $\sigma_{\mu 2}$ with allowance for the form factor $F_{T}$ :

$$
\begin{equation*}
a_{\mu \nu}=\frac{1}{3} \mathcal{F}_{2},\left\{1-\frac{B}{3} E_{\nu} \frac{F_{T}}{F_{A}}\right\} \tag{13}
\end{equation*}
$$

In this formula the dependence on $m_{2}$ is quadratic through the neutrino velocity $P_{2}=\left\{1-\left[m_{2} /\left(E_{\mu}-\right.\right.\right.$ AE) $\}^{2} y^{1 / 2}$. Eq. (13) may be used to estimate the neutrino mass $m_{2}$ and the form factor $F_{T}$. At $F_{T}=$ $1.4 \cdot 10^{3} \mathrm{MeV}^{1}$ the relative contribution from SCC to the coefficient $\alpha_{\mu 2}$, is 40\%. For unpolarized nuclei a detailed analysis of the contribution from SCC to the coefficient on has been done in [10, 17].

Dne of the interesting characteristics of process (1) is the coefficient of the asymmetry between the polarization directions of the muon ( ${\underset{S}{*}}_{\mu}$ ) and the nucleus ( $\vec{s}_{n}$ ), defined by

$$
A_{M n}=\frac{d W\left(s_{\mu} T \mid \vec{s}_{n}\right)-d W\left(s_{\mu} T \mid \vec{s}_{n}\right)}{d W\left(s_{\mu} T \mid \vec{s}_{n}\right)+d W\left(s_{\mu} T \mid s_{n}\right)}
$$

where ${ }_{5}^{5}$ is a unit vector in the nuclear polarization direction.

The coefficient $a_{m n}$ for the $\left(1^{+} \rightarrow \theta^{+}\right)$-transition has the form

$$
\begin{equation*}
A_{1 n}=\frac{\mathrm{PH}_{3}}{\mathrm{H}_{1}+\mathrm{AH}_{2}} \tag{15}
\end{equation*}
$$

where the functions $H_{i}(i=1,2$, 3$)$ ar:z given by the expressions
$H_{1}=3+\beta_{2} \cos \theta+2 E_{2} \tilde{F}_{T}\left(\beta_{2}-\cos \theta\right)+4 E_{2} \tilde{F}_{2}\left(\beta_{2}+\cos \theta\right) ;$
$H_{2}=2 \hat{\beta}_{2} \cos \theta+E_{2} \beta_{2}\left(3 \cos { }^{2} \theta-1\right)\left(\tilde{F}_{2}-\tilde{F}_{T}\right)+2 E_{2} \cos \theta\left(\tilde{F}_{2}+\tilde{F}_{T}\right):$
$H_{3}=-\xi\left[1+\beta_{2} \cos \theta-E_{w} \mathcal{F}_{w} \tilde{F}_{T} \sin n^{2} \theta+E_{2} \tilde{F}_{2}\left(f_{w} \cos { }^{2} \theta+2 \cos \theta+\beta_{w}\right)\right]$.

Here and below ${\underset{F}{X}}^{X}=F_{X} / F_{A}$ (where $X=2, T$. Note: that $H_{1}$ give the differential rate averaged over the parent nucleus spin states.

If $e=\pi / 2$ and the neutrino mass is neglected, the coefficient $A_{\mu n}$ is expressed as:

$$
\begin{equation*}
A_{\mu n}=-P\left\{1-(1 / 3) \beta_{2} E_{2},\left[F_{2}(1-A)+\tilde{F}_{T}(5+A)\right]\right\} \tag{17}
\end{equation*}
$$

At the alignment equal to one $(A=1)$ we obtain

$$
\begin{equation*}
A_{\mu n}=-P\left(1-2 B_{2} E_{2} \tilde{F}_{T}\right) \tag{18}
\end{equation*}
$$

In this case the relative contribution from SCC to the coefficient $A_{\mu n}$ at $F_{T}=1,410^{-3} \mathrm{MeV}^{-1}$ is $\approx 40 \%$ Note that the information on the value and sign (relative to the form factor $F_{2}$ ) of the form factor $F_{T}$ may be obtained but using expression (18).

At $\theta=\theta^{\circ}$ and $A \neq 1$ the coefficient $A_{\mu n}$ will differ from zero only if the non-zero neutrino mass exists, and in this case $A_{\mu}$ is equal to
$A_{\text {An }}=\cdot-(3 / 4)\left(m_{2}^{2} / E_{2}^{2}\right) F\left[1-2 E_{2}\left(\tilde{F}_{2}+\tilde{F}_{T}\right)\right] /\left(1-\hat{F}_{2} A\right)$.
The latter equation may be used . to determine the muon neutrino mass.

For the coefficient $A_{\text {Hn }}$ after integrating the dit+erential capture rate, we obtain the expression

$$
\begin{equation*}
A_{1-n}=F\left\{1+(2 / 3) E_{2}(1-A)\left(\tilde{F}_{2}+\tilde{F}_{T}\right)\right\} \tag{20}
\end{equation*}
$$

It follows from here that the contributions from SCC and weak magnetism to the coefficient $A_{\text {An }}$ in this case are correlated and it will be difficult to differentiate between them.

Thus, the present limits on the form factor $F_{T}$ maus be 1 mproved bu studying the coefficient $A_{\mu n}$ at various values of alignment $A$.
 $\left.\vec{S}_{\mu}\right) \times \vec{S}_{\mu}$. Then, after summing the differential rate over the neutrmo spin states for the asymmetry coefficient defined by

$$
\begin{equation*}
A_{S}=\frac{d W\left(\xi_{n} T H_{s}\right)-d W\left(\xi_{n} T \|_{s}\right)}{d W\left(\vec{s}_{n} T \|_{5}\right)+d W\left(\vec{s}_{n} \uparrow \|_{u_{s}}\right)} \tag{21}
\end{equation*}
$$

we obtain the expression

$$
\begin{equation*}
A_{S}=\frac{\mathrm{PH}_{3}}{H_{1}+A H_{2}} \tag{22}
\end{equation*}
$$

The function $H_{1}$ is given in (16) and the functions $\mathrm{H}_{2}$ and $\mathrm{H}_{3}$ have the form
$H_{2}=-\hat{\beta}_{2} \cos \theta+E_{2} \dot{\beta}_{2}\left(\sin \tilde{2}_{\theta-1}\right)\left(\tilde{F}_{2}-\tilde{F}_{T}\right)-E_{2} \cos \theta\left(\tilde{F}_{2}+\tilde{F}_{T}\right) ;$
$H_{3}=3 \sin \theta\left[\beta_{2}+E_{2} \beta_{2} \tilde{F}_{\mathrm{T}} \cos \theta+E_{2} \tilde{F}_{2}\left(2-\beta_{2} \operatorname{cose}\right)\right]$.
In the case of $e=\pi / 2$ the coefficient $A_{S}$ has the form

$$
A_{5}=F\left[\dot{B}_{2}+(2 / \Xi) E_{2}\left(\tilde{F}_{2}-\tilde{F}_{T}\right)(1-A)\right]
$$

At $A=1$ there are no contributions from the form tactors $\mathrm{F}_{\mathrm{T}}$ and $\mathrm{F}_{2}$ to the coefficient $\mathrm{A}_{5}$. At $e=0$ and $\pi$ the coefficient $A_{S}$ is equal to zero.

In the case of the polarization of nuclei in the direction that is perpendicular to the reaction plane $\left(\vec{F}_{7} \uparrow \mid \vec{p}_{\nu}, x \quad \vec{S}_{\mu}\right)$, the asymmetry coefficient, defined by

$$
d W\left(\vec{\theta}_{n} \prod_{\left.\mid \vec{P}_{\omega} \times \vec{S}_{3}\right)}\right. \text { - dW(unpol ar.) }
$$

dW (unpol ar.)
15 proportional to the alignment $A$ and has the form $A_{N}=-A\left[F_{A} \beta_{n+} \cos \theta-E_{n+} F_{T}\left(\beta_{m+}-\cos \theta\right)+E_{2+} F_{2}\left(\mathcal{F}_{2+}+\cos \theta\right)\right] / H_{1}-$

The function $H_{1}$ is given in (16).
At cose $=-1$ for the massless neutrino the coefficient $\mathcal{A}_{N}$ is expressed as

$$
\begin{equation*}
A_{N}=(1 / 2) A \tag{27}
\end{equation*}
$$

and in the case of cose $=+1$ the coefficient $\mathcal{A}_{\mathrm{N}}$ is given by

$$
\begin{equation*}
A_{N}=-(1 / 4) A \tag{28}
\end{equation*}
$$

In these cases the coefficient $A_{N}$ does not depend on the form factors $F_{T}$ and $F_{2}$.

At cose $=0$ the coefficient $A_{N}$ is equal to

$$
\begin{equation*}
A_{\mathrm{N}}=-(1 / 3) A E_{2},\left(\tilde{F}_{2}-\tilde{F}_{\mathrm{T}}\right) \tag{29}
\end{equation*}
$$

which is the same as the expression for the coefficient $A_{N}$ obtained after the integration of differential rate (3).

Thus, the analysis shows that for getting information on the form factor $F_{T}$ the angular dependences of various correlation coefficients ( $a_{\mu+\rightarrow}, A_{\mu}, A_{S}$ and $A_{N}$ ) in the $\mu^{\text {- }}$-capture bu the polarized nuclei should be investigated. At $\theta=-\pi / 2$ and $A=1$ the coefficient $A_{\rho}$ depends only on the form factor $F_{T}$, and at $\theta=\theta^{\circ}$ and $A \neq 1$ the coefficient $A_{\rho}$ is not equal to zero only if a non-zero neutrino mass exists. In the case of $\theta=$ $\pi / 2$ the coefficient $A_{5}$ depends on the form factors $F_{2}$ and $F_{T}$ only when $A \neq 1$. At $\Leftrightarrow=\theta^{0}$ and $\pi$ the coefficient $A_{N}$ does not depend on the form factors $F_{2}$ and $F_{T}$, and at $\theta=\pi / 2$ the quantitu $A_{N}$ is proportional to the difference between $F_{2}$ and $F_{T}$.

## REFERENCES

1. Weinberg 5. Phus. Rev., 1958, v. 112, p. 1375.
2. Langacker F. Fhys. Fev., 1977, v. D15, p. 2386.
3. Lobov G. A. Frreprint ITEP-65, 1987.
4. Morita M. Hyperf. Interact. 1985, v. 21, p. 143
5. Minamisono T. et al. Hyperf. Interact., 1987, v. 34, P. 135.
6. Kurihara Y. J. Sci. Hirochima Univ., 1987, V. AS1, p. 1.
7. Albrecht H. et al. Phys.Lett., 1987,v.B195,p.307.
8. Derrick M. et al. Phus. Lett., 1987, V. B189,p. 260. 9. Albrecht W.H. et al. Preprint DESY 88-113, 1988. 10. Kathat C.L. Preprint JINR E6-88-121, Dubna, 1988.; Kathat C.L. Sov. J. Izv. Akad Nauk. Ser. Fiz. (in Kussian), 1989, v. S3, p. 103.
9. Balashow V.V., Korenman G. Ya. and Eramzyan fi.A., Absorption of mesons by atomic nuclei (in Russian), M. :Atomizdat, 1978.
10. Samsonenko N.V., Samgin A.L., Kathat C.L. Sov. J. of Nuclear Phys. 1988, v. 47, p. 348.
11. Samsonenko N.V., Kathat C.L., Samgin A.L. Nucl. Phys., 1989, v. A491, p. 642.
12. Samsonenko N.V., Kathat C.L., Ousmane M.A., Samgin A.L. Preprint JINF Fb-88-925, Dubna, 1988.
13. Brilyev E.V., Kathat C.L. Sov. J. of Izv. Akad. Nauk, Ser. Fiz. (in Russian), 1988, v.52, p.7.
14. Kathat C.L. Izv. Akad Nauk Kazakhs SSR, Fiz.-Mat. Ser. (in Fussian) 1986, N 4, p. 54.
15. Kathat C.L., Samsonenko N.V. Preprint JINR R6-88-926, Dubna, 1988.
16. Walecka J.D. In: Muon Physics, V. 2/Eds Hughes U.W., Wu C.S. New York: Acad. Press, 1975,p. 113.
17. Donnelly T.W. New Vistas in Electro-Nuclear Physics. - New York-London, Plenum Press, 1986, p. 151.
18. Donnelly T.W., Kaskin A.S. Ann. Phys., 1986, v. 169, P. 247.

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