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THE PREDICTION OF THE BEHAVIOUR OF A-HYPERON ELECTROMAGNETIC FORM FACTORS

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1. Introduction

The strange Λ -hyperon is a charge-neutral particle which according to the SU(3) symmetry classification belongs to the same octuplet like nucleons, Σ - and Ξ - hyperons. Its anomalous magnetic moment is nonzero and takes the value

$$\mu_{\Lambda} = -0.613 \pm 0.004 \ [\mu_{\rm sr}] \tag{1}$$

in the nuclear magneton units $\mu_{_{\rm N}}.$ Consequently the A- particle can in principle interact with electrons in elastic scattering experiments. However, oving to the fact that it decays in 2.631x10⁻¹⁰sec. (mainly into a nucleon and a pion) one cannot practically provide the A- hyperon target for experiments of that type and there are no data on the cross section of the process $e^{\Lambda} \rightarrow e^{\Lambda}$ till now, from which one could extract the information on the electromagnetic (e.m.) structure of A in the space-like region. Similarly to nucleons, the latter is completely described by two independent scalar functions of the photon momentum transfer squared t < 0, which can be chosen in the form of the Dirac $F_1^{\Lambda}(t)$ and Pauli $\mathbf{F}_{n}^{\Lambda}(t)$ form factors (ff's) or of the more practical electric $\bar{G}_{E}^{\Lambda}(t)$ and magnetic $G_{M}^{\Lambda}(t)$ ones. The only difference from nucleons is that owing to the zero value of isospin of the A-hyperon there is no splitting of the Dirac and Pauli ff's into the combinations of isoscalar and isovector parts, but $F_{4}^{\Lambda}(t)$ and $F_{2}^{\Lambda}(t)$ are just identified with the corresponding isoscalar ff's.

The e.m. structure of Λ in the time-like region can be measured for $t > 4 m_{\Lambda}^2$ in the annihilation process $e^+e^- \rightarrow \Lambda \Lambda$. The differential and total cross sections of the latter, expressed through the electric and magnetic ff's, are

 $\frac{\mathrm{d} \sigma^{\mathrm{c.m.}}}{\mathrm{d} \Omega} \stackrel{(\mathrm{e^+e^-} \to \Lambda\bar{\Lambda})}{(\mathrm{e^+e^-} \to \Lambda\bar{\Lambda})} = \frac{\alpha^2}{4\mathrm{t}} \beta \left[\frac{4\mathrm{m}^2_{\Lambda}}{\mathrm{t}} |G_{\mathrm{E}}^{\Lambda}|^2 \mathrm{sin}^2\vartheta + |G_{\mathrm{M}}^{\Lambda}|^2 (1 + \mathrm{cos}^2\vartheta) \right] (2)$

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and

$$\sigma(e^+e^- \rightarrow \Lambda \overline{\Lambda}) = -\frac{4\pi\alpha^2}{3t}\beta \left[\frac{2m_A^2}{t} |G_E^{\Lambda}|^2 + |G_M^{\Lambda}|^2\right]$$
(3)

respectively, where t is the total c.m. energy squared, β and m_{Λ} are the velocity and mass of a preduced lambda or antilambda hyperon and ϑ is the angle of $\Lambda(\bar{\Lambda})$ relative to $e^+(e^-)$ beam.

It is not easy task to identify the produced neutral lambda-antilambda pairs among other particles created in the final state of the electron-positron annihilation process. Nevertheless, all technical problems connected with the latter have been overcome recently and just one experimental point on the $e^+e^- \rightarrow \Lambda \overline{\Lambda}$ cross section

 $\sigma(e^+e^- \rightarrow \Lambda \bar{\Lambda}) = 0.100 \pm \frac{0.060}{0.035}$ [nb] at t = 5.693 GeV² (4)

has been obtained [1] by the DM2 group at ORSAY for the first time. It exceeds a theoretically predicted [2] value of the cross section, assuming the t-dependence of the constraint-free ff's to arise from the coupling of many vector mesons in the form of a product of poles.

In this paper we do not try to predict the value (4) theoretically. We, however, employ it as a scale to determine a true behaviour of the predicted $e^+e^- \rightarrow \Lambda \overline{\Lambda}$ cross section and then from the latter to reproduce the electric and magnetic ff's both in the time-like and in the space-like region.

In the next section we construct the modified VMD model of the e.m. structure of the Λ -hyperon with correct analytic properties and the asymptotic behaviour predicted by the quark model for baryon ff's. Section 3 is devoted, first, to the evolution of the resonance couplings to Λ from known couplings to nucleons by utilizing the SU(3) symmetry and the normalization conditions for Dirac and Pauli ff's, and then to the prediction of the Λ -hyperon electric and magnetic ff's behaviour. Here also the electric and magnetic mean square radii of the Λ -particle are evaluated numerically. Conclusions and summary are given in section 4. 2. A modified VMD model for the electromagnetic structure of Λ -hyperon.

The electric and magnetic ff's of the Λ -hyperon in (2) and (3) are defined through Dirac $F_1^{\Lambda}(t)$ and Pauli $F_2^{\Lambda}(t)$ ff's, obtained [3] by the most general decomposition of the matrix element of the Λ -hyperon e.m. current into a maximal number of linearly independent covariants constructed from momenta and spin parameters, by means of the ralations

$$G_{\mathbf{E}}^{\Lambda}(t) = F_{1}^{\Lambda}(t) + \frac{t}{4m_{\Lambda}^{2}} F_{2}^{\Lambda}(t)$$

$$G_{\mathbf{M}}^{\Lambda}(t) = F_{1}^{\Lambda}(t) + F_{2}^{\Lambda}(t) .$$
(5)

Both sets of ff's are normalized as follows

$$G_{\rm E}^{\Lambda}(0) = F_1^{\Lambda}(0) = 0$$

 $G_{\rm M}^{\Lambda}(0) = F_2^{\Lambda}(0) = \mu_{\Lambda}$ (6)

(7)

Since, as a consequence of the zero value of the A-hyperon isospin, contributing is only the isoscalar part $F_1^{\Lambda}(t)$ and $F_2^{\Lambda}(t)$, according to the idea of the standard VMD model [4], each $F_{1,2}^{\Lambda}(t)$ in (5) is expressed in the form



where the summation is carried out just through the well established isoscalar vector mesons. The J/Ψ and $\Psi'(3685)$ have

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not been included as they are rather narrow resonances and they are found to be far above the $\Lambda\bar{\Lambda}$ threshold. The subindex zero in the ff's $F_{1,2}^{\Lambda}(t)_0$ means the zero width of the considered vector meson resonances. The ratios of the coupling constants in (7) are constrained by the equations

$$\sum_{s=\omega,\phi,\phi'} (\mathbf{f}_{s\Lambda\bar{\Lambda}}^{(1)} / \mathbf{f}_{s}) = 0$$

$$\sum_{s=\omega,\phi,\phi'} (\mathbf{f}_{s\Lambda\bar{\Lambda}}^{(2)} / \mathbf{f}_{s}) = \mu_{\Lambda}$$

(8)

following from the normalization conditions (6).

The unitarization of the VMD model (7) is carried out by incorporation of the two-cut-approximation of the analytic structure of Dirac and Pauli A-hyperon ff's. This structure is generated by two branch points, t_0 and t_{in} , which correspond to the lowest normal or anomalous [5] threshold and to an effective threshold (to be left as a free parameter of the constructed model) simulating the contributions of other virtual processes, respectively.

For the pure isoscalar ff's $F_1^{\Lambda}(t)$ and $F_2^{\Lambda}(t)$ the lowest normal threshold is at $t = 9m_{\pi}^2$, where the m_{π} is the pion mass. However, there is a triangle Feynman diagram of the e.m. vertex of the Λ -hyperon presented in Fig.1a, which could in principle generate the anomalous threshold below $9m_{\pi}^2$ and therefore one has to determine its position explicitly.



From the dual diagram [6] given in Fig. 1b one finds

$$t_a = 4 m_K^2 - \left[1 - \left(\frac{m_A^2 - (m_P^2 + m_K^2)}{2 m_P m_K}\right)^2\right]$$
 (9)

or numerically

$$t_a = 48.889 m_{\pi}^2$$
 (10)

The latter value reveals that the lowest anomalous threshold of the Λ -hyperon ff is above the lowest normal threshold at $9m_{\pi}^2$. As a result, the first branch point t_0 of $F_1^{\Lambda}(t)$, and $F_2^{\Lambda}(t)$ is then incorporated into Eqs.(7) by the transformation

$$z = t_{0} - \frac{4 \left[t_{in} - t_{0}\right]}{\left[\frac{1}{W} - W\right]^{2}}$$
(11)

that is transparent from the inverse transformation

$$W(t) = 1 \frac{\left[\left[\frac{t}{t_0} - 1 \right]^{1/2} + \left[\frac{t}{t_0} - 1 \right]^{1/2} \right]^{1/2} - \left[\left[\frac{t}{t_0} - 1 \right]^{1/2} + \left[\frac{t}{t_0} - 1 \right]^{1/2} \right]^{1/2}}{\left[\left[\frac{t}{t_0} - 1 \right]^{1/2} + \left[\frac{t}{t_0} - 1 \right]^{1/2} \right]^{1/2} + \left[\left[\frac{t}{t_0} - 1 \right]^{1/2} + \left[\frac{t}{t_0} - 1 \right]^{1/2} \right]^{1/2}} \right]^{1/2}$$

which maps the whole t-plane into the left-half of the unit disc. For more details of this transformation see ref.[7].

If we, further, denote the zero-width VMD poles, corresponding to the considered resonances ω, ϕ, ϕ', in the W-plane by W_{so} and the normalization point t=0 by W_N, one can write for the mass squared of resonances the relation

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$$h_{\rm S}^2 = t_0 - \frac{4 \left(t_{\rm In} - t_0 \right)}{\left(1/w_{\rm S0} - w_{\rm S0} \right)^2}$$
(13)

and also the identity

$$0 = t_0 - \frac{4 (t_{1n} - t_0)}{(1/W_N - W_N)^2}$$
(14)

Now, substituting the transformation (11), together with (13) and (14) into (7) one gets

$$F_{1}^{\Lambda}(t)_{0} = \left(\frac{1-w^{2}}{1-w_{N}^{2}}\right)_{g}^{2} \frac{(w_{N}-w_{g0})(w_{N}+w_{g0})(w_{N}+w_{g0})(w_{N}+1/w_{g0})(w_{N}+1/w_{g0})}{(w-w_{g0})(w-1/w_{g0})(w+1/w_{g0})} \left[f_{g\Lambda\bar{\Lambda}}^{(1)}f_{g}\right]$$
(15a)

$$\mathbb{P}_{2}^{\Lambda}(t)_{0} = \left(\frac{1-w^{2}}{1-w_{N}^{2}}\right)_{s}^{2} \frac{(W_{N}-W_{s0})(W_{N}+W_{s0})(W_{N}-1/W_{s0})(W_{N}+1/W_{s0})}{(W-W_{s0})(W-1/W_{s0})(W+1/W_{s0})} \left(\int_{s\Lambda\Lambda}^{(2)} f_{s\Lambda\Lambda}^{(2)} f_{s}\right).$$
(15b)

To exhibit the reality of (15a,b) on the real axis for $t < t_0$ explicitly, we arrange them by using properties of VMD pole positions w_{g0} in the w plane, following directly from (12). Let us suppose, e.g., that

then
$$\begin{array}{c} t_0 < m_{\omega}^2 < t_{1n} & \text{and} & m_{\varphi}^2 , m_{\varphi}^2 > t_{1n} & (16) \\ w_{\omega_0} = -w_{\omega_0}^* & \text{and} & w_{s_0} = (w_{s_0}^*)^{-1}, s = \phi, \phi' & (17) \end{array}$$

respectively. As a result, eqs.(15a, b) take the form

$$\mathbf{F}_{1}^{\Lambda}(t)_{0} = \left[\frac{1 - \mathbf{w}^{2}}{1 - \mathbf{w}_{N}^{2}}\right]^{2} \left[\frac{(\mathbf{w}_{N} - \mathbf{w}_{\omega 0})(\mathbf{w}_{N} - \mathbf{w}_{\omega 0}^{*})(\mathbf{w}_{N} - \frac{1}{\mathbf{w}_{\omega 0}})(\mathbf{w}_{N} -$$

$$+\sum_{\mathbf{s}=\Phi,\Phi'}\frac{(\mathbf{W}_{N}-\mathbf{W}_{so})(\mathbf{W}_{N}-\mathbf{W}_{so}^{*})(\mathbf{W}_{N}+\mathbf{W}_{so})(\mathbf{W}_{N}+\mathbf{W}_{so})}{(\mathbf{W}-\mathbf{W}_{so})(\mathbf{W}-\mathbf{W}_{so}^{*})(\mathbf{W}+\mathbf{W}_{so})(\mathbf{W}+\mathbf{W}_{so})}\left[\mathbf{f}_{s\Lambda\Lambda}^{(1)}/\mathbf{f}_{s}\right]$$
(18a)

>

$$\mathbb{P}_{2}^{\Lambda}(t)_{0} = \left(\frac{1-w^{2}}{1-w_{N}^{2}}\right)^{2} \left[\frac{(w_{N}-w_{\omega0})(w_{N}-w_{\omega0})(w_{N}-1/w_{\omega0})(w_{N}-1/w_{\omega0})(w_{N}-1/w_{\omega0})}{(w-w_{\omega0})(w-w_{\omega0})(w-w_{\omega0})(w-1/w_{\omega0})(w-1/w_{\omega0})} \left[f_{\omega\Lambda\bar{\Lambda}}^{(2)}f_{\omega}\right] + \frac{(w_{N}-w_{\omega0})(w_{N}-w_{\omega0})(w_{N}-1/w_{\omega0})(w_{N}-1/w_{\omega0})}{(w-w_{\omega0})(w-w_{\omega0})(w-w_{\omega0})(w-1/w_{\omega0})(w-1/w_{\omega0})}\right]$$

$$+ \sum_{\mathbf{s}=\phi,\phi'} \frac{(\mathbf{w}_{N} - \mathbf{w}_{so})(\mathbf{w}_{N} - \mathbf{w}_{so}^{*})(\mathbf{w}_{N} + \mathbf{w}_{so})(\mathbf{w}_{N} + \mathbf{w}_{so})}{(\mathbf{w} - \mathbf{w}_{so})(\mathbf{w} - \mathbf{w}_{so}^{*})(\mathbf{w} + \mathbf{w}_{so})(\mathbf{w} + \mathbf{w}_{so}^{*})} \left[\mathbf{f}_{s\Lambda\bar{\Lambda}}^{(2)} \mathbf{f}_{s} \right]$$
(18b)

from which the reality for $t < t_0$, where w(t) is real, is already transparent. We note, however, that the inequalities (16) should not be true ones and their precise form will be only known upon determining the value of $t_{\rm in}$ numerically in the next section.

In expressions (15a,b), as well in (18a,b), the vector mesons are still considered to be (see subindex zero in the corresponding ff's) stable particles. However, by introducing nonzero values of widths $\Gamma_g \neq 0$ ($s=\omega, \phi, \phi'$) they can be defined as complex poles $t_g=(m_g-1\Gamma_g/2)$ on unphysical sheets of the four-sheeted Riemann surface in conformity with all required qualities of the constructed unitarized VMD model. The latter is ensured in (18a,b) by a simple change

 $W_{so} \rightarrow W_{s}$ (19)

which, leads to the shift of poles from the real axis to the complex region of the corresponding unphysical sheets.

Now we would like to draw attention to the factorization property of the used transformation (11), which makes possible to accomodate the asymptotic behaviour of the Λ -hyperon e.m. ft's in conformity with the quark model prediction for baryons. Really, the transformation (11) splits the resultant expressions (18a,b) (see also (15a,b)) into a product of two factors. The first one

 $\left[\begin{array}{c} \frac{1-w^2}{1-w_N^2} \end{array}\right]^2$

(20)

determing the asymptotic behaviour of the VMD model (7), does not depend on the type of a contributing vector meson to the Λ -hyperon e.m. ff's and so it is the same for all considered vector mesons. The second factor consists of a sum of pole terms and describes the nontrivial behaviour of ff's in the resonance region. Since for $t \to \pm \infty$ it approaches a real constant, it does not contribute to the asyptotic behaviour of ff's.

The particular form $\simeq t^{-1}$ of the asymptotic behaviour of the zero-width VMD model is in the factor (20)

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ensured by the power "2" above the round brackets. So, the change of the latter to any other even positive number leads to the change of the power asymptotic behaviour of considered e.m. ff's, however, without a violation of any quality of the constructed unitarized VMD model.

In conformity with the quark model prediction [8] for baryon ff's the power "2" in (18a) will be changed to the power "4" and in (18b) to the power "6". Taking into account these changes of the powers in (18a, b) and introducing nonzero values of vector meson widths by the replacement (19) one gets the modified VMD model

$$F_{1}^{\Lambda}(t) = \left[\frac{1-w^{2}}{1-w^{2}_{N}}\right]^{4} \frac{(w_{N}-w_{\omega})(w_{N}-w_{\omega}^{*})(w_{N}-1/w_{\omega})(w_{N}-1/w_{\omega})}{(w-w_{\omega})(w-w_{\omega}^{*})(w-1/w_{\omega})(w-1/w_{\omega}^{*})} \left[f_{\omega\Lambda\bar{\Lambda}}^{(1)}/f_{\omega}\right] + \\ + \sum_{s=\Phi,\Phi'} \frac{(w_{N}-w_{s})(w_{N}-w_{s}^{*})(w_{N}-w_{s}^{*})(w_{N}+w_{s})(w_{N}+w_{s}^{*})}{(w-w_{s}^{*})(w+w_{s}^{*})} \left[f_{s\Lambda\bar{\Lambda}}^{(1)}/f_{s}\right] \right]$$
(21a)
$$F_{2}^{\Lambda}(t) = \left[\frac{1-w^{2}}{1-w_{\Lambda}^{2}}\right]^{6} \frac{(w_{N}-w_{\omega})(w_{N}-w_{\omega}^{*})(w_{N}-w_{\omega}^{*})(w_{N}-1/w_{\omega})(w_{N}-1/w_{\omega})}{(w-w_{\omega})(w-w_{\omega}^{*})(w-1/w_{\omega})(w_{N}-1/w_{\omega})} \left[f_{\omega\Lambda\bar{\Lambda}}^{(2)}/f_{\omega}\right] +$$

 $+ \sum_{\mathbf{s}=\boldsymbol{\Phi}, \boldsymbol{\Phi}'} \frac{(\mathbf{W}_{N} - \mathbf{W}_{s})(\mathbf{W}_{N} - \mathbf{W}_{s}^{*})(\mathbf{W}_{N} + \mathbf{W}_{s})(\mathbf{W}_{N} + \mathbf{W}_{s})(\mathbf{W}_{N} + \mathbf{W}_{s}^{*})}{(\mathbf{W} - \mathbf{W}_{s})(\mathbf{W} - \mathbf{W}_{s}^{*})(\mathbf{W} + \mathbf{W}_{s})(\mathbf{W} + \mathbf{W}_{s}^{*})} \left[\mathbf{f}_{s\Lambda\Lambda}^{(2)} \mathbf{f}_{s} \right] \right]$ (21b)

for the A-hyperon e.m. ff's with correct analytic properties the asymptotic behaviour predestined by the quark model for baryons. The latter is utilized for a prediction of the $G_{\rm E}^{\Lambda}(t)$ and $G_{\rm M}^{\Lambda}(t)$ ff's behaviour both in the time-like and in the space-like region. However, it is a subject of the next section.

3. The behaviour of the electric and magnetic form factors of the $\Lambda\text{-hyperon.}$

The model for a calculation of $G_E^{\Lambda}(t)$ and $G_M^{\Lambda}(t)$ is obtained by substituting (21a,b) into the relations (5). It depends on the following 13 physical parameters t_{in} , m_s , Γ_s , $f_{s\Lambda\Lambda}^{(1)}/f_s$, $f_{s\Lambda\Lambda}^{(2)}/f_s$ (s= ω, ϕ, ϕ'), which are reduced to 11 linearly independent parameters by the constraints (8) on the coupling ratios following from the normalization conditions (6). As can be seen from subsequent, it is extremely useful to express just $f_{\phi'\Lambda\Lambda}^{(1)}/f_{\phi}$, and $f_{\phi'\Lambda\Lambda}^{(2)}/f_{\phi}$, through other coupling ratios by the relations (8) as follows

$$f_{\phi,\Lambda\bar{\Lambda}}^{(1)}/f_{\phi} = -f_{\omega\Lambda\bar{\Lambda}}^{(1)}/f_{\omega} - f_{\phi\Lambda\bar{\Lambda}}^{(1)}/f_{\phi}$$

$$f_{\phi,\Lambda\bar{\Lambda}}^{(2)}/f_{\phi} = \mu_{\Lambda} - f_{\omega\Lambda\bar{\Lambda}}^{(2)}/f_{\omega} - f_{\phi\Lambda\bar{\Lambda}}^{(2)}/f_{\phi} .$$
(22)

Then one can predict the behaviour of $G_{\rm E}^{\Lambda}(t)$ and $G_{\rm N}^{\Lambda}(t)$ as soon as 11 remaining parameters are known numerically.

The masses and the widths of all three resonances are taken from the Review of Particle Properties [9].

The resonance couplings $f_{S\Lambda\bar{\Lambda}}$ (s= ω, ϕ) to the A-hyperon are estimated from the resonance couplings to nucleons, determined in a new nucleon ff analysis [10] by an improved model in comparison with the model presented in [7], utilizing the SU(3) symmetry.

Really, from the SU(3) invariant Lagrangian for the vector-meson-baryon-antibaryon vertex

$$L_{\nabla B\overline{B}} = \frac{1}{\nu^{2}} f_{F} \left[B_{\beta}^{\alpha} \gamma_{\mu} B_{\gamma}^{\beta} - B_{\gamma}^{\beta} \gamma_{\mu} B_{\beta}^{\alpha} \right] \left[V_{\mu} \right]_{\alpha}^{\gamma} + \frac{1}{\nu^{2}} f_{D} \left[B_{\gamma}^{\beta} \gamma_{\mu} B_{\beta}^{\alpha} + B_{\beta}^{\alpha} \gamma_{\mu} B_{\gamma}^{\beta} \right] \left[V_{\mu} \right]_{\alpha}^{\gamma} +$$
(23)

 $\frac{1}{\nu^2}$ is $B^{\alpha}_{\beta}\gamma_{\mu}B^{\beta}_{\alpha}\omega^{0}_{\mu}$

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with a consideration of the ideal
$$\omega - \phi$$
 mixing $\phi^0 = \phi_8 \cos \vartheta - \omega_1 \sin \vartheta$

$$\omega^0 = \phi_{\rm A} \sin \theta + \omega_{\rm A} \cos \theta$$

where B,B and V are [11] baryon, antibaryon and vector-meson octuplet matrices, ω_{μ}^{0} is the omega-meson singlet, $f_{\rm F}$, $f_{\rm D}$ and $f_{\rm S}$ are the corresponding coupling constants and $\vartheta \cong 35.3^{\circ}$ is the mixing angle, one can obtain (besides other relations) the following expressions for couplings of ρ -, ω -, ϕ - mesons to nucleons

$$f_{\rho N \overline{N}} = \frac{1}{2} (f_{p} + f_{p})$$

$$f_{\omega N \overline{N}} = \frac{1}{2} \cos \theta f_{s} - \frac{2}{2\sqrt{3}} \sin \theta (3f_{p} - f_{p}) \qquad (24)$$

$$\mathbf{f}_{\phi N \overline{N}} = \frac{1}{\sqrt{2}} \sin \theta \mathbf{f}_{s} + \frac{1}{2\sqrt{3}} \cos \theta (3\mathbf{f}_{F} - \mathbf{f}_{D})$$

and to the Λ -hyperon

$$f_{\omega\Lambda\bar{\Lambda}} = \frac{1}{2} \cos\theta f_{s} + \sqrt{\frac{2}{3}} \sin\theta f_{p}$$

$$f_{\bar{\omega}\Lambda\bar{\Lambda}} = \frac{1}{6} \sin\theta f_{s} - \sqrt{\frac{2}{2}} \cos\theta f_{p}$$
(25)

Now, calculating the values of the universal vector-meson coupling constants

$$f_{\rho} = 4.987$$

 $f_{\omega} = 16.268$ (26)
 $f_{\phi} = 13.178$

by the relation

$$\frac{f_{V_{-}}^{2}}{4\pi} = \frac{\alpha^{2}}{3} \frac{m_{V_{-}}}{\Gamma(V \to e^{+}e^{-})}, \qquad (27)$$

where $\Gamma(V - e^+e^-)$ is taken from the Review of Particle Properties [9], one finds from the results on the nucleon ff analysis [10] the couplings to nucleons as follows

$$f_{\rho N \bar{N}}^{(1)} = 1.875 \qquad f_{\rho N \bar{N}}^{(2)} = 6.361$$

$$f_{\omega N \bar{N}}^{(1)} = 6.803 \qquad f_{\omega N \bar{N}}^{(2)} = -7.155 \qquad (28)$$

$$f_{\phi N \bar{N}}^{(1)} = 2.254 \qquad f_{\phi N \bar{N}}^{(2)} = 12.797 .$$

Substituting the latter values into (24), by means of the solution of the corresponding three linear algebraic equations according to f_s , f_p and f_F , the numerical values

1 _s ⁽¹⁾ = 8.291	$f_{\rm S}^{(2)} = 7.657$		
$f_{D}^{(1)} = 4.016$	$f_{\rm D}^{(2)} = -0.717$	12. –	(29)
$f_{\rm F}^{(1)} = -0.266$	$f_{\rm F}^{(2)} = 13.439$		

are found, which (together with the value of the mixing angle $\vartheta \cong 35.3^\circ$) through the relations (25) give

$$f_{\omega\Lambda\bar{\Lambda}}^{(1)} = 6.680 \qquad f_{\omega\Lambda\bar{\Lambda}}^{(2)} = 4.081 \qquad (30)$$

$$f_{\phi\Lambda\bar{\Lambda}}^{(1)} = 0.712 \qquad f_{\phi\Lambda\bar{\Lambda}}^{(2)} = 3.607 .$$

Dividing the values in (30) by the corresponding universal vector-meson coupling constants (26), finally the coupling ratios of the modified VMD model for Λ -hyperon e.m. ff's are obtained

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$$f_{\omega\Lambda\bar{\Lambda}}^{(1)}/f_{\omega} = 0.411 \qquad f_{\omega\Lambda\bar{\Lambda}}^{(2)}/f_{\omega} = 0.251$$

$$f_{\phi\Lambda\bar{\Lambda}}^{(1)}/f_{\phi} = 0.054 \qquad f_{\phi\Lambda\bar{\Lambda}}^{(2)}/f_{\phi} = 0.274 . \qquad (31)$$

The values of $f_{\varphi'}^{(1)} \Lambda \overline{\Lambda} / f_{\varphi'}$ and $f_{\varphi'}^{(2)} \Lambda \overline{\Lambda} / f_{\varphi'}$, calculated by the relations (22) and the values (31) are as follows

 $f_{\phi'\Lambda\bar{\Lambda}}^{(1)}/f_{\phi'} = -0.465$ $f_{\phi'\Lambda\bar{\Lambda}}^{(2)}/f_{\phi'} = -1.138$. (32)

In this manner, finally, we are left only with one unknown parameter, t_{in} , of the modified VMD model for a description of the e.m.structure of the Λ -hyperon. This effective threshold, common for both, Dirac and Pauli ff's, is determined from the fit of the existing [1] ORSAY DM2 experimental point on the $e^+e^- \rightarrow \Lambda\Lambda$ cross section at $t = 5.693 \text{ GeV}^2$. As a result, the following optimal value

 $t_{1m} = 1.462 \pm 0.020 \text{ GeV}^2$

(33)

(34)

is found. The corresponding behaviour of the total cross section (3) with (33) and the values of other parameters of the model given by (31) and (32) is presented in Fig.2.

The predicted behaviour of the electric $G_E^{\Lambda}(t)$ and the magnetic $G_M^{\Lambda}(t)$ Λ -hyperon ff's both in the space-like and in the time-like region are presented in Figs.3a, b and Figs.4a, b, respectively.

The electric and magnetic mean square radii defined by the relations

$$\langle \mathbf{r}_{\mathbf{E}}^{2} \rangle_{\Lambda} = 6 \frac{d G_{\mathbf{E}}^{\Lambda}(t)}{d t} \Big|_{t=0}$$

$$\langle \mathbf{r}_{\mathbf{M}}^{2} \rangle_{\Lambda} = 6 \frac{d G_{\mathbf{M}}^{\Lambda}(t)}{d t} \Big|_{t=0}$$



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are found to be

 $\langle r_{\rm E}^2 \rangle_{\Lambda} = 0.021 \ {\rm F}^2 \ {\rm and} \qquad \langle r_{\rm M}^2 \rangle_{\Lambda} = -0.135 \ {\rm F}^2.$ (35)

So, unlike the neutron, the charge neutral A-hyperon has the positive electric mean square radius, though in the magnetic mean square radius both particles are coinciding in sign.

4. Conclusions and summary

The unitarized analytic VMD model with correct analytic properties and the asymptotic behaviour compatible with the quark model predictions, which has been shown to be successful in a description of the pion [12], kaon [13] and nucleon [7,10] e.m. ff's, is in this paper applied to the prediction of the behaviour of electric and magnetic Λ -hyperon ff's.

The crucial point of the procedure is a determination of the numerical values of the free parameters t_{in} , m_s , Γ_s , $f_{s\Lambda\Lambda}^{(1)}/f_s$, $f_{s\Lambda\Lambda}^{(2)}/f_s$ of the model, however, with a clear physical meaning. There are three independent sources used to determine these parameters. First, the masses and widths of all considered resonances are fixed at the world averaged values. given by [9]. Second, the resonance couplings to the A-hyperon are evaluated from the known [10] couplings to nucleons by utilizing the SU(3) symmetry and normalization conditions for Dirac and Pauli ff's. Third, the optimal value of the effective inelastic threshold is determined from the fit of the only existing ORSAY DM2 experimental point on the $e^+e^- \rightarrow \Lambda \overline{\Lambda}$ cross section. So, the existing ORSAY DM2 point was used as a scale to reach a true behaviour of $\sigma(e^+e^- \rightarrow \Lambda \overline{\Lambda})$ up to t=10 GeV² (see Fig.2), which seems to be interesting in connection with the FENICE experiment at Frascati, where simultaneously with neutron ff's the experimental measurement of A-hyperon e.m. ff's is expected to be realized too.

In conclusion we would like to note that a simplified

assumption was introduced that the effective inelastic threshold of the Dirac ff is required in our model to be equal to the value of the effective inelastic threshold of the Pauli ff. Though it was shown in the nucleon ff's case to be almost true [10], there is no deeper reason for them to be equal. However, without this simplification of the model and also without the neglect of the J/ψ and $\psi'(3685)$ particle contributions at present any realistic prediction could not be possible for the A-hyperon e.m. ff's behaviour.

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