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## THE SHAPE OF FAST-ROTATING NUCLEI

IN THE REGION OF SUBSHELL $\mathbf{N}=82$

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## 1- INTRODUCTION


#### Abstract

The nuclear reactions with heavy ions allow to obtain the compound-nucleus states with angular momenta as high as I $\sim 60-80 \%$ and with appreciable excitation energy. To analyse the experimental data, one needs the knowledge of the parameters characterizing the average selfconsistent nuclear field, the deformation energy, the inertia properties of the nuclei, as well as the level-density of the excited nuclei.


The dependence of the nuclear shape on the rotational frequency has been studied theoretically by several authors. The effect of the rotation was investigated by Cohen, Plasil and Swiatecki ${ }^{1 /}$ in the framework of the nuclear droplet model. The Dubna-Rössendorf collaboration ${ }^{2}$, the Lund-Warsaw collaboration ${ }^{\prime \prime}$ and the Jülich group ${ }^{4}$ ) carried out investigations of nuclear-shape properties at high angular momenta using the shell-correction method developed by Strutinsky ${ }^{5}$ ). In ref. ${ }^{6)}$ the combined effects of nuclear rotation and statistical excitation have been considered.

In the present work me investigate the fast-rotating nuclei in the vicinity of the magic neution number $N=82$. We focus our attention on "near-cold" nuclei (very amall excitation energies) and discuss the influence of increasing the nuclear temperature on the shell-effects. We determine the spin-values at which oblate-to-prolate transition occurs in different erbium isotopes, as a function of the neutron number. We also illustrate the influence of shell-effects on the moment of inertia.

For the description of fast-rotating nuclei we employ the model developed in ref. ${ }^{6}$ ). The model unifies two different approaches : a method used in the description of fast-rotating cold nuclei ${ }^{2-4}$ ) and a statistical approach for the determination of the properties of low-spin excitations. To simplify the model, we disregard the pairing correlations whose effects are important only at low temperatures (t $<0.6 \mathrm{MeV}$ ) and small angular momenta ( $\mathrm{I}<25-30$ f).

Using the Strutinsky shell-correction method and averagiog statistically the Routhian function $R(\beta, \omega, t)$ of a rotating nucleus, one obtains 1) :

$$
\begin{equation*}
R(\hat{\beta}, \omega, t)=E_{L D}(\hat{\beta})+\sum_{V} \varepsilon_{v}^{\omega}(\hat{\beta}) \overline{\bar{n}_{v}}(t)-\overline{\sum_{v} \varepsilon_{v}^{\omega=0}(\hat{\beta}){\overline{n_{v}}}_{v}(t=0)} \tag{1}
\end{equation*}
$$

Here $\hat{\beta}$ is a set of deformation parameters, $\omega$ is the rotational frequency and $t$ is the nuclear temperature. The liquid-drop component of the energy $E_{L D}(\hat{\beta})$ calculated in the droplet-model ${ }^{7)}$ is :

$$
\begin{equation*}
E_{L D}(\hat{\beta})=E_{S}^{s p h}\left[\left(B_{S}(\hat{\beta})-1\right)+2 x\left(B_{C}(\hat{\beta})-1\right)\right] \tag{2}
\end{equation*}
$$

where $B_{C}$ and $B_{S}$ describe the Coulomb and nuclear-surface energy, respectively, and are normalized so that they become unity for spherical nuclei :

$$
\begin{align*}
\mathrm{E}_{\mathrm{S}}^{\mathrm{Sph}} & =17.9439\left[1-\mathrm{k}\left(\frac{\mathrm{~N}-2}{\mathrm{~A}}\right)^{2}\right] \mathrm{A}^{2 / 3} \mathrm{MeV}  \tag{3}\\
x & =\left(2^{2} / \mathrm{A}\right) /\left[\left.50.88\left(1-k\left(\frac{\mathrm{~N}-\mathrm{Z}}{\mathrm{~A}}\right)^{2}\right) \right\rvert\,\right.  \tag{4}\\
k & =1.7826 .
\end{align*}
$$

The eigenvalues of the one-particle Routhian-function, $\varepsilon_{v}(\hat{\beta})$, are given by :

$$
\begin{align*}
& h^{\omega}(\hat{\beta})\left|\theta_{v}^{\omega}(\hat{\beta})\right\rangle=\varepsilon_{v}^{\omega}(\hat{\beta})\left|\theta_{v}^{\omega}(\hat{\beta})\right\rangle  \tag{6}\\
& h^{\omega}(\hat{\beta})=h(\hat{\beta})-\omega j_{x}, \tag{7}
\end{align*}
$$

where $h(\hat{\beta})$ is the one-particle hamiltonian of the self-consistent nuclear field. Eq. (I) can be written as :

$$
\begin{align*}
& R(\hat{\beta}, \omega, \mathrm{t})=\mathrm{E}_{\mathrm{LD}}(\hat{\beta})+ \\
& {\left[\sum_{v} \varepsilon_{v}^{\omega}(\hat{\beta}) \bar{n}_{v}(t)-\sum_{v} \varepsilon_{v}^{\omega}(\hat{\beta}) \bar{n}_{v}(t=0)\right]+} \\
& {\left[\begin{array}{l}
{\left[\sum_{V}^{\omega} \varepsilon_{V}^{\omega}(\hat{\beta}) \bar{n}_{V}(t=0)-\overline{\sum_{V}^{E_{V}^{\omega}}(\hat{\beta}) \bar{n}_{V}(t=0)}\right]+} \\
{\left[\sum_{V}^{E_{V}^{\omega}(\hat{\beta})} \bar{n}_{V}(t=0)\right.}
\end{array} \overline{\sum_{V}^{\varepsilon_{V}^{\omega}=0}(\hat{\beta})} \bar{n}_{V}(t=0)\right]=} \\
& R_{L D}(\hat{\beta}, \omega)+U(\hat{\beta}, \omega, t)+\delta R_{\text {shell }}(\hat{\beta}, \omega, t=0) . \tag{8}
\end{align*}
$$

Here, $U(\hat{\beta}, \omega, t)$ represents the excitation energy of the rotating nucleus

$$
\begin{equation*}
U(\hat{\beta}, \omega, t)=\sum_{V} \varepsilon_{V}^{\omega}(\hat{\beta})\left[\bar{n}_{V}(t)-\bar{n}_{v}(t=0)\right] \tag{9}
\end{equation*}
$$

and $\delta \mathrm{R}_{\text {shell }}(\hat{\beta}, \omega, t=0)$ is the Strutinsky shell correction for a rotating nucleus at temperature $t=0$ :

$$
\begin{equation*}
\delta R_{\text {shell }}(\hat{\beta}, \omega, t=0)=\sum_{V} \varepsilon_{V}^{\omega}(\hat{\beta}) \bar{n}_{V}(t=0)-\overline{\sum_{V} \varepsilon_{V}^{\omega}(\hat{\beta}) \vec{n}_{V}(t=0)} . \tag{10}
\end{equation*}
$$

The occupation numbers, $\bar{n}_{v}(t)$, are given by the Fermi distribution :

$$
\begin{equation*}
\bar{n}_{v}(t)=\left\{1+\exp \left[\left(\varepsilon_{v}^{\omega}(\beta)-\bar{\lambda}\right) / t\right]\right]^{-1} \tag{11}
\end{equation*}
$$

with the chemical potential, $\bar{\lambda}$, determined by the number of particles (protons or neutrons) contained in the considered system:

$$
\begin{equation*}
{\underset{z}{\mathbf{N}}\}=\sum_{v}}_{n_{v}}(t) \tag{12}
\end{equation*}
$$

The angular frequency $\omega$ and spin I are related by :

$$
\begin{equation*}
I=\sum_{V}\left(j_{x}\right)_{V V} \bar{n}_{V}(t), \tag{13}
\end{equation*}
$$

where the matrix elements, $\left(j_{x}\right)$, are expressed in the representation of the eigenvectors of the Routhian-function (7). $R_{T . D}(\hat{B}, \omega)$ is the Routhian of a rotating liquid drop :

$$
\begin{equation*}
R_{L D}(\hat{\beta}, \omega)=E_{L D}(\hat{\beta})-1 / 2 \omega^{2} \bar{J}(\hat{\beta}, \omega) . \tag{14}
\end{equation*}
$$

In the above formula the averaged moment of inertia $\bar{J}(\hat{\beta}, \omega)$ is defined as :

$$
\begin{equation*}
-1 / 2 \omega^{2} \bar{J}(\hat{\beta}, \omega)=\overline{\sum_{V} \varepsilon_{V}^{\omega}(\hat{\beta}) \bar{n}_{v}(t=0)}-\overline{\sum_{V} \varepsilon_{V}^{\omega=0}(\hat{\beta}) \bar{n}_{V}(t=0)} . \tag{15}
\end{equation*}
$$

As is known, the moment of inertia averaged according to the Strutinsky shell-correction method using a velocity-independent nuclear field is close to the rigid-body value. It follows then that, for the WoodsSaxon self-consistent field, one obtains :

$$
\begin{equation*}
\bar{J}(\hat{\beta}, \omega) \rightarrow J_{\mathbf{r l g}_{\mathrm{g}}}(\hat{\beta}) . \tag{16}
\end{equation*}
$$

In the statistical treatment of the properties of beated nuclei other thermodynamic potentials are also convenient :
a) The Gibbs-Routhian function :

$$
\begin{equation*}
F_{R}(\hat{\beta}, \omega, t)=R(\hat{\beta}, \omega, t)-t S(\hat{\beta}, \omega, t), \tag{17}
\end{equation*}
$$

b) The Gibbs function (free energy) :

$$
\begin{equation*}
F(\hat{\beta}, I, t)=F_{R}(\hat{\beta}, \omega(I), t)+\omega(I) I \tag{18}
\end{equation*}
$$

and
c) the energy at a fixed value of the entropy :

$$
\begin{equation*}
E(\hat{\beta}, I, S)=E(\hat{\beta}, I, S=0)+U(\hat{\beta}, \omega(I), t(S)), \tag{19}
\end{equation*}
$$

where $E(\hat{\beta}, I, S=0)$ is the energy on the yrast line and $U(\hat{\beta}, I, S)$ is the excitation energy above the yrast line at fixed spin $I$. The entropy of a heated nucleus is defined by :

$$
\begin{equation*}
S(\hat{\beta}, \omega, t)=\sum_{v}\left[\left(\varepsilon_{v}^{\omega}(\hat{\beta})-\bar{\lambda}\right) \bar{n}_{v}(t) / t-\ln \left(1-\bar{n}_{v}(t)\right)\right] \tag{20}
\end{equation*}
$$

The results presented in this paper have been obtained using the Woods-Saxon potential $(8,9)$.

$$
\begin{equation*}
v(\vec{r}, \hat{\beta})=v_{o} /[1+\exp (\ell(\vec{r}, \hat{\beta}) / a)] \tag{21}
\end{equation*}
$$

where $V_{o}$ is the depth of the potential-well and a is the diffuseness of the nuclear surface. The function $\ell(\vec{r}, \hat{\beta})$, describing the distance between a given point $\vec{r}$ and the nuclear surface, has been determined numerically and taken negative for points inaide the nucleus. For spherical nuclei : $\ell(r, \hat{\beta}=0)=r-R_{0}$, where $R_{0}=r_{0} A^{1 / 3}$ is the radius of the corresponding spherical nucleus.

The usual form of the spin-orbit interaction bas been assumed :

$$
\begin{equation*}
\mathrm{v}_{\mathrm{SO}}(\vec{r}, \vec{\beta})=-\lambda\left(\frac{\hbar^{2}}{2 \mathrm{MC}}\right)[(\vec{\nabla} \mathrm{V} \times \vec{p}) \cdot \overrightarrow{\mathrm{s}}]_{\mathrm{r}} \rightarrow\left(r_{\mathrm{o}}\right)_{\mathrm{SO}} \tag{22}
\end{equation*}
$$

where $\vec{p}$ and $\vec{s}$ are nucleon momentum and spin operators respectively, and $V$ is given by eq. (21) with ( $r_{0}$ ) so being the corresponding spin-orbit interaction radius given in the table. The Coulomb potential for protons has been determined as a classical electrostatic potential of a uniformly charged nucleus with a nuclear surface given by eq. (23) below, and a coulomb radius of the central part of the potential $:\left(r_{o}\right)_{C}=1.275 \mathrm{fm}$. The nuclear surface for moderate deformations can be expressed in the aultipole expansion as :
where $\beta_{L M}^{*}=(-1)^{M} \beta_{L-M} ; \Omega$ stands for the set of the polar angles $(\varphi, \theta)$. The function $C(\beta)$ secures the conservation of the nuclear volume with the changes of nuclear surface.
One can choose a coordinate system in which :

$$
\begin{equation*}
\beta_{2 \pm 1}=0, \quad \beta_{2+2}=\beta_{2-2} \tag{24}
\end{equation*}
$$

and introduce parameters $\beta_{2}$ and $\gamma{ }^{10}$ )

$$
\begin{align*}
& \beta_{20}=\beta_{2} \cos \gamma \\
& \beta_{22}=\beta_{2-2}=\frac{\beta_{2}}{\sqrt{2}} \sin \gamma \tag{25}
\end{align*}
$$

In such a parametrization of the quadrupole degrees of freedom, axially symmetric nuclear surfaces are described by $\gamma=k_{\frac{\pi}{3}}^{\pi},(k=0, \pm 1, \pm 2, \pm 3)$. To extend this property to hexadecapole degrees of freedom we have used the Cayley-Hamiliton theorem to write the spherical, rank-four tensor, $\mathrm{B}_{4 \mathrm{M}}$ as :

$$
\begin{aligned}
& \beta_{40}=\frac{\beta_{4}}{6}\left(5 \cos ^{2} \gamma+1\right) \\
& \beta_{42}=\beta_{4-2}=\frac{\beta_{4}}{6} \sqrt{\frac{15}{2}} \sin 2 \gamma \\
& \beta_{44}=a_{4-4}=\frac{\beta_{4}}{6} \sqrt{35}=2^{2} \because \\
& \beta_{4 \pm 1}=\beta_{4 \pm 3}=0 .
\end{aligned}
$$

A more general parametrization of the hexadecapole deformation has been suggested recently in ref.(11).
This leaves us with a set of three independent deformation parameters, $\hat{\beta}=\left(\beta_{2}, \beta_{4}, \gamma\right)$. Since the full minimization with respect to the bexadecapole deformation parameter $\beta_{4}$ is practically beyond our technical possibilities, its value has been inferred from the minimization of the liquid drop energy with respect to $B_{4}$ for a prolate $\left(\gamma=0^{\circ}\right.$, rotation around the axis perpendicular to the symmetry axis) and an oblate shape ( $\gamma=-60^{\circ}$, rotation around the symmetry axis).

Fig. 1 presents the dependence of $\beta_{4}$ on $\beta_{2}$ for $\gamma=0^{\circ}$ and $\gamma=-60^{\circ}$, for two spin-values : $I=0$ and $I=60$. It can be seen that the difference between the equilibrium deformations for $I=0$ and $I=60$ is not very significant. Thes, in the subsequent calculations the hexadecapole deformation $\beta_{4}$ has been deduced from its equilibrium value for the liquiddrop at $i=0$. The values of $\beta_{4}$ for $0^{\circ}>\gamma>-60^{\circ}$ have been detemined by a linear interpolation at fixed $\beta_{2}$.

All calculations presented in this paper have been carried out using the level spectrum of ${ }^{158} \mathrm{Er}$. The relevant values of parameters are listed in Table I.

The calculations were carried out for even isotopes of erbium : $146-154 \mathrm{Er}$ and ${ }^{158} \mathrm{Er}$. The heaviest of the studied isotopes represent a stably deformed nucleus, the lighter ones represent the transitional nuclei. The position of these nuclei in the periodic table makes them an interesting field of investigation, both for the theorists and experimentators.

The results of our calculations for the energy surfaces are given in figs. 2-9. Each of the figures shows several energy surfaces obtained for different characteristic values of the spin. The results are presented in triangular plots as contour lines in the $\beta_{2}-\gamma$ plane. The parameter $\beta_{2}$ measures the distance from a given point in the plot to the left vertex. The angle $\gamma$ changes from $\gamma=0^{\circ}$ at the lower edge (a prolate nucleus rotating around the axis perpendicular to the symmetry axis of the field) to $\gamma=-60^{\circ}$ at the upper edge (the oblates shape with coinciding symmetry and rotation axes). The lines in the plots are contour-lines corresponding to a given equal free-energy. The interval separating the neighbouring lines is 0.5 MeV . The "valleys" in the free-energy landscape are indicated by shaded areas, the darker ones corresponding to the deeper depression.

Most of the calculations were periormed ion $L=0.2$ iiciv. Sucit value of the temperature does not destroy the shell-effects and, at the same time, facilitates the interpolation procedure used in the calculations. The effects of statistical excitation were studied for ${ }^{154} \mathrm{Er}$ at temperatures $t=0.6 \mathrm{MeV}$ and $t=1.2 \mathrm{MeV}$. Comparing our figures one can see that the shell effects enrich the structure of the energy surfaces, leaving the poaitions of the main minima at about the same place. At $t=0.2 \mathrm{MeV}$ the shell effects generate very complicated free-energy surfaces, at $t=0.6$ MeV the low-scale variations of the energy are already washed out, and at $t=1.2 \mathrm{MeV}$ the shell effects are not seen in the energy surfaces at all. A more detailed information concerning the spin-dependence of the equilibrium deformation is given in figs. 10 and 11 . The above-mentioned tendencies can be seen from these figures too. Figs. 12 and 13 show the moment of inertia of $148,154 \mathrm{Er}$ as a function of $\omega^{2}$. The large-scale variations of the oments of inertia are related to the changes in the nuclear shape. Such changes appear as combined effects of the shell and the liquid-drop forces. The additional shell-effects, not related to the shape transitions, are also visible in the figures as low-scale fluctuations disappearing at moderate temperatures ( $t=0.6 \mathrm{MeV}$ ). At high temperatures there remains a large
bump in the moment of inertia, corresponding to the transition from the oblate to the three-axial close-to-prolate configurations

The shell effects determine also the critical value of spin at which the oblate-to-prolate transition taices place. As is seen in fig. 14, the dependence of such spin values on the neutron number $N$ is rather strong : it increases from around 40 th to more than 70 then going from ${ }^{146} \mathrm{Er}$ to ${ }^{154} \mathrm{Er}$. Similar conclusions are obtained in ref.12), although our values for such spins are somewhat larger as compared to those of ref.12)

Calculations of the nuclear shape properties in ${ }^{154} \mathrm{Er}$ are also reported in ref.13) for zero temperature. The comparison of fig. 6 in the present work ( $\mathrm{T}=0.2 \mathrm{MeV}$ ) with fig. 1 l in ref.13) shows a qualitative agreement of these calculations.

As is seen in figs.2-9, the free energy surfaces have more than one minimum for small temperatures. Such is the situation in ${ }^{154} \mathrm{Er}$. The energies of states in ${ }^{154} \mathrm{Er}$ corresponding to different winima are shown in fig. 15 as functions of the spin. One sees that the yrast-line in this nucleus consists of several lines : the deformation changes slowly with the spin in each of these lines, but undergoes a rather drastic change with the change of the yrast configuration.

It is useful to present the results by calculating the rotational frequency $\omega_{\text {rot }}(\mathrm{I})$ as a function of the nuclear spin for each of the confi-
 determines the energy spacings of the states with different values of spins belonging to such configurations. If one considers the stretched quadrupole $\gamma$-transitions with $\Delta I=2$ which go along the yrast line or along the lines corresponding to other low-lying configurations, one has for the energy of $\gamma$-quanta the expression $E_{\gamma}(I)=2 \omega_{\text {rot }}(I)$.

As an example in fig. 16 we present the energies of stretched E2 $\gamma$-quanta as functions of the spin for ${ }^{154} \mathrm{Er}$. The different curves in fig. 16 correspond to the energies of $\gamma$-rays cascading along the different configurations shown in fig. 15. The number of $\gamma$-rays in a given interval of energy which are emitted from the high-spin states is related to the slope of the curves. A plateau may be assocfated with an accumulation of $\gamma$-rays with the same energy. The same is expected for those values of $E_{Y}(I)$ which correspond to more than one curve, because in this case, one may envisage the emission of $\gamma$-rays in cascades going along different lines.

Thus the irregularities in the curves in fig. 16 (in particular, the position of plateaux) may be associated with the bumps in the intensity spectra of $\gamma$-rays emitted from the high-spin nuclear states. The spectra of quasi-continuous $\gamma$-rays following ( $\mathrm{HI}, \mathrm{xn}$ ) reactions are known experimen-
tally in a number of cases. Strong irregularities in the intensity of $\gamma$-rays, $n_{\gamma}\left(E_{\gamma}\right)$, are found in the case of the nucleus ${ }^{154}{ }^{E r}{ }^{14-20)}$ : the cascade starting in the region of spins of about $I \sim 60-70 \mathrm{n}$ produces the spectrum of $\gamma$-rays with $n_{\gamma}\left(E_{\gamma}\right)$ having two strong bumps. The positions of the two maxima of $n_{\gamma}\left(E_{\gamma}\right)$ are indicated in fig. 16 by dotted lines.
As is seen, these positions may be explained, at least partially, by the spin dependence of the energies of different nuclear configurations.

## 3 - CONCLUDING REMARKS

In this paper we investigated theoretically the erbium isotopes from the well-deformed to the quasi-spherical regions. The evolution of the shape of the nuclear surface has been studied as a function of spin for different number of neutrons ( $78 \leqslant \mathrm{~N} \leqslant 90$ ).
 the point of view of experiments in which the multiplicity and energy distributions of $\gamma$-quanta following the ( $\mathrm{HI}, \mathrm{xn}$ ) reaction are measured. Such experiments have been done during the last years ${ }^{(14-20)}$. As is shown above the shape variations and the resulting changes in the nuclear moment of inertia determine the spectrum of that part of the $\gamma$-spectrum which corresponds to the yrast cascade in the nucleus obtained in the fusion process. A more detailed analysis of the $\gamma$-spectra obtained in the C.S.N.S.M. (Orsay) ${ }^{(16,17)}$ and based on the calculations reported here is in progress.

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Parameters of the average field potential for ${ }^{158} \mathrm{Er}$

|  | Central potential |  |  | Spin orbit interaction |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{gathered} r_{0} \\ (\mathrm{fm}) \end{gathered}$ | $\begin{gathered} a \\ (f \mathbb{f}) \end{gathered}$ | $\begin{gathered} v_{0} \\ (\mathrm{MeV}) \end{gathered}$ | $\begin{gathered} \left(r_{0}\right)_{s o} \\ (f m) \end{gathered}$ | $\begin{aligned} & \mathbf{a}_{\mathbf{s o}} \\ & (\mathrm{fm}) \end{aligned}$ | $\lambda$ |
| protons | 1.275 | 0.70 | -55.5 | 0.901 | 0.70 | 18.9 |
| neutrons | 1.347 | 0.70 | -43.7 | 1.221 | 0.70 | 33.3 |



Fig. 1 : The dependence $\beta_{4}$ on $\beta_{2}$ for the prolate ( $\gamma=0^{\circ}$ ) and oblate ( $\gamma=60^{\circ}$ ) shapes resulting from the minimization of the liquid-drop energy. Calculations correspond to ${ }^{154} E_{I}$ and are shown for two values of the $\operatorname{spin}$ ( $\mathrm{I}=0$ and $\mathrm{I}=60 \mathrm{n}$ ) indicated at the lines.




Fig.3: Same as in fig. 2 for ${ }^{148-154} \mathrm{Er}$ and ${ }^{158} \mathrm{Er}$.








F1g. 13 : The moment of inertia as a function of the square of the rotational frequency for ${ }^{148} \mathrm{Er}$. (temperature $\mathrm{t}=0.2 \mathrm{MeV}$ ).


Fig. 14 : The value of the spin 1 , at which the oblate-to-prolate transition occurs, given as a function of the neutron number for Erbium 1 sotopes.


Fig. 15: The structure of the yrast-11ne in ${ }^{154}{ }^{\mathrm{Er}}$ ( $\mathrm{T}=0.2 \mathrm{MeV}$ )


Fig. 16 : Energies of the stretched E2 transitions along the different configurations in ${ }^{154}$ Er shown in fig. 15.

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[^0]Цвек С., Михайлов Н.Н., Бриансон Ш.
E4-83-401
Форма быстровращающихся атомных ядер
из окрестности магической оболочки $\mathrm{N}=82$
Используя метод оболочечной поправки Струтинского, исследованы быстровращающиеся ядра изотопов эрбия из окрестности магической оболочки $N=82$. В качестве среднего поля использован потенииал Вудса-Саксона с учетом неаксиальной гексадекапольной деформации. Рассчитаны параметры равновесных деформаций и моменты инериии при разных значениях спинов ндер. Исследовано влияние нагревания ядра на его оболочечные эффекты.

Работа выполнена в Лаборатории теоретической Физики ОКЯИ.

Препринт Объединенного института ядерных исследованнй. Дубна 1983
Cwiok S., Mikhailov I.N., Briancon Ch.
E4-83-401 The Shape of Fast-Rotating Nucle
in the Region of Subshell $N=82$
The fast rotating erbium nuclei in the vicinity of $N=82$ are investigated in the framework of the Strutinsky shell-correction method using the Woods-Saxon potential including non-axial hexadecapole deformations. The equilibrium deformation and moment of inertia are calculated for different spin values. The influence of nuclear temperature on the shelleffects is also discussed.

The investigation has been performed at the Laboratory of Theoretical Physics, JINR.


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