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ROLE OF DEUTERON NN^* -COMPONENTS
IN PROCESSES $pd \rightarrow dp$ AND $pd \rightarrow dN^*$

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Роль NN^* -компонент в дейтроне в процессах $pd \rightarrow dp$ и $pd \rightarrow dN^*$

Вычислен вклад обмена нуклонными изобарами N^* в упругое pd -рассеяние назад на основе шестикварковой модели дейтрона и установлено, что он пренебрежимо мал по сравнению с обменом нейтроном. Показано, что полюсная амплитуда подхвата нейтрона из nN^* компоненты дейтрона выделена в реакции $pd \rightarrow dN^*$ при вылете назад изобар $N^*(1440)$ и $N^*(1710)$ при кинетической энергии начального протона в л-системе 1,5—2 ГэВ, в то время как амплитуда треугольной диаграммы с подпроцессом $pp \rightarrow d\pi^+$, опирающаяся на обычную pn -компоненту дейтрона, существенно подавлена.

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Role of Deuteron NN^* -Components
in Processes $pd \rightarrow dp$ and $pd \rightarrow dN^*$

The contribution of nucleon isobar N^* exchanges to backward elastic pd -scattering is calculated on the basis of deuteron 6q-model and found to be negligible in comparison with neutron exchange. It is shown that the pole amplitude of neutron pickup from the deuteron nN^* -component is favoured in the reaction $pd \rightarrow dN^*$ for backward going $N^*(1440)$ and $N^*(1710)$ at kinetic energy of incident proton of 1.5—2 GeV whereas the triangular diagram with subprocess $pp \rightarrow d\pi^+$ related to the usual pn -component of deuteron is considerable suppressed.

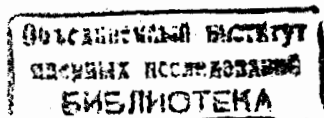
The investigation has been performed at the Laboratory of Nuclear Problems, JINR.

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1 Introduction

An idea of preexistence of nucleon isobars in the deuteron at short NN-distances suggested for the first time in Ref. [1] is compatible both with the meson exchange theory [2] and 6-quark picture of the deuteron structure [3]. Backward elastic pd -scattering, $pd \rightarrow dp$, is one source of information on the short-range structure of the deuteron. According to calculations [1] based on the Regge phenomenology and analysis [4] performed in the meson exchange theory the contribution of the NN^* -component to the $pd \rightarrow dp$ process is essential to explain the experimental data at energies $\sim 1\text{GeV}$. However, the application of the Regge-model at rather low energies as well as considerable uncertainties in knowledge on $\text{meson} - N - N^*$ vertices make these estimations questionable. Developed in last decade, the 6-quark model of the deuteron [5]-[8] provides a new regular approach to construction of dNN^* -vertices. In this model the deuteron structure at short relative NN-distances $r_{NN} \leq 1\text{fm}$ is determined by superposition of nonexcited s^6 and excited $s^4p^2 - s^52s$ 6-quark shell-model configurations. Presence of two-quantum excitations in the configuration $s^4p^2 - s^52s$ is a reason for the phenomenological repulsive core in the NN-interaction potential [7]. Besides, the excited quark configuration leads to an admixture of a small NN^* -component in the deuteron wave function. The effective numbers and momentum distributions are calculated in the framework of this approach [8, 9]. Recently the results [9] for dNN^* vertices were found sufficient [10] to explain the available experimental data on the inclusive reaction of deuteron disintegration $d + A \rightarrow p(0^\circ) + X$ [11] within the $n + N^*$ -exchange mechanism.

In this work the contribution of N^* -exchanges to $pd \rightarrow dp$ (Fig.1,a) is calculated in the interval of incident proton kinetic energy in the labsystem of $T_p = 0.5 - 3\text{GeV}$



on the basis of the 6-quark model [8, 9] for dNN^* -vertices. As is found here, this contribution is negligible in comparison with the mechanism of neutron exchange calculated in the Born approximation (Fig.1, b) and with account of rescatterings (Fig.1,c-e).

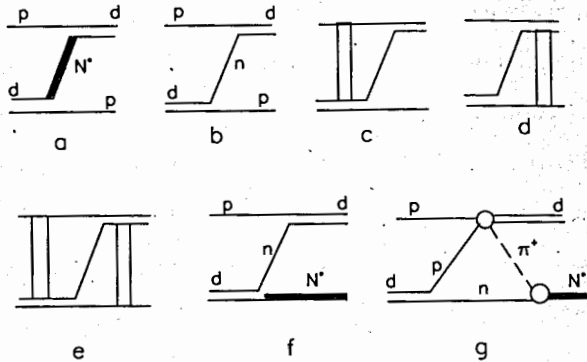


Figure 1: The mechanisms of the $pd \rightarrow dp$ and $pd \rightarrow dN^*$ processes: the one baryon exchange (OBE) (a - f); the neutron exchange (NE) in the Born approximation (b, f) and taking into account rescatterings (c - e); the triangular diagram of one-pion exchange (OPE) (g).

Furthermore we investigate the reaction $pd \rightarrow dN^*$ for the backward going N^* -isobar in the framework of the neutron exchange (NE) pole diagram (Fig.1,f) and triangle diagram (Fig.1,g) of one-pion exchange (OPE). The experimental investigation of the $pd \rightarrow dN^*(1440)$ reaction is planned at SATURNE [12].

If the NE-mechanism dominates, this reaction can give the direct information

on the deuteron nN^* -component. The OPE amplitude involves the usual np -component of the deuteron and masks the NN^* -component. However, as will be shown here, for the nucleon-like $N^*(1/2^+)$ -states there is a kinematic region for the $pd \rightarrow dN^*$ reaction in which the OPE mechanism is considerably suppressed.

2 The model

The relativistic effects play an important role in the NE-mechanism at energies $\geq 1\text{GeV}$, especially for the $d \rightarrow p+N^*$ channel with large binding energy, $\varepsilon \sim 500\text{MeV}$ [13]. In order to allow for relativistic effects we use here the phenomenological relativistic approach for the three-body problem developed in Ref. [14]. In this approach the amplitude of the process $pd \rightarrow dB$, where B denotes either a proton (for $pd \rightarrow dp$) or N^* (for $pd \rightarrow dN^*$), in the framework of one baryon exchange (OBE) can be written as a direct generalization of the $pd \rightarrow dp$ formalism of Ref. [15]

$$A_{OBE} = 4\sqrt{E_d(E_p + E_N)E_d'(E_B + E_N)} \frac{\sqrt{s} - M_0}{E_N} \sum_{|N\rangle} \left\{ \Psi_{\lambda'}^{\sigma_p \sigma_N}(\mathbf{q}') \right\}^+ \Psi_{\lambda}^{\sigma_B \sigma_N}(\mathbf{q}). \quad (1)$$

Here $E_k = \sqrt{m_k^2 + \mathbf{p}_k^2}$ and \mathbf{p}_k are the energy and momentum of the k -th particle in the $p+d$ c.m.s., m_k is its mass; $M_0 = E_N + E_p + E_B$; \sqrt{s} is the invariant mass of the $p+d = d+B$ system; $\Psi_{\lambda'}^{\sigma_p \sigma_N}(\Psi_{\lambda}^{\sigma_B \sigma_N})$ is the deuteron wave function in the channel $d \rightarrow Np$ ($d \rightarrow NB$) normalized to the effective number, N_{pN}^d , of the corresponding channel

$$\frac{1}{2J_d + 1} \sum_{\lambda, \sigma_p, \sigma_N} \int |\Psi_{\lambda}^{\sigma_p \sigma_N}(\mathbf{q})|^2 \rho_{pN}^{-1}(q) \frac{d^3q}{(2\pi)^3} = N_{pN}^d, \quad (2)$$

where $\rho_{pN}(q) = 2\varepsilon_p(q)\varepsilon_N(q)/[\varepsilon_p(q) + \varepsilon_N(q)]$; $\varepsilon_k(\mathbf{q}) = \sqrt{m_k^2 + \mathbf{q}_k^2}$; σ_j is the spin projection of the nucleon j ($j=p,B,N$); $\lambda(\lambda')$ denotes the spin projection of the initial (final) deuteron. The sum over the internal states φ_N , including σ_N , of the

transferred baryon N (neutron or N^*) is assumed in Eq. (1). Two combinator factors $\sqrt{2}$ are included in Eq.(1) since the 6-quark deuteron wave function is fully antisymmetric. The arguments \mathbf{q} and \mathbf{q}' of the initial and final deuteron wave functions can be written in the following form

$$\mathbf{q}' = \mathbf{p}_p - \frac{\varepsilon_p(\mathbf{q}') + E_p}{\varepsilon_N(\mathbf{q}') + E_N + \varepsilon_p(\mathbf{q}') + E_p} \mathbf{d}', \quad (3)$$

$$\mathbf{q} = \mathbf{p}_B - \frac{\varepsilon_B(\mathbf{q}) + E_B}{\varepsilon_N(\mathbf{q}) + E_N + \varepsilon_B(\mathbf{q}) + E_B} \mathbf{d}, \quad (4)$$

the relations $\mathbf{p}_N = \mathbf{d} - \mathbf{p}_B = \mathbf{d}' - \mathbf{p}_p$ are used here which are valid in the p+d c.m.s. [14]; \mathbf{d} (\mathbf{d}') is the momentum of the initial (final) deuteron. The amplitude (1) is related to the c.m.s. cross section of $pd \rightarrow dB$ as

$$\frac{d\sigma}{d\Omega} = \frac{1}{64\pi^2 s} \frac{p_B}{p_p} |A|^2. \quad (5)$$

The basis for calculation of dNN^* -vertices is the fully antisymmetric 6q-wave function of deuteron which in the resonating group method (RGM) has a form

$$\Psi_d(1, \dots, 6) = \hat{A}\{\varphi_p(1, 2, 3)\varphi_n(4, 5, 6)\chi(\mathbf{r})\}. \quad (6)$$

Here φ_p and φ_n are the quark wave functions of proton and neutron, $\chi(\mathbf{r})$ is the RGM distribution function for the pn component of deuteron and \hat{A} is the quark antisymmetrizer. When deriving the function $\chi(\mathbf{r})$ one can either calculate it in the microscopic 6q-dynamics or construct it by means of RGM-renormalization procedure [8] for the conventional phenomenological wave function of deuteron in pn-channel, like Paris or RSC. The difference between the effective numbers for these two methods is negligible, of few percentage [8]. To describe the internal quark motion in the baryons the translationally invariant shell model (TISM) is used. The wave function $\Psi_\lambda^{\sigma_B \sigma_N}$ for the channel $d \rightarrow N + B$ entering Eq.(1) is determined by

the overlap integral between the 6-quark wave function of the deuteron, Ψ_d , (6) and the product of the internal wave functions of the baryons, φ_N and φ_B , as $\Psi_\lambda^{\sigma_B \sigma_N} = \sqrt{\frac{6!}{3!3!}} \langle \varphi_N \varphi_B | \Psi_d \rangle$. The details of the formalism and the effective numbers for N^* in the deuteron are presented in Refs. [8, 9].

Rescatterings in the initial and final states for the NE amplitude are taken into account here in the eikonal approximation on the basis of the method developed in Ref. [16]. As a result, besides the Born term (Fig.1, a or b), three additional terms arise allowing for pd-rescattering at small angles in the initial state (Fig.1,c), pp-rescattering in the final state (Fig.1, d) and rescatterings both in the initial and final states simultaneously (Fig.1,e).

The spin-averaged square of the NE-amplitude of the $pd \rightarrow dN^*$ reaction (Fig.1,f) takes the form

$$|A_{NE}(pd \rightarrow dN^*)|^2 = \frac{3}{64\pi^2} K^2 \rho_{pn}(q') \rho_{nB}(q) [u^2(q') + w^2(q')] \Phi_{N_B L_B}^2(q), \quad (7)$$

where K is the same kinematic factor as in front of the sum sign in Eq.(1), u and w are the S- and D-components of the deuteron function in the $d \rightarrow pn$ channel, $\Phi_{N_B L_B}^2(q)$ is the momentum distribution in the channel $d \rightarrow nN^*$ for the N^* -isobar with the number of internal excitation quanta N_B and internal orbital momentum L_B normalized by the condition $\int_0^\infty \Phi_{N_B L_B}^2(q) q^2 dq = N_{eff}^{nB} (2\pi)^3$. The corresponding formula for the NE mechanism in $pd \rightarrow dp$ follows from Eq.(7) after substitution $\Phi_{N_B L_B}^2(q) \rightarrow u^2(q) + w^2(q)$. In the framework of the NE-mechanism the tensor polarization of the final deuteron in the $pd \rightarrow dN^*$ reaction has a form

$$T_{20}(\theta_{c.m.} = 180^\circ) = -\frac{1}{\sqrt{2}} \frac{w^2(q') - \sqrt{8}u(q')w(q')}{u^2(q') + w^2(q')}. \quad (8)$$

This formula coincides the one for the $pd \rightarrow dp$ process within the NE-mechanism.

The triangular diagram OPE with the subprocess $pp \rightarrow d\pi^+$ was investigated in [16, 17] in the analysis of the $pd \rightarrow dp$ process. Generalization of the formalism from Refs. [16, 17] to the $pd \rightarrow dN^*$ reaction is quite obvious if we restrict ourselves to the nucleon-like states of N^* , $J^P = 1/2^+$. In this case the only difference between the reactions $pd \rightarrow dN^*$ and $pd \rightarrow dp$ is the mass inequality, $m_p \neq m_{N^*}$. Consequently, the modification of the formalism from Refs. [16, 17] has a kinematic character. It results in the following form for the spin-averaged square of the OPE amplitude

$$|A(pd \rightarrow dN^*)|^2 = \frac{3}{2} \frac{\tilde{G}^2}{4\pi} \tilde{F}^2(k^2) \frac{E_{N^*} + m_{N^*}}{E_{N^*}^2} (f_{01}^2 + f_{21}^2) \frac{3}{2} |A(pp \rightarrow d\pi^+)|^2, \quad (9)$$

where $\tilde{F}^2(k^2)$ is the πNN^* -formfactor; for the estimation we use the monopole πNN -formfactor as \tilde{F} ; according to Ref.[18], for the Roper resonance $N^*(1440)$ the squared coupling constant $\tilde{G}^2/4\pi$ in the πNN^* -vertex equals 14.7×0.472^2 ; the same value we use for the $\pi NN^*(1710)$ vertex in accordance with arguments of Ref. [4]; E_{N^*} and p_{N^*} are the total energy and momentum of the N^* -isobar in the lab-system; the nuclear formfactors for the S- and D- components of the deuteron ($l=0, 2$) $f_{1l}(p_{N^*})$ are expressed via r-space integrals of the product of the deuteron wave function $\psi_l(r)$ and the spherical Bessel function of the first order, $j_1(p_{N^*} m_{N^*} r / E_{N^*})$ (see details in Refs. [16, 17]). Such a form for $f_{1l}(p_{N^*})$ comes from the p-wave nature of the πNN and $\pi NN^*(1/2^+)$ vertices. Owing to the equality $j_1(x=0) = 0$, the formfactor $f_{1l}(p_{N^*})$ becomes zero at the point $p_{N^*} = 0$ and the OPE-amplitude (9) vanishes, too. The rest point in the lab-system for the N^* -isobar is at $T_p = 1.876 \text{ GeV}$ for $N^*(1440)$, 2.75 GeV for $N^*(1535)$ and 6.86 GeV for $N^*(1710)$.

3 Numerical results and discussion

The numerical calculations are performed with the Paris wave function for the np-component and its RGM-modification [9] for the NN^* -component of the deuteron. The sum over ten TISM states listed in Tabl.2 of Ref.[9], for which the effective numbers $N_{NN^*}^d$ are not less than 10^{-5} , is carried out in the Eq. (1) in calculation of the OBE-amplitude of $pd \rightarrow dp$ process. The cross section of the $pd \rightarrow dN^*$ reaction is

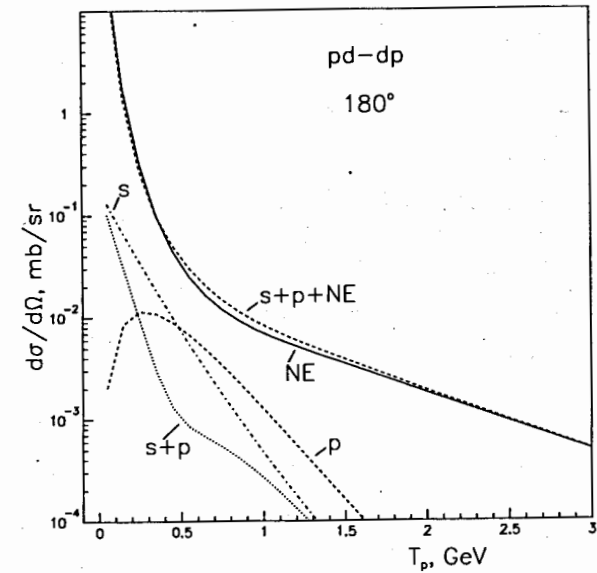


Figure 2: The calculated cross section of $pd \rightarrow dp$ at $\theta_{c.m.} = 180^\circ$ as a function of kinetic energy of incident proton in the lab-system T_p within the OBE mechanisms: the neutron exchange (full curve, NE), the positive parity N^* exchange (s), the negative parity N^* exchange (p), the total contribution of N^* -exchanges ($s+p$), the coherent sum of $n + N^*$ exchanges ($s+p+NE$).

calculated here under assumption that N^* is a stable state to simplify the com-

parison with $pd \rightarrow dp$ process. The contribution of N^* -exchanges to the $pd \rightarrow dp$ cross section is shown in Fig.2. The total contribution of N^* -states of positive parity (s-waves) and negative parity (p-waves) to the $pd \rightarrow dp$ cross section is by a factor of > 30 smaller than the neutron exchange. In the energy interval $T_p = 0.5 - 1\text{GeV}$

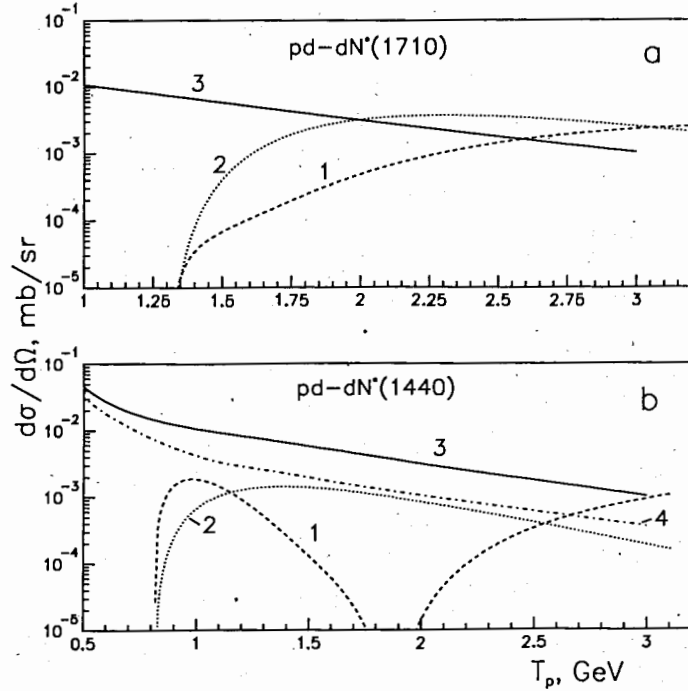


Figure 3: The cross section of the $pd \rightarrow dN^*$ reaction at $\theta_{c.m.} = 180^\circ$ calculated within the different mechanisms as a function of T_p for $N^*(1710)$ (a) and $N^*(1440)$ (b): curve 1 - OPE, 2 - NE. The $pd \rightarrow dp$ cross section within the NE mechanism is shown by curve 3 (for the diagram in Fig 1,b) and 4 (for the coherent sum of four diagrams in Fig.1,b - e).

the p- contribution increases the OBE-cross section by a factor of ~ 1.3 due to interference with the neutron exchange amplitude. However, the interference be-

tween the s- and p-wave amplitudes of N^* -exchange is destructive. As a result, the total contribution of N^* -exchanges to the cross section and T_{20} of the $pd \rightarrow dp$ process is negligible. We should note that, on the contrary, in the inclusive reaction $d + A \rightarrow p(p^0) + X$ the interference between s- and p-waves of N^* -exchanges does not occur [9]. We found numerically that the cross section of $pd \rightarrow dp$ at $\theta_{c.m.} = 180^\circ$, $T_p = 1 - 3\text{GeV}$ within the NE-mechanism decreases by a factor $\sim 2 - 3$ due to rescatterings and practically does not change its form as a function of T_p (Fig.3,b). The tensor polarisation T_{20} is modified by the rescatterings by not more than 5-10%.

The small contribution of N^* -exchanges to $pd \rightarrow dp$ is mainly due to the small effective numbers of N^* -isobars in deuteron, $N_{NN}^d < 10^{-2}$. Unlike N^* -exchanges in the $pd \rightarrow dp$ amplitude including two dNN^* vertices (Fig.1,a), the NE-amplitude of the $pd \rightarrow dN^*$ reaction (Fig.1,f) contains only one dNN^* vertex. Therefore the modulus of this amplitude can be larger than that of the amplitude in Fig.1.a. Moreover, there is an additional enhancement factor for the NE-mechanism of the $pd \rightarrow dN^*$ reaction in the case of s-states of relative motion in the $d \rightarrow n + N^*$ channel, namely, the presence of a point with zero relative momentum $\mathbf{q} = 0$ (4) in this channel. For the Roper resonance the point $\mathbf{q} = 0$ lies at $T_p = 1.2\text{GeV}$ and for $N^*(1710)$ at 2.2GeV . It is easy to find that the point $\mathbf{q} = 0$ arises in the nonrelativistic kinematics, too.

For the N^* isobars of negative parity the NE-amplitude is strongly suppressed in the vicinity of the point $\mathbf{q} = 0$ because of p-wave behaviour of the momentum distribution in the dnN^* vertex. As follows from Fig.3,a, the modulus square of the NE-amplitude of the $pd \rightarrow dN^*(1710)$ reaction is the same order of magnitude as that for the $pd \rightarrow dp$ process and by one order of magnitude larger than the OPE-

contribution in the energy interval of $T_p = 1.5 - 2\text{GeV}$. For the Roper resonance $N^*(1440)$ the NE-contribution is also comparable with that for $pd \rightarrow dp$ (Fig.3,b).

This conclusion is mainly determined by the effective numbers $N_{NN(1710)}^d = 6.75 \cdot 10^{-3}$ [9], $N_{NN(1440)}^d = 10^{-3}$ [8] and not changed after substituting the harmonic oscillator wave function $\varphi_{00}(q)$ with the oscillator parameter $b = 0.6\text{fm}$ [6] or $b = 0.8\text{fm}$ [9] for the RGM-modified Paris wave function [9]. Furthermore the NE-mechanism of the $pd \rightarrow dN^*$ reaction can be indentified by measurement of tensor polarisation. We found from Eq.(8) that the tensor polarisation of the final deuteron in the $pd \rightarrow dN^*$ reaction at $T_p = 1 - 3\text{GeV}$ is $T_{20} \sim 0.6 - 0.7$ both for the $N^*(1440)$ and $N^*(1710)$ nucleon isobars. T_{20} is approximately constant since at energies of $T_p = 1 - 3\text{GeV}$ the argument q' in Eq.(8) slowly varies in the interval of $0.7-0.8\text{ GeV}/c$ for $N^*(1440)$ and $0.9-1.0\text{ GeV}/c$ for $N^*(1710)$. Otherwise the tensor analyzing power of this reaction in respect of the initial deuteron is zero for the NE-mechanism, $t_{20} = 0$. In accordance with the above notes after Eq. (9), the OPE mechanism predicts a deep minimum in the cross section of $pd \rightarrow dN^*(1440)$ at proton energy $T_p = 1.876\text{GeV}$ (Fig.3,b) which corresponds to the rest point of $N^*(1440)$ at that energy. Thus, in conclusion, there are favourable conditions in the interval $T_p = 1.5 - 2\text{GeV}$ to pick out the contribution of the NE-mechanism in the $pd \rightarrow dN^*$ reaction for backward going $N^*(1710)$ and $N^*(1440)$ nucleon isobars and to search for the corresponding NN^* components of the deuteron.

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