ОБЪЕДИНЕННЫЙ ИНСТИТУТ ЯДЕРНЫХ ИССЛЕДОВАНИЙ ДУБНА

12/11-24

E4: - 7812

2330 2-74 A.I.Vdovin, Ch.Stoyanov

....

11用11

V-33

MIXING OF THE VIBRATIONAL AND TWO-QUASIPARTICLE EXCITATIONS IN ISOTONES N=80,82,84



ТЕОРЕТИЧЕСНОЙ ФИЗИНИ

E4 - 7812

A.I.Vdovin, Ch.Stoyanov

MIXING OF THE VIBRATIONAL AND TWO-QUASIPARTICLE EXCITATIONS IN ISOTONES N=80,82,84

Submitted to "Изв. AH CCCP;

The present paper is devoted to a rather widely discussed recently problem about an interaction of vibrational and two-quasiparticle excitations in even-even atomic nuclei.

The semimagic and neighbouring to them nuclei have such an energy gap that the two-phonon and two-quasiparticle states have nearly the same excitation energies. If so, even not very strong interaction may cause sensible mixing of these excitations and complicating of the structure of "true" states.

Within the framework of superfluid nuclear model 9 the above situation has been investigated already for deformed nuclei $^{1/}$. For spherical nuclei such investigations have been made quite recently $^{2-4/}$. There it has been shown that the admixture of noncollective components may be rather significant.

The account of the above admixture in the structure of "two-phonon" states is of importance not only in itself. If the only collective degrees of freedom (for anharmonic terms of Hamiltonian not higher than those cubic in the number of phonon operators) are allowed for in calculations then, as is known (7.8), the energy of 2^+_2 level is very high, the quantity $B(F2,0^+_{\pm},s^2_2)$ is larger by an order than the experimental one and the sequence of levels in triplet $0^+_1, 4^+_1, 2^+_2$ is given strictly.

In papers 77 it is pointed out that inclusion of the noncollective components into the wave function of $2_2^+, 4_1^+$ states can improve a theoretical description.

We have calculated characteristics of a series of 2^+ and 3^- levels in the isotones N=80,82,84. The energies

of states, probabilities of electromagnetic transitions, quadrupole moments have been computed. All the details of calculations and arguments for basic approximations can be found in paper $^{/3/}$ We give here only the expression for the state wave function Ψ_{μ} (IM)

$$\Psi_{\nu}(\mathbf{IM}) = \{\sum_{i} C_{i}^{\nu} Q_{\mathbf{IMi}}^{+} + \sum_{\substack{\lambda_{1} \mu_{1} i_{1} \\ \lambda_{2} \mu_{2} i_{2}}} \Delta_{\lambda_{1} i_{1}}^{\lambda_{2} i_{2}} (\mathbf{I}_{\nu}) < \lambda_{1} \mu_{1} \lambda_{2} \mu_{2} \} \mathbf{IM} > Q_{\lambda_{1} \mu_{1} i_{1}}^{+} \times Q_{\lambda_{2} \mu_{2} i_{2}}^{+} \\ \times Q_{\lambda_{3} \mu_{3} i_{3}}^{+} \{ |0 > ph \}$$
(1)

and the secular equation for the energy η_{11} of this state:

$$\det \{ (\omega_{[1} - \eta_{[\nu]}) \delta_{ii}, -K(ii \gamma) \} = 0.$$
 (2)

The following conventions are used in (1), (2): $Q_{\lambda\mu i}^+$, $Q_{\lambda\mu i}$ are, respectively, the phonon creation and annihilation operators with moment and projection $\lambda_{,\mu}$ and number i; ω_{1i} is the energy of phonon with quantum numbers IMi, $\langle \lambda_{,\mu} | \lambda_{,\mu} | M \rangle$ - the Clebsch-Gordan coefficient, ν -the number of root of eq. (2).

Note that 1, λ_1 , $\lambda_2 = 2,3$. The expression for coefficients K(ii') can be found in paper $^{3/}$. The operator of $E\lambda$ -transition which we have employed in calculations of probabilities of the electric transitions and quadrupole moments is taken from book $^{9/}$ (Chapter 6, Sect. 3). The wave function (1) which includes the components not higher than two-phonons permits one to calculate states with an excitation energy not higher than 2.5-3.0 MeV for positive parity and 3.5-4.0 MeV for negative parity. Accordingly, the summation over i in (1) is restricted, $i \leq 4$.

The Hamiltonian of spherical nucleus consists of average field for neutron and proton systems and the following residual interactions: pairing, quadrupole-quadrupole and octupole-octupole.

The average field is described by the Saxon-Woods potential with the following parameters:

a) for the proton system: A=141; Z=59; $r_0=1.24$ fm, V₀ = 58.0 MeV, $\kappa = 0.349$ fm², $\alpha = 1.587$ fm⁻¹; b) for the neutron system with N>82: A=137, $r_0 = -1.28$ fm, V₀ = 43.4 MeV, $\kappa = 0.413$ fm²; $\alpha = -1.28$ fm, V₀ = 43.4 MeV, $\kappa = 0.413$ fm²; $\alpha = -1.28$ fm, V₀ = 43.4 MeV, $\kappa = 0.413$ fm²; $\alpha = -1.28$ fm, V₀ = 43.4 MeV, $\kappa = 0.413$ fm²; $\alpha = -1.28$ fm, V₀ = 43.4 MeV, $\kappa = 0.413$ fm²; $\alpha = -1.28$ fm² fm 1.613 fm^{-1}

c) for the neutron system with N < 82: A = 141, r₀=1.27 fm, $V_0 = 46.5$ MeV, $\kappa = 0.409$ fm², $\alpha = 1.613$ fm⁻¹.

Here A is the atomic number, Z - the proton number, R = r, A^{1/3} - the potential radius, V₀-the potential depth, κ - the constant of spin-orbital part of the potential,

 α - the parameter of diffusion of the potential boundary.

The choice of these parameters was made on the basis of papers ⁽¹⁰⁾ Single-particle schemes and matrix elements of multipole operators were calculated by the program of paper 'IT

The constants of pairing interaction were chosen to ensure the correct description of pair energies . In calculations only the levels of open shell were involved. The values obtained for the correlation function and chemical potential are in good agreement with the results of papers /12/ The constants of quadrupole-quadrupole and octupole-octupole forces were taken for each nucleus in such a way that the values of η_{21} and η_{31} coincide with the experimental energies of 2^+_1 and $3^-_1_1$ levels, respectively. The effective charge used for describing the electromagnetic transitions and quadrupole moments is taken to equal 0.6 for all nuclei.

Calculating energies of two-quasiparticle states in the isotones N=80,84 we have taken the blocking effect 9/ into account. The account of this effect results decreasing of energies of two-quasiparticle states in by 200-400 keV as compared to the values calculated with the correlation function of the ground state. The main result of this decreasing is just the energy lowering of the second and higher roots of eq. (2) and change of the structure of their wave functions. An example of the above changes is given in Table 1 (for ^{140}Nd and ^{144}Nd). Allowing for the blocking effect has caused the energy lowering of the second 2^+ levels by 100-250 keV. Note also should be made that the blocking effect changes the

The influence of blocking effect on the energy and struc-

ture of the wave function of the states with $1^{\pi} = 2^+, 3^-$ in isotones N=80,84

| | T. | E KeV | With | out blocking effect | Ţ | With blocking effect |
|--------------------|-------------------|-------|-------------------------------|---|--------|--|
| Nucleu | 19 ^I i | exp. | Z _{zy} KeV theory | Structure of the wave funct. | theory | Structure of the wave function |
| | 21 | 697 | 723 | 81.1% 2 + + 9.3% Q + Q + | 704 | $B3.7\% Q_{21}^{\dagger} + 10\% Q_{21}^{\dagger} Q_{21}^{\dagger}$ |
| ¹⁴⁴ Nd- | 2 ⁺ 2 | 1556 | 1852 | 7.65 Q_{ac}^{+} + 63.15 Q_{ac}^{+} + + 1.25 Q_{ac}^{+} +1.35 Q_{ac}^{+} + 255 Q_{ac}^{+} Q_{ac}^{+} | 1715 | 3.4% Q_{μ}^{\dagger} +82.6% Q_{aa}^{\dagger} + 10.7% Q_{μ}^{\dagger} Q_{aa}^{\dagger} |
| | 34 | 1510 | 1484 | 66.7%Q + +4.4%Q + +26%Q | 1505 | $69.7\%Q_{M}^{+}$ 24.2%Q_{AL}^{+}Q_{M}^{+}+3.5% Q_{33}^{+} |
| | 32 | 2776 | 3110 | 2.8% Q_{1}^{+} +70.5% Q_{2}^{+} +14.4% Q_{2}^{+} +0.4% Q_{1}^{+} Q_{1}^{+} +5.8% Q_{2}^{+} Q_{2}^{+} + + 3.6% Q_{2}^{+} Q_{2}^{+} | 2995 | $1.8\%Q_{31}^{+} +80\%Q_{32}^{+} +8\%Q_{33}^{+} +1\%Q_{31}^{+} Q_{31}^{+} + 4.2\%Q_{41}^{+} Q_{33}^{+}$ |
| ¹⁴⁰ Nd. | 21 | 775 | 783 | $78.6\% Q_{a}^{\dagger} + 15.2\% Q_{a}^{\dagger} Q_{a}^{\dagger}$ | 731 | 77% Q_{at}^{+} + +4.3% Q_{at}^{+} Q_{at}^{+} |
| | 22 | 1490 | 2069 | $9\% \ Q_{21}^{\dagger} + 30\% \ Q_{22}^{\dagger} + 11\% \ Q_{32}^{\dagger} + 34.6\% \ Q_{41}^{\dagger} + 6.6\% \ Q_{22}^{\dagger} \ Q_{42}^{\dagger}$ | 1822 | $\begin{array}{r} 11.6\% \ Q_{a1}^{+} + 47.5\% \ Q_{a1}^{+} + 9.7\% \ Q_{a3}^{+} \\ + \ 17.6\% \ Q_{a1}^{+} + 8.9\% \ Q_{a1}^{+} \ Q_{a1}^{+} \end{array}$ |

structure of phonons themselves, as well, especially the noncollective ones, and, besides, diminishes slightly the strength of interaction between quasiparticles and phonons.

The numerical results are presented in Tables 2 (for states with $I^{\prime\prime\prime} = 2^+$) and 3 (for those with $I^{\prime\prime\prime} = 3^-$). The experimental data are taken from papers $^{/14-19}$. At first we will say a few words concerning the general properties of the results obtained. Mainly we shall speak about 2^+ levels where we have more experimental information.

Inclusion of the noncollective components into the structure of wave function of the 2^+ states, as was expected, results in a sensitive improvement of description of energies of the $2\frac{1}{2}$ levels. For instance, in ¹⁴⁴Nd nucleus for the same parameters the energy of the second 2^+ level appears to be equal to 2429 keV when we allow for the collective components in (1) only, and this one equals 1715 keV when switching on the noncollective components (experimental value for this level is 1556 keV). Analogously, also the description of probabi-lities of E2 transitions $2\frac{1}{2} \cdot 0^+_{R,B}$ becomes better. However, the decrease of quantities resulting from the insertion of noncollective components into the wave function of states proves to be not always sufficient for correct 21 description of experimental data. For a series of nuclei where the quasiparticle-phonon interaction is strong, the component $Q_{21}^+ Q_{21}^+$ appears to be suppressed in the structure of $2\frac{1}{2}$ states that results in nonrealistically small value of $B(E2,2^+_2,2^+_1,2^+_1)$. Now we discuss in more detail the structure of studied

Now we discuss in more detail the structure of studied states in various nuclei, starting from the levels $|_{\pi=2}^{+}$

In the isotones N=82 the structure of these states is rather simple and reduces, as a rule, to a single component Q_{2i}^+ . The reason for this is the high energy and weakened collectivization of the 2_{1}^+ state in semimagic nuclei. On the one hand, the two-phonon pole of secular eq. (2) appears to be much higher that the two-quasiparticle ones, and, on the other hand, the quasiparticlephonon interaction proves to be weak. As a result, the intensive mixing of various types of excitations emerges

| Calculated | results | of the properties of excited st | ates |
|------------|-------------------|---------------------------------|------|
| with | $I^{\pi} = 2^{+}$ | in isotones N=80,82,84 | |

| | | E | 2 t) Kev | B(22,0) | -2;+)¢6 | Q, | (2;†) e-6 | B(E2,2,++2,2)e4 |
|-----------------|---|---------------|-----------|---------|--------------------|-------|-----------|---------------------|
| fucleus | 1 | exp. | theor. | exp. | theor. | exi | , theor. | theor. |
| 134 Ka | I | 847 | 819 | - | 0,36 | - | 0,27 | 0.075 |
| | 2 | 1613 | I493 | - | 0,02 | - | -0,17 | 0,075 |
| | I | 818 | 815 | 0,42 | 0,42 | 0,43 | 0.46 | |
| "Ba | 2 | I55I | 17II | - | 0.06 | - | -0.12 | 0,042 |
| _ | 3 | 2081 | 1858 | - | 0.0004 | ~ | -0,15 | 0.0002 |
| 181 5. | I | 789 | 792 | - | 0.46 | - | 0,58 | |
| 28 | 2 | 15I I | 1825 | - | 0,07 | - | -0,014 | 0.02 |
| NO | I | 755 | 73I | - | 0.46 | - | 0.63 | |
| Ne | 2 | I490 | 1822 | - | 0.08 | - | ~0.016 | 0.014 |
| 134 - | I | I278 | I262 | · - | 0.17 | - | -0.34 | |
| /e | 2 | - | 2030 | - | 0.007 | - | -0.25 | 0.0005 |
| | I | 1313 | 1335 | _ | 0.30 | - | -0.12 | |
| [™] Xe | 2 | 7 | 2107 | - | 0.004 | - | -0.23 | 3x10 ⁻⁵ |
| | 3 | 2640 | 2265 | - | 0.008 | - | -0.19 | 2x10-4 |
| 1N Ba | I | 1436 | 1454 | 0.38 | 0.37 | -0.07 | 0.11 | |
| | 2 | 2218 | 2161 | - | 5xI0 ⁷ | | -0.13 | 0.001 |
| | I | 1596 | 1569 | 0.29 | 0.40 | | 0.23 | |
| "Le | 2 | 2348 | 2246 | - | 3x10 ⁻⁵ | - | -0.03 | 0.002 |
| | з | 2522 | 2269 | - | 0,000I | - | -0.05 | 4x10 ⁻⁴ |
| _ | I | 1576 | 1576 | 0.39 | 0.47 | _ | 0.32 | |
| *** Nd | 2 | 2385 | 2380 | | 0.003 | - | 0.02 | Ix10 ⁵ |
| | з | 2583 | 2405 ^ | - | 0.002 | - | 0.08 | 0.002 |
| | I | 1659 | 1669 | 0,25 | 0,56 | - | 0.27 | |
| "Sni | 2 | 2450 | 2589 | - | 5x10-4 | - | 0.07 | 0.002 |
| | 3 | 2800 | 2652 | - | 0.33 | - | 0.34 | 0.03 |
| 14 01 | I | I570 | 1587 | - | 0.73 | - | -0.21 | |
| 64 | 2 | - | 257I | - | 0.002 | - | 0.1 | 0.13 |
| 144 | I | 64I | 662 | 0.46 | 0.32 | -0.I | 2 -0.40 | |
| Ze | 2 | I536 | I665 | - | 0.16 | - | 0.14 | 0.024 |
| "" Nd | I | 697 | 704 | 0.5I | 0.31 | -0.2 | 3 -0.39 | |
| | 2 | 1556 | 1715 | - 0 | .16 | - | 0.17 | 0.025 |
| | Ι | 747 | 731 | - 0 | .29 | - | -0.45 | |
| "Sm | 2 | I 64 8 | 1903 | - 0 | .I9 | - | 0.24 | 0.015 |
| | 3 | 2157 | 2438 | - 0 | .03 | - | 0.06 | +7xI0 ⁻⁵ |

only in the structure of states corresponding to the high roots of eq. (2). The value of the component $Q_{21}^2 Q_{21}^4$ becomes noticeable (10-20%) only in the wave function of the 2_3^+ state and only for 142 Nd and 144 Sm nuclei. The theoretical and experimental values of energies of

the $2\frac{1}{2}$ levels are in satisfactory agreement, except for 136 Xe nucleus where the $2\frac{1}{2}$ state itself was not observed, (apparently it should have an energy of 2.1-2.3 MeV as the analysis of experimental data on the neighbouring isotones N=82 evidences). Energies of the 2_3^+ levels are systematically lower (by 100-300 keV) than experimental values which is due to inexactitude of the single-particle level scheme. Experimental knowledge on the electromagnetic characteristics of levels is rather poor. The data available (on the 2_1^+ levels only) are in quite good agreement with our calculations. Note that the sign and magnitude which we have found for quadrupole moment of various 2⁺ levels for a single nucleus in the isotones N=82, do not obey the rule stated by authors of the paper 7/, viz: sign $Q_2(2_1^+) = -\text{sign } Q_2(2_2^+)$ and $|Q_2(2_1^+)| < |Q_2(2_2^+)|$. No experimental data exist on the electromagnetic characteristics of higher 2^+ levels. We have compared our results with theoretical calculations of the paper $^{/13}$. There all 2⁺ leve's were treated as one-phonon, the Tamm-Dankoff method was used and effective forces were chosen either of a Gaussian type or in a form of the surface δ -interaction. As compared to our results the authors of ref. /13/ give much larger probabilities of E2-transitions from the 2_2^+ levels into the ground state and very small transitions $2_2^+ + 2_1^+$. Besides, we have opposite signs of quadrupole moments of the 2_1^+ -levels.

The structure of wave functions of states $1^{\pi} = 2^+$ in the isotones N = 80,84 is more interesting. The quasiparticle-phonon interaction is here rather strong so that the ratio $\omega_{21}/\eta_{21} = 1.2$ -1.5. As a result, the two-phonon pole is located very close to the two-quasiparticle ones and in the wave function of 2^+ level a considerable admixture of both the noncollective components and two-phonon ones is observed. In the structure of 2^+_1 level the main component is Q_{21}^+ , from others only the two-phonon component, Q_{21}^+ , Q_{21}^+ , can be observed (it amounts to 10-15%). The description of energies of 2⁺ levels should be recognized as satisfactory though for 2^+_2 levels the energy values obtained are higher than experimental ones. For some nuclei there is an experimental information, though rather poor, on the quadrupole moments and electromagnetic transitions. Our results for the $2\frac{1}{1}$ levels agree quite well with these data. The matter is worse with the 2^+ levels. Here, of course, no direct experimental infor m^2 tion is available on the transition probabilities but for the nuclei $^{136}{\rm Ba}$, $^{134}{\rm Xe}^{/16/}{\rm and} ^{144}{\rm Nd}^{/17/}$ the ratio

 $\frac{B(E2, 2_2^+ \rightarrow 0_{g, \infty}^+)}{B(E2, 2_2^+, 2_2^+)}$ is known which equals approximately

0.02-0.04 for all the three nuclei. Our results give correctly this ratio only for $^{134}\,\chi_e$. As to the nuclei $^{136}\,Ba$ and ¹⁴⁴Nd our value is larger by an order, and even more, than the experimental one. For 136 Ba -nucleus the reason is obviously that the description of the transition 2, + 0, + is bad. This follows from comparison of our calculations with those performed by the Alaga model 15/ . viz; we obtain the same values for $B(E2, 2\frac{1}{2}, 2\frac{1}{2})$ and the values differing by an order for $B(E2, 2\frac{1}{2}, -0\frac{1}{8})$. In this connection one should point out a rather strong sensitiveness of the results to a choice of the signle-particle level scheme. In Table 4 we present the calculations for some nuclei with N=80,84 with changed single-particle schemes (for N=80 the scheme is taken from ref.) In this consideration not only the description of energies of the 2, levels becomes much better but also the results have been distinctly improved for electromagnetic transitions and quadrupole moments in the isotones N=84. Thus, the

ratio $\frac{B(E2, 2_2^+ \to 0_{g.s.}^+)}{B(E2, 2_2^+ \to 2_1^+)}$ in ¹⁴⁴Nd becomes six times

smaller.

The present experimental information on 3^{-} states in the nuclei of interest is much more scanty than for 2⁺ levels. The second 3⁻ levels are known only in two nuclei, 144 Nd and 144 Sm (their energy agrees rather well

10

Calculated results of the properties of excited states with $1^{\prime\prime}=3^{-1}$ in isotones N=80,82,84

| | | E(3]) Kev | | B(E3,0 | Q2(31)e.b | |
|-------------------|--------|--------------------|--------------|-----------|-----------------|--------------|
| Nucleus | 1 | exp. | theor. | exp. | theor. | theor. |
| 142 Ce | I 2 | 1653 ~ | 1654 3114 | I.I3 - | 0.15 0.001 | 0.70 0.34 |
| *** Nd | 1 2 | 1510 2776 | 1505 2995 | 0.26 | 0.18 0.001 | 0.68 0.40 |
| ¹⁴⁶ Sm | I 2 | 1381 - | 1399 2832 | - | 0.21 0.022 | 0.65 0.14 |
| 134 Xe | 1 2 | 3 2 77 - | 3288 3575 | | 0.035 0.0006 | 0.68 0.28 |
| tar Ba | I 2 | 2881 - | 2857 3419 | - | 0.089 0.0004 | 0.64 0.32 |
| **° Ee | I 2 | 2464 - | 2422 3280 | 0.76 - | 0.15 0.0005 | 0.59 0.39 |
| ¹⁴² Nd | I 2 | 2084 | 2041 3149 | 0.44 - | 0.19 0.0009 | 0.59 0.39 |
| *** Sm | I 2 | 1809 3227 | 1846 3059 | - | 0.24 0.001 | 0,52 0,45 |
| *** Gd | 1 2 | 1586 | 1614 3031 | ~ | 0.32 0.001 | 0.38 0.53 |
| ** Ba | I 2 | 2532 - | 2510 3230 | - | 0.II 0.002 | 0.67 0.32 |

Calculated results of the properties of excited states with $I^{\pi} = 2^+$ in isotones N = 80,84 for changed single-particle level scheme

| Nucleus | | E(2') | k 2V | B(E2, 0, | B(E2, 9, -2, +) +5 | | 9e.b | B(E2,2,+~2;)e*b* | |
|------------------|---|-------------|---------------|----------|--------------------|-------|--------|---------------------------------------|--|
| **** | | exp. | theor. | exp. | theor. | exp. | theor. | theor. | |
| ⁶⁴ Ca | I | 78 9 | 771 | - | 0.38 | - | -0.42 | | |
| 6 | 2 | 1511 | I 44 4 | - | 0.18 | - | 0.23 | 0.07 | |
| ⁶⁴ Ba | I | 818 | 794 | 0.42 | 0.36 | +0.43 | -0.44 | | |
| | 2 | 1551 | 1510 | - | 0.11 | - | 0,10 | 0.04 | |
| | 3 | 2061 | 1689 | - | 0.003 | - | 0.29 | 0.004 | |
| ### Nd | I | 697 | 678 | 0.51 | 0.49 | -0.23 | -0.21 | · · · · · · · · · · · · · · · · · · · | |
| | 2 | 1556 | 1488 | - | 0.12 | - | 0.21 | 0.13 | |
| ^{₩ℓ} Ee | I | 641 | 656 | 0.46 | 0.48 | -0 12 | -0.23 | | |
| | 2 | 1536 | I46 9 | - | 0.11 | - | 0.19 | 0.12 | |

with our calculation). However, in a number of cases we obtain the probabilities of E3 transitions $0^+_{g.s.} \rightarrow 3^-_1$ much smaller than experimental values, but these data are known with large errors and are not very reliable. For 1^{42} Nd, , e.g., in paper $^{/19/}$ the value B(E3, $0^+_{g.s.} \rightarrow 3^-_1) = 0.24 \ e^2 b^3$ is given. Note also should be made that the probabilities of these transitions calculated in paper $^{/13/}$ appear to be even smaller by one order than our values.

The quasiparticle-phonon interaction influences the structure of 3⁻ states not less than that of 2⁺ states. The component $Q_{21}^+Q_{31}^+$ is large in the wave function of 3_1^- level. Even in the isotones N=82 it amounts to 10% and in other nuclei its value reaches 20-30%. This results in a significant magnitude of $Q_2(3_1^-)$ which experimental measurement would be of interest. To the structure of 3_2^- states the main contribution comes from the noncollective phonons Q_{32}^+ and Q_{33}^+ . The change of single-particle schemes does not practically affect the properties of 3⁻ states, therefore the correspondong results are omitted here.

Thus, we could see that the interaction of collective and two-quasiparticle excitations is considerable in the nuclei we have discussed. It complicates the state structure even at excitation energies 1.5-2.0 MeV. Insertion of the noncollective components into the wave function has made it possible to improve the description of energies and electromagnetic characteristics of the 2^+ levels. The above improvement was sufficient not all the time. This is partly due to the inexact knowledge on the singleparticle level scheme; in other cases the more complicated wave function must be used. No doubt, the problem remains open concerning the role of residual forces of another type, e.g., of quadrupole interaction in the particle-particle channel $\frac{1}{20}$. To analyze the noncollective components the study seems to be necessary of those processes which are more directly connected with the differential structure of states, e.g., of β -decay.

The authors express their deep gratitude to V.G.Soloviev for valuable advices and remarks, to R.V.Jolos for fruitful discussions.

References

- V.G.Soloviev. Nucl.Structure, Dubna Symp., 1968, р. 101. IAEA, Vienna, 1968.
 2.А.И.Вдовин, Ч.Стоянов. Изв. АН СССР, сер.физ.,
- 37, 1750 /1973/.
- З. А.И. Вдовен, Г.Кырчев, Ч.Стоянов. ОИЯИ, Р4-7374, Дубна, 1973.
- 4. В.Е.Митрошин. Тезисы XXIII совещания по ядерной спектроскопии и структуре атомного ядра. Тбилиси, 1973. H.Reinhard and F.Dönau. XIII совещание по ядерной

спектроскопни и теории ядра, Д6-7094, Дубна, 1973.

5. Г.Алага. Структура ядра. ОИЯИ. Д-6465. Дубна. 1972.

G.Alaga, V.Paar and V.Lopac Phys.Lett., 43B, 459 (1972).

- 6. N.Meyer-Levy, V.Lopac, Preprint LYCEN 7315, March 1973.
- 7. Е.Б.Бальбуцев, Р.В.Джолос. ЯФ, 7, 788 /1968/. Р.В.Джолос. ОИЯИ, 4-3757. Дубна, 1968.
- 8. S.R.Almonev and J.G.Borse, Nucl. Phys., A171, 660 (1971).
- 9. В.Г.Соловьев. "Теория сложных ядер", М., "Наука", 1971.
- 10. В.А.Чепурнов. ЯФ, 6, 955 /1967/. K.Takeuchi, P.A.Moldauer. Phys.Lett., 28B, 384 (1969). 11. Н.Ю.Ширикова. Сообщение ОИЯИ, Р5-3712, Дубна,
- 1968.
- 12. Л.А.Малов, В.Г.Соловьев, И.Д.Христов. ЯФ, 6, 1186 /1967/. А.И.Вдовин, А.Л.Комов, Л.А.Малов. Сообщение ОИЯИ, Р4-5125, Дубна, 1970.
- 13. M.Waroquier, K.Heyde. Nucl. Phys., A164, 113 (1971).
- 14. M.Sakai. Nuclear Data Tables, 10, 511 (1972). A.Christy, O.Häusser. Nucl.Data Tables, 11, 281 (1972).
- 15. C.W.Towsley, R.Cook, D.Cline and R.N.Horoshko. Proc. Int. Conf. of Nuclear Moments and Nucleus Structure, Osaka (Japan) 1972 v. 3.
- 16. J.R.Kerns and J.X.Saladin. Phys.Rev., C6, 1016 (1972).
- 17. P.A.Crowley, J.R.Kerns, J.X.Saladin, Phys.Rev. C3, 2049 (1971).
- 18. O.Hansen and O.Nathan. Nucl. Phys., 42, 197 (1963).
- 19. D.W.Madsen, L.S.Cardman, J.R.Legg and C.K.Bockelman. Nucl. Phys., A168, 97 (1971).

 B.L.Birbrair, K.I.Erokhina, I.Kh.Lembegr. Nucl.Phys., A145, 129 (1970).
 B.L.Birbrair. Phys.Lett., 32B, 165 (1970).
 H.Toki and M.Sano. Preprint OULNS 73-6, Osaka University. Laboratory of Nuclear Studies, 1973.

> Recived by Publishing Department on March 18, 1974.