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**SUPERSTRING Z'-BOSON  
AT UNK ENERGIES**

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## INTRODUCTION

Investigations of superstrings<sup>/1/</sup> are expected to lead to a unified theory of all fundamental interactions. From the point of view of physical consequences one now prefers the model of the 10-dimensional heterotic superstring with the gauge group  $E_8 \times E_8$ <sup>/2/</sup>. One of the most advanced schemes of compactification onto the Calabi-Yau manifold at energies below the Planck masses  $M_p \sim 10^{19}$  GeV yields an effective 4-dimensional  $N = 1$  supersymmetrical theory with the gauge group  $E_6$ <sup>/3/</sup>. A large number of new exotic fermions and an extra  $Z'$ -boson of mass below 1 TeV are predicted. It is still not clear whether the exotic fermions can be light enough<sup>/4,5/</sup>. So the experiments in the search for the  $Z'$ -boson at accelerators of the new generation (SSC, LHC, UNK) seem better substantiated, though one considers the possibility of observing exotic  $E_6$  fermions.

The following simple arguments<sup>/5/</sup> for existence of this particle in the  $E_6$ -model are in place here. Let us consider the maximal subgroup

$$E_6 \supset SU_{3C} \times SU_{3L} \times SU_{3R}. \quad (1)$$

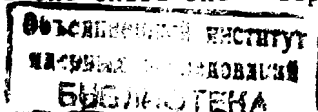
assuming such an imbedding of the standard group  $SU_{3C} \times SU_{2L} \times SU_{1Y}$  that  $SU_{2L} \subset SU_{3L}$ .

In the superstring-inspired  $E_6$ -model the breaking of the gauge group at the compactification scale  $M_c$  ( $M_c \leq M_p \sim 10^{19}$  GeV) is due to the flux breaking mechanism<sup>/3/</sup>. This mechanism has the same effect as the Higgs mechanism with the Higgs fields in the adjoint representation of the group  $E_6$ , i.e. in its 78-plet. Remember that each generation of fermions is part of the fundamental 27-dimensional representation. For the above maximal subgroup (1) there is a decomposition

$$78 = (8, 1, 1) + (1, 8, 1) + (1, 1, 8) + (3^*, 3, 3) + (3, 3^*, 3^*) \quad (2)$$

$$27 = (3^*, 1, 3^*) + (3, 3, 1) + (1, 3^*, 3). \quad (3)$$

The first set of parentheses in (3) contains antiquarks, the second one - quarks, and the third one - leptons.



The Higgs fields preserving  $SU_{3C}$  can be present in  $(1,8,1) + (1,1,8)$ . It is known that if the group  $SU_3$  is broken by the Higgs fields from its octet representation, the subgroup  $SU_2$  can remain only with the  $U_1$ -factor. Thus,  $SU_{3L}$  can be broken to  $SU_{2L} \times U_{1L}$ . The charge  $Y_L$  corresponding to  $U_{1L}$  cannot be identified with the weak hypercharge  $Y$ . It follows from the relation

$$Q^{em} = I_{3L} + Y/2$$

and decomposition of the 27-plet (3) that in this case  $SU_{3L}$ -singlet antiquarks would not carry the electric charge  $Q^{em}$  and the leptons would have a fractional charge. Consequently, one of the preserved quantities corresponding to  $SU_{3R}$  must make a contribution to the weak hypercharge  $Y$ . In other words, at least one subgroup  $U_{1R} \subset SU_{3R}$  must survive the breaking. So a group appears in the superstring-inspired  $E_6$ -model, it is wider than the standard one at least by one  $U_1$ -factor

$$E_6 \rightarrow SU_{3C} \times SU_{2L} \times U_{1Y} \times U_1' \quad (4)$$

This is just the indication of existence of an additional  $Z'$ -boson associated with  $U_1'$ .

In a general case the  $E_6$ -symmetry may be broken in superstring models only to the rank 5 and rank 6 subgroups depending on the topology of the compact manifold<sup>/3/</sup>. Other possibilities are regarded as non-realistic<sup>/6/</sup>.

Below we shall consider a model with an intermediate gauge group of rank 5, since its predictions are more definite.

Note that there can be direct and indirect experimental manifestations of the  $Z'$ -boson. Produced in high-energy collisions,  $Z'$  can be directly observed in colliding beams of SSC ( $\sqrt{S} = 40$  TeV), LHC ( $\sqrt{S} = 16.5$  TeV), UNK ( $\sqrt{S} = 6$  TeV). The study of indirect manifestations of the  $Z'$ -boson has good prospects in fixed target experiments at UNK ( $\sqrt{S} = 75$  GeV). In some cases these manifestations are practically independent of the energy and the possibility of observing them is determined by the accuracy of measurements. According to tentative estimations<sup>/7/</sup>, the necessary statistics can be provided by the planned neutrino experiments at UNK<sup>/8/</sup>. Higher neutrino beam energies, as compared with the present level, result in larger statistics owing to the linear growth of total cross sections for neutrino interactions ( $\sigma \sim \sigma_0 E_\nu$ ).

In this paper we study the contribution of the  $Z'$ -boson to neutral currents taking into account the  $Z^0$ - $Z'$  mixing. We have found quantities composed of deep inelastic  $\nu(\bar{\nu})N$  scatter-

ring cross sections which are most sensitive to the  $Z'$  contribution. These quantities analysed, we discuss some possibilities of indirect observation of this particle in neutrino experiments at UNK.

## 1. MASS MATRIX AND $Z'$ INTERACTIONS WITH FERMIONS

Properties of the  $Z'$ -boson can be considered on the same basis within the models with the intermediate group of both the 5th and 6th rank:

$$SU_{3C} \times SU_{2L} \times U_{1Y} \times U_1' \quad \text{rank} = 5, \quad (5)$$

$$SU_{3C} \times SU_{2L} \times U_{1Y} \times U_{1X} \times U_{1\psi} \quad \text{rank} = 6. \quad (6)$$

Imbedding in  $E_6$  is determined by a sequence of subgroups:

$$E_6 \supset SO_{10} \times U_{1\psi} \supset SU_5 \times U_{1X} \times U_{1\psi}, \quad (7)$$

when

$$SU_5 \supset SU_{3C} \times SU_{2L} \times U_{1Y}. \quad (8)$$

Generators of  $U_1'$  have the form

$$Q' = \sqrt{\frac{3}{8}} Q_X - \sqrt{\frac{5}{8}} Q_\psi \quad (9)$$

$Q_X$  and  $Q_\psi$  are the generators of  $U_{1X}$  and  $U_{1\psi}$ .  $Q'$  is associated with the  $Z'$ -boson in the model with the group of rank 5.

In the version with the group of rank 6 there is also one light boson. This is the additional  $Z(\theta)$ -boson coupled with the superposition of the generators:

$$\bar{Q}(\theta_{E_6}) = Q_\psi \cos \theta_{E_6} + Q_X \sin \theta_{E_6}. \quad (10)$$

Values of the charges  $Q_X, Q_\psi, Q'$  for the fields from the  $E_6$  27-plet are listed in the Table. The angle  $\theta_{E_6}$  parametrises the  $E_6$ -symmetry breaking scheme. Evidently, (9) is a particular case of (10) at  $\theta_{E_6} = 142.24^\circ$ , i.e.  $Q' = \bar{Q}(142.24^\circ)$ . It is this case that we shall consider. The narrowing of the parametric arbitrariness allows more specific estimations of the contribution of the  $Z'$ -boson.

The initial Lagrangian of interactions with neutral currents has the form:

Table. Quantum numbers of the  $E_6$  27-plet

$SO_{10}$	$SU_5$	left-handed field	$Su_{3C} I_{3L}$	$Q^{em}$	$2\sqrt{15} \cdot Q'$	$2\sqrt{10} \cdot Q_X$	$\sqrt{24} \cdot Q_\psi$	
16	5*	$d^c$	3*	0	1/3	1	3	1
		$e^-$	1	-1/2	-1	1	3	1
		$\nu_e$	1	1/2	0	1	3	1
	10	$e^{-c}$	1	0	1	-2	-1	1
		$d$	3	-1/2	-1/3	-2	-1	1
		$u$	3	1/2	2/3	-2	-1	1
10	$u^c$	3*	0	-2/3	-2	-1	1	
	$N^c$	1	0	0	-5	-5	1	
	$h^c$	3*	0	1/3	1	-2	-2	
5	$E^-$	1	-1/2	-1	1	-2	-2	
	$\nu_E$	1	1/2	0	1	-2	-2	
	$h$	3	0	-1/3	4	2	-2	
	$E^{-c}$	1	1/2	1	4	2	-2	
1	1	$N_E^c$	1	-1/2	0	4	2	-2
		$n$	1	0	0	-5	0	4

$$-\mathcal{L}_{NC} = e A^\mu J_\mu^{em} + g Z^\mu J_\mu^Z + g' Z'^\mu J_\mu^{Z'} \quad (11)$$

Here  $J_\mu^{em}$  is the usual electromagnetic current,  $J_\mu^Z$  and  $J_\mu^{Z'}$  are the currents interacting with Z- and Z'-bosons, respectively,

$$J_\mu^Z = \sum_i \bar{\psi}_i \gamma_\mu (I_{3L} - Q^{em} x_W) \psi_i \equiv \sum_i Q_i \bar{\psi}_i \gamma_\mu \psi_i \quad (12)$$

$$J_\mu^{Z'} = \sum_i Q_i' \bar{\psi}_i \gamma_\mu \psi_i, \quad (13)$$

where  $x_W = \sin^2 \theta_W$ .

Let us specify the coupling constants  $g$  and  $g'$  by the formulae<sup>9/</sup>:

$$g = \frac{e}{\sqrt{x_W(1-x_W)}}, \quad g' = \sqrt{\frac{5}{3}} \frac{e}{\sqrt{1-x_W}}. \quad (14)$$

Then the normalization of the charge  $Q'$  chosen ensures equality of these constants at the scale of unification of  $M_C$  into the  $E_6$  group. Ignoring a slight difference in the renormalisation-group evolution of  $g$  and  $g'$ , we shall use expressions (14) for energies  $\sim M_W$  as well.

In a general case the mass matrix in the basis of  $Z^0 - Z'$  is non-diagonal:

$$M^2 = \begin{pmatrix} M_{Z_0}^2 & \delta M^2 \\ \delta M^2 & M_{Z'}^2 \end{pmatrix} \quad (15)$$

It leads to the mixing of the  $Z'$ -boson with the standard  $Z_0$ -boson. Diagonalisation of matrix (15) results in the states  $Z_{1,2}$  with a definite mass:

$$\begin{pmatrix} Z_1 \\ Z_2 \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} Z_0 \\ Z' \end{pmatrix} \quad (16)$$

The masses and the mixing angle are expressed through the initial parameters:

$$M_1^2 = M_{Z_0}^2 - \frac{(\delta M^2)^2}{M_{Z'}^2 - M_{Z_0}^2}, \quad M_2^2 = M_{Z'}^2 + \frac{(\delta M^2)^2}{M_{Z'}^2 - M_{Z_0}^2} \quad (17)$$

$$\tan^2 \theta = (M_{Z_0}^2 - M_1^2) / (M_2^2 - M_{Z_0}^2). \quad (18)$$

In the models with  $SU_{2L}$ -doublet and singlet Higgs fields the following relation occurs:

$$M_{Z_0}^2 = \frac{M_W^2}{1-x_W}, \quad (19)$$

i.e. for  $x_W = 0.229 \pm 0.05$  we have  $M_{Z_0} = 92.1 \pm 0.7$  GeV. In the superstring-inspired  $E_6$ -model with the intermediate gauge

group of rank 5 there are two doublet ( $H, \bar{H}$ ) and one singlet ( $N$ ) Higgs fields. In this case

$$\delta M^2 = \sqrt{x_W} \frac{4v^2 - \bar{v}^2}{3(v^2 + \bar{v}^2)},$$

$$M_{Z'}^2 = M_{Z_0}^2 \frac{16v^2 + \bar{v}^2 + 25x^2}{9(v^2 + \bar{v}^2)}, \quad (20)$$

where  $\langle H^0 \rangle \equiv \langle \bar{N}_E^c \rangle = v$ ,  $\langle \bar{H}^0 \rangle \equiv \langle \bar{\nu}_E \rangle = \bar{v}$ ,  $\langle N \rangle \equiv \langle \bar{n} \rangle = x$ . This structure of the Higgs sector leads to a restriction for the mixing angle<sup>10/</sup>:

$$-\frac{8}{3} \frac{\sqrt{x_W}}{(M_{Z'}^2/M_{Z_0}^2 - 1)} < \tan 2\theta < \frac{2}{3} \frac{\sqrt{x_W}}{(M_{Z'}^2/M_{Z_0}^2 - 1)}. \quad (21)$$

In the popular "no-scale" version of the model<sup>11/</sup>  $\theta > 0$ . With allowance for mixing, the Lagrangian (11) has the form:

$$\begin{aligned} -\mathcal{L}_{NC} = & eA^\mu J_\mu^{em} + gZ_1^\mu (J_\mu^Z \cos\theta + \frac{g'}{g} J_\mu^{Z'} \sin\theta) \\ & + g'Z_2^\mu (J_\mu^{Z'} \cos\theta - \frac{g}{g'} J_\mu^Z \sin\theta). \end{aligned} \quad (22)$$

Hence we obtain the low-energy effective Lagrangian of  $\nu N$ -neutral current interactions<sup>12/</sup>

$$\mathcal{L}_{NC}^{eff} = \frac{G_F}{\sqrt{2}} (\bar{\nu}_L \gamma^\mu \nu_L) \sum_i \epsilon_i' \bar{f}_i \gamma_\mu f_i. \quad (23)$$

Dependence on the mixing angle  $\theta$  and the masses  $M_1$  and  $M_2$  of intermediate bosons is concentrated in chiral constants:

$$\begin{aligned} \epsilon_1' = & \frac{M_{Z_0}^2}{M_1^2} \left( \cos\theta - \frac{g'}{g} \frac{\sin\theta}{3} \right) (Q_1 \cos\theta + Q_1' \frac{g'}{g} \sin\theta) + \\ & + \frac{M_{Z_0}^2}{M_2^2} \left( \sin\theta + \frac{g'}{g} \frac{\cos\theta}{3} \right) (Q_1 \sin\theta + Q_1' \frac{g'}{g} \cos\theta), \end{aligned} \quad (24)$$

where  $Q_1$  and  $Q_1'$  are defined in (12) and (13).

In the standard model (SM) the chiral constants have a simple form

$$\epsilon_i = Q_i. \quad (25)$$

A cross section for deep inelastic scattering is the following linear combination<sup>12/</sup>

$$\sigma_{NC}^\nu = \frac{2G_F^2 ME}{\pi} \sum_i |\epsilon_i'|^2 C_i. \quad (26)$$

The coefficients  $C_i$  are determined by the hadron target structure and do not depend on the type of the intermediate boson.

## 2. DEVIATIONS FROM THE STANDARD MODEL DUE TO THE SUPERSTRING $Z'$ -BOSON

To investigate these deviations, we shall analyse the quantities of the type

$$\delta = \frac{A'(Z, Z') - A(Z)}{A(Z)}. \quad (27)$$

$A'(Z, Z')$  and  $A(Z)$  are the observable quantities calculated with and without the  $Z'$  contribution. It is important that the value of  $\delta$  weakly depends on the hadron target structure.

1. Let us consider deviations in the ratio of cross sections  $R = \sigma^{NC}/\sigma^{CC}$ .

At high energies the total cross sections for deep inelastic  $\nu(\bar{\nu})N$  scattering have the form:

$$\sigma(\nu h + \nu X) = C \{ \epsilon_L'^2(u) U_L^h + \epsilon_L'^2(d) D_L^h + \epsilon_R'^2(u) U_R^h + \epsilon_R'^2(d) D_R^h \}, \quad (28)$$

$$\sigma(\bar{\nu} h + \bar{\nu} X) = C \{ \epsilon_L'^2(u) U_R^h + \epsilon_L'^2(d) D_R^h + \epsilon_R'^2(u) U_L^h + \epsilon_R'^2(d) D_L^h \},$$

where  $C = \frac{2}{\pi} G_F^2 M E D_{\nu h}^p$ ,  $h$  is the number of nucleons in the target  $h$ ,  $D_{\nu}^p = \int dx dx_d^p(x, Q^2)$  is the total momentum of valence  $d$ -quarks in a proton;

$$U_L = \eta - \beta\eta + \beta + (1 + \omega)(\xi + \zeta),$$

$$U_R = \omega(\eta - \beta\eta + \beta) + (1 + \omega)(\xi + \zeta),$$

$$D_L = 1 - \beta + \beta\eta + 2(1 + \omega)\xi,$$

$$D_R = \omega(1 - \beta + \beta\eta) + 2(1 + \omega)\xi, \quad (29)$$

$\beta = n/h$ ,  $n$  is the number of neutrons in the target  $h$ ,  $\beta = (0, 1/2, 1)$  for proton, isoscalar, neutron,  $\eta = \int x dx u_{\nu}^p(x)/D_{\nu}^p$ , in our case  $\eta = 2$  (isotopically symmetric distribution functions),

$$\xi = \int x dx s(x)/D_{\nu}^p = 0.25^{13/}$$

$$\zeta = \int x dx c(x)/D_{\nu}^p = 0.125,$$

$\omega = 1/3$  is the kinematic factor.

The multiplicative factor  $C$  taken out of the brackets in (28) is insignificant, since it is removed when one calculates the quantity

$$\delta_{\nu, \bar{\nu}} = \frac{R'_{\nu, \bar{\nu}} - R_{\nu, \bar{\nu}}}{R_{\nu, \bar{\nu}}} = \frac{\sigma'_{\nu, \bar{\nu}} - \sigma_{\nu, \bar{\nu}}}{\sigma_{\nu, \bar{\nu}}} \quad (30)$$

Figs. 1 (2) show the dependence of  $\delta_{\nu}(\delta_{\bar{\nu}})$  on the mass of the  $Z'$ -boson  $M_2$  for different mixing angles. The curves have typical features:

a) They all intersect at the same point for  $M_1 = M_2$ . It follows from (24). There is no dependence on the mixing angle if  $M_1 = M_2$ ;

b) At zero mixing angles  $|\delta_{\nu, \bar{\nu}}|$  decreases, at non-zero ones it increases with the mass  $M_2$ . In fact, if  $\theta = 0$ ,

$$\epsilon'_i = \epsilon_i - Q_i \frac{\sin^2 Q_W}{3} \frac{M_0^2}{M_2^2} \quad (31)$$

tends to the  $\epsilon_i$  (standard model) with growing  $M_2$ . At fixed non-zero  $\theta$  the second term in (24) proportional to  $M_2^{-2}$  rapidly decreases while  $M_2$  increases, and the first term proportional to  $M_1^{-2}$  increases, since  $M_1$  decreases because of relation (18).

A disagreement between  $\epsilon'_i$  and  $\epsilon_i$  leads to considerable deviations of  $R'_{\nu, \bar{\nu}}$  from  $R_{\nu, \bar{\nu}}$ ;

c) According to (18), the value of the  $Z_0$ -boson mass  $M_1 = 91.5 \pm 1.2 \pm 1.7 \text{ GeV}^{14}$  known from the experiment imposes a constraint

$$M_2^2 \lesssim \frac{M_W^2}{(1 - x_W) \sin^2 \theta} - \cot^2 \theta M_{\min}^2 \quad (32)$$

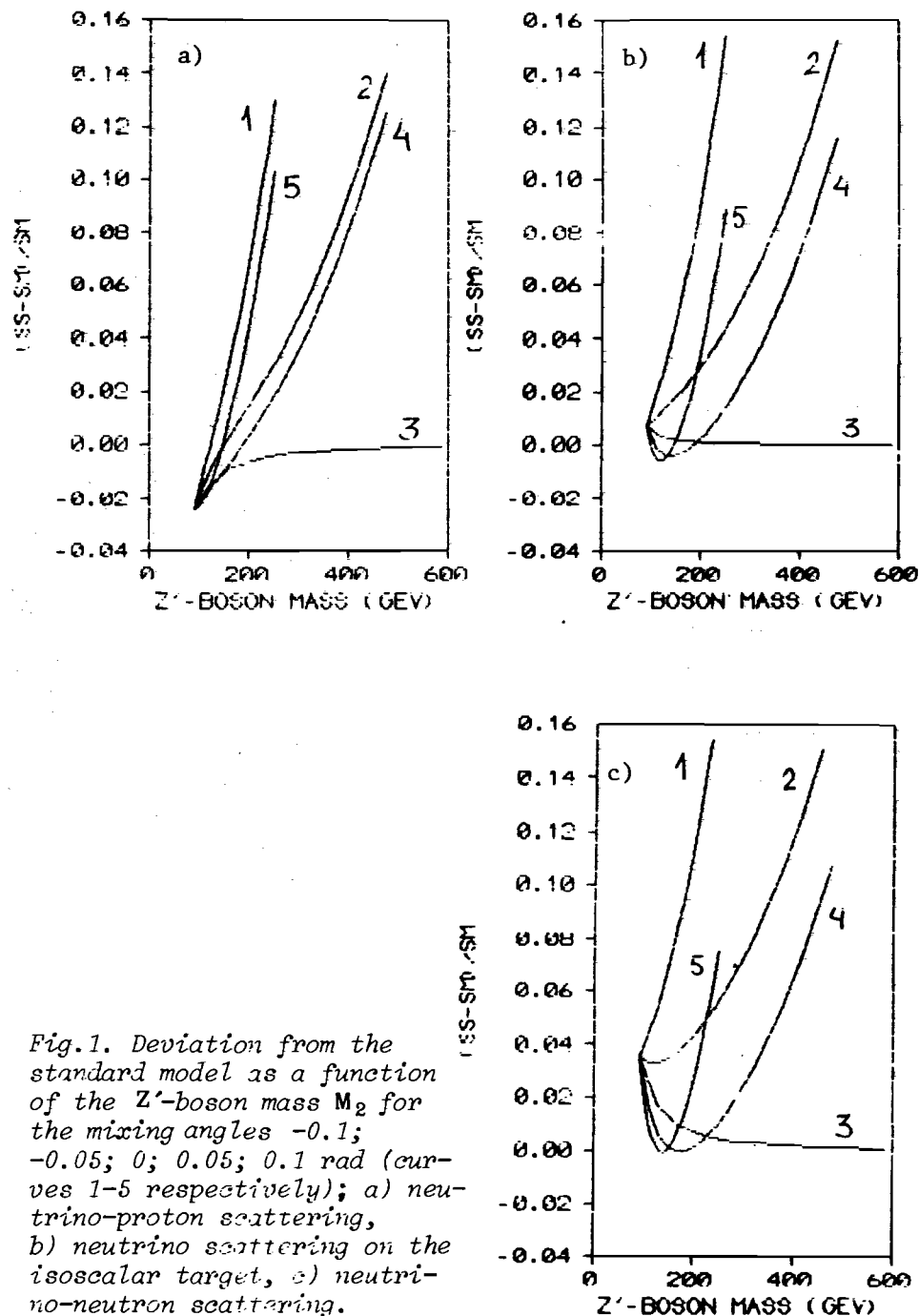


Fig. 1. Deviation from the standard model as a function of the  $Z'$ -boson mass  $M_2$  for the mixing angles  $-0.1$ ;  $-0.05$ ;  $0$ ;  $0.05$ ;  $0.1$  rad (curves 1-5 respectively); a) neutrino-proton scattering, b) neutrino scattering on the isoscalar target, c) neutrino-neutron scattering.

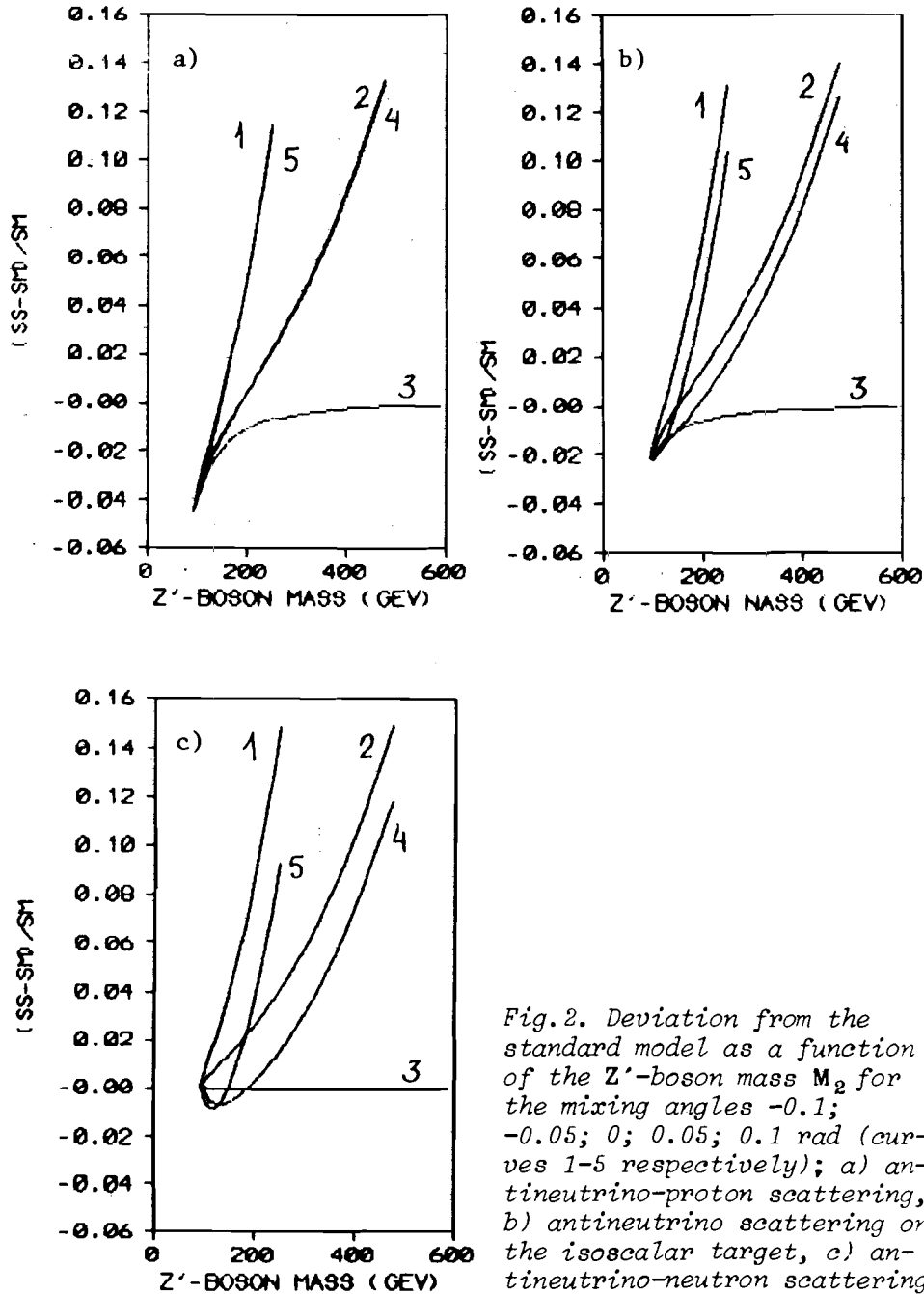


Fig.2. Deviation from the standard model as a function of the  $Z'$ -boson mass  $M_2$  for the mixing angles  $-0.1$ ;  $-0.05$ ;  $0$ ;  $0.05$ ;  $0.1$  rad (curves 1-5 respectively); a) antineutrino-proton scattering, b) antineutrino scattering on the isoscalar target, c) antineutrino-neutron scattering.

where  $M_{\min} \cong 90$  GeV. Therefore at increasing  $|\theta|$  the curves are cut off at smaller  $M_2$ . Besides, very large values of  $|\delta_{\nu, \bar{\nu}}|$  ( $\delta_{\nu, \bar{\nu}} \geq 10\%$ ) are excluded owing to the experimental accuracy achieved.

The present region of allowable mixing angles and masses of the additional  $Z'$ -boson ( $\theta$  and  $M_2$ ) is shown in Figs.3 (4) by contour 1' 15'. Curves 2 and 3 show the narrowing of this region when  $R_{\nu}(R_{\bar{\nu}})$  is measured on the isoscalar target with an accuracy 1% and 0.5%. It is the accuracy that one plans to achieve in neutrino experiments at the UNK.

As is seen, the same accuracy of measurements in the anti-neutrino beam will probably allow more rigid constraints on the region of  $M_2$  and  $\theta$ .

2. Let us consider deviations from SM in the Paschos-Wolfenstein relation

$$r^h = \frac{\sigma(\nu h \rightarrow \nu X) - \sigma(\bar{\nu} h \rightarrow \bar{\nu} X)}{\sigma(\nu h \rightarrow \mu X) - \sigma(\bar{\nu} h \rightarrow \mu X)} \quad (33)$$

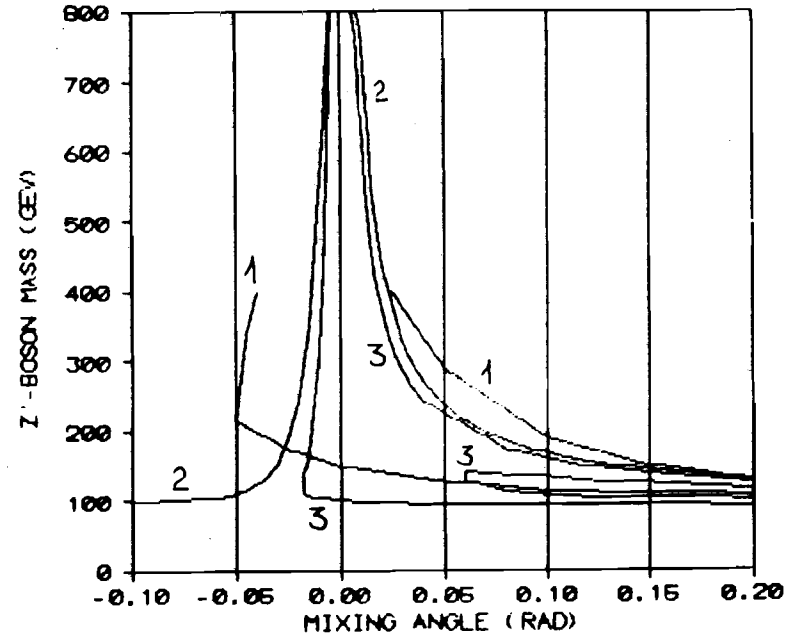


Fig.3. Constraints on the mixing angle  $\theta$  and the mass  $M_2$  of the  $Z'$ -boson from neutral currents. 1 - contour from Ref. 15'; 2, 3 - contours corresponding to the measurement of  $R_{\nu}$  on the isoscalar target with an accuracy 1%, 0.5%.

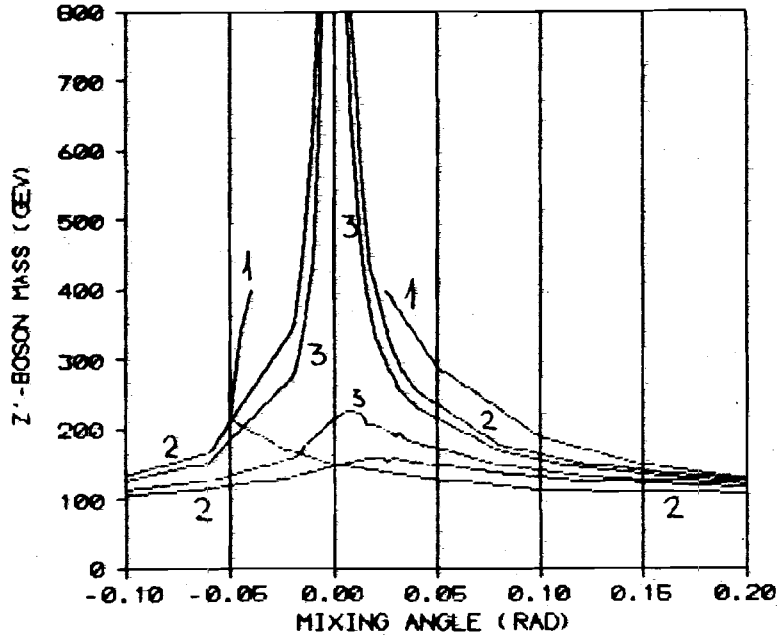


Fig. 4. Constraints on the mixing angle  $\theta$  and the  $Z'$ -boson mass  $M_2$  from neutral currents. 1 - contour from Ref. /15/; 2-3 - contours corresponding to the measurement of  $R_p$  on the isoscalar target with an accuracy 1%, 0.5%.

In the usual parton model there is a relation

$$r^h = \frac{C}{\sigma_{CC}^{\nu} - \sigma_{CC}^{\bar{\nu}}} \{ [\epsilon_L'^2(u) - \epsilon_L'^2(d)] U^h + [\epsilon_R'^2(u) - \epsilon_R'^2(d)] D^h \}, \quad (34)$$

where

$$U^h = (1 - \omega)(\eta - \beta\eta + \beta),$$

$$D^h = (1 - \omega)(1 - \beta + \beta\eta)$$

and other quantities are defined earlier.

Deviation from SM

$$\delta^h = \frac{r'^h - r^h}{r^h}$$

is plotted in Fig.5 as a function of the  $Z'$ -boson mass for different mixing angles and targets.

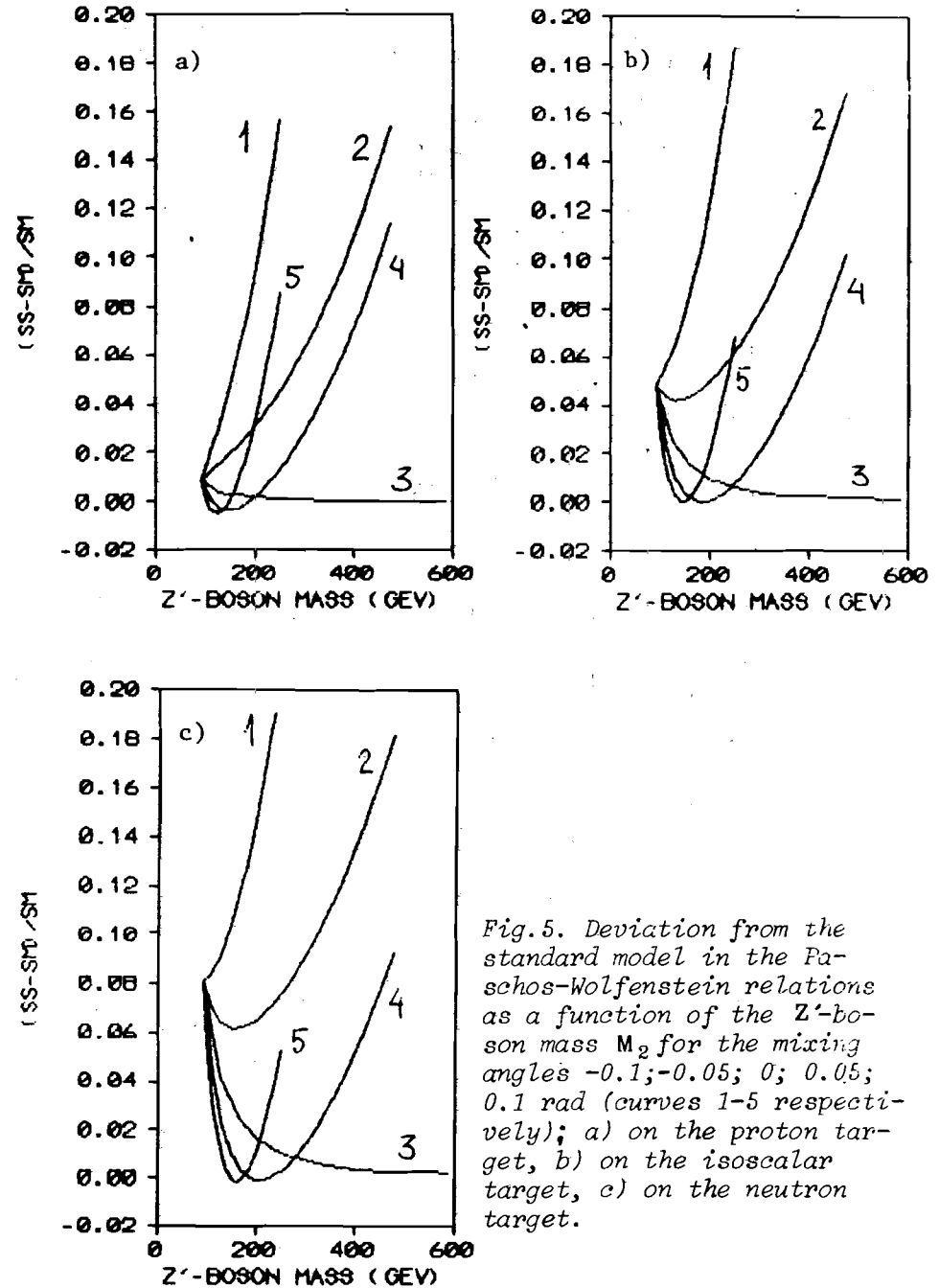


Fig. 5. Deviation from the standard model in the Paschos-Wolfenstein relations as a function of the  $Z'$ -boson mass  $M_2$  for the mixing angles  $-0.1; -0.05; 0; 0.05; 0.1$  rad (curves 1-5 respectively); a) on the proton target, b) on the isoscalar target, c) on the neutron target.



Peculiarities in the behaviour of the curves (coincidences at  $M_1 = M_2$ , increase with  $M_2$  at non-zero  $\theta$  and decrease at  $\theta = 0$ , cut off graphs when  $M_2$  and  $\theta$  increase) have the same reasons as in the case of  $R_{\nu, \bar{\nu}}$ .

The accuracy achieved in measurements of  $r^h$  is not high (about 10-20%); only the region of large negative mixing angles is excluded. More details can be found in Fig.6. Besides contour 1, one can see curves 2 and 3 corresponding to the measurement of  $r$  on the isoscalar target with an accuracy 3% and 1.5%.

The measurement of  $r$  on the isoscalar target with the above accuracy will evidently allow one to exclude almost the whole of the region of negative mixing angles  $\theta \leq -0.02$ .

3. Let us consider deviations from SM in the ratios of cross sections

$$R_{\nu}^{n/p} = \frac{\sigma(\nu n \rightarrow \nu X)}{\sigma(\nu p \rightarrow \nu X)}, \quad R_{\bar{\nu}}^{n/p} = \frac{\sigma(\bar{\nu} n \rightarrow \bar{\nu} X)}{\sigma(\bar{\nu} p \rightarrow \bar{\nu} X)} \quad (35)$$

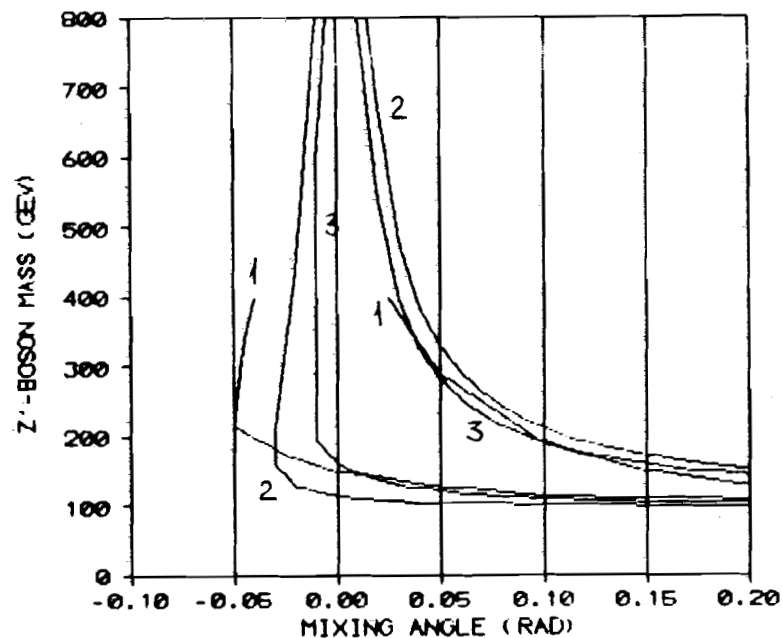


Fig.6. Constraints on the mixing angle  $\theta$  and the  $Z'$ -boson mass  $M_2$  from the analysis of the Paschos-Wolfenstein relation. 1 - contour from Ref. '15', 2,3 - contours corresponding to measurements of  $r$  on the isoscalar target with an accuracy 3%, 0.5%.

The quantity we are interested in

$$\delta_{\nu, \bar{\nu}} = \frac{R_{\nu, \bar{\nu}}^{n/p} - R_{\nu, \bar{\nu}}^{n/p}}{R_{\nu, \bar{\nu}}^{n/p}}$$

is calculated by means of formulae (28)-(29) for the proton and the neutron.

Figs.7 and 8 show the dependence of  $\delta_{\nu}$ ,  $\delta_{\bar{\nu}}$  on the  $Z'$ -boson mass for different mixing angles. The curves do not go beyond the presently achieved experimental accuracy in determination of  $R_{\nu, \bar{\nu}}^{n/p}$  (about 10%). At all  $\theta$  they decrease as  $M_2$  increases, at positive  $\theta$  they increase in absolute values.

In figs.9 and 10 the curves corresponding to measurement of  $R_{\nu, \bar{\nu}}^{n/p}$  with an accuracy 3% and 1.5% are numbered 2 and 3.

Thus, measurement of  $R_{\nu, \bar{\nu}}^{n/p}$  with an accuracy 3% does not impose more constraints on the region of allowable values of the parameters.

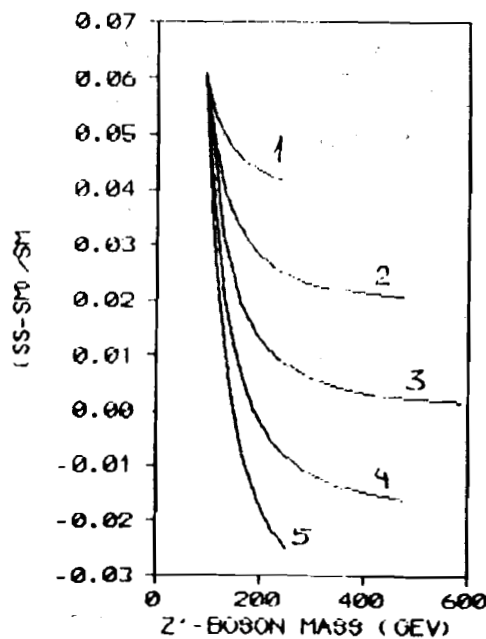


Fig.7. Deviation from the standard model in  $R_{\nu}^{n/p}$  as a function of the  $Z'$ -boson mass  $M_2$  for mixing angles  $-0.1$ ;  $-0.05$ ;  $0$ ;  $0.05$ ;  $0.1$  rad (curves 1-5 respectively).

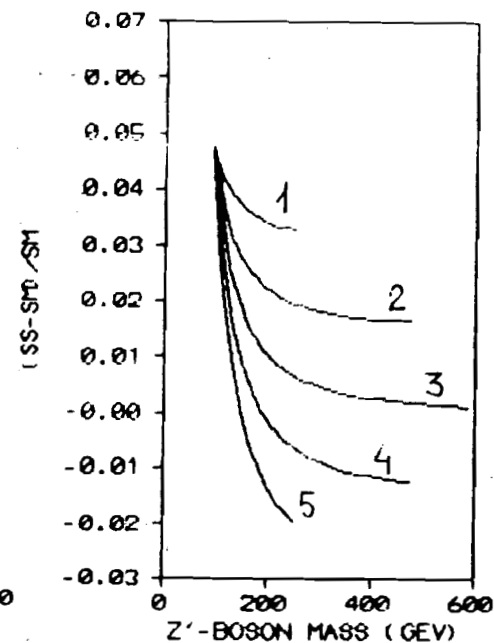


Fig.8. Deviation from the standard model in  $R_{\bar{\nu}}^{n/p}$  as a function of the  $Z'$ -boson mass  $M_2$  for mixing angles  $-0.1$ ;  $-0.05$ ;  $0$ ;  $0.05$ ;  $0.1$  rad (curves 1-5 respectively).

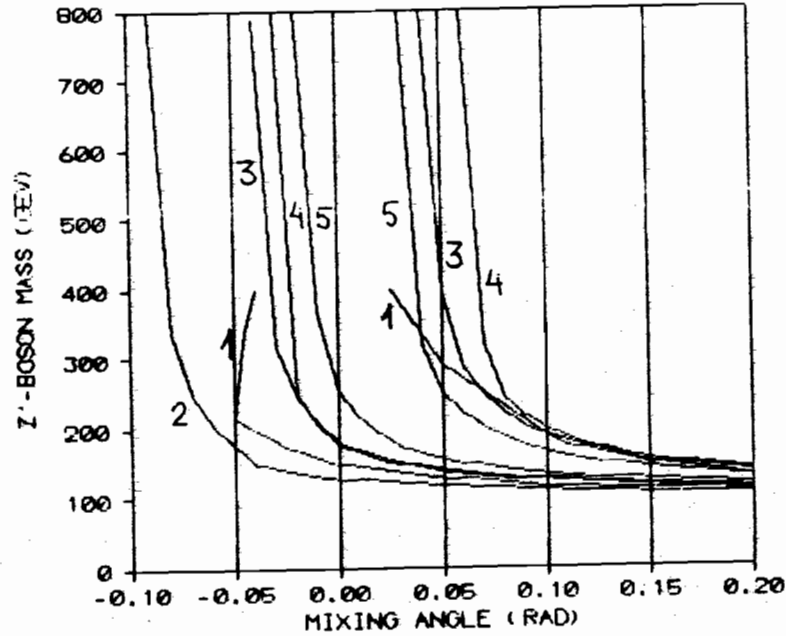


Fig.9. Constraints on the mixing angle  $\theta$  and the  $Z'$ -boson mass  $M_2$  from measurements of  $R_V^{n/p}$  and  $\Delta_V$ , 1 - contour from Ref. <sup>15/</sup> 2,3 - contours corresponding to the measurement of  $R_V^{n/p}$  with an accuracy 3% and 1.5%, 4,5 - contours corresponding to the measurement of  $\Delta_V$  with an accuracy 20% and 10%.

#### 4. The relative differences

$$\Delta_V = \frac{\sigma(\nu n \rightarrow \nu X) - \sigma(\nu p \rightarrow \nu X)}{\sigma(\bar{\nu} n \rightarrow \mu X) - \sigma(\bar{\nu} p \rightarrow \mu X)},$$

$$\Delta_{\bar{\nu}} = \frac{\sigma(\bar{\nu} n \rightarrow \bar{\nu} X) - \sigma(\bar{\nu} p \rightarrow \bar{\nu} X)}{\sigma(\bar{\nu} n \rightarrow \mu X) - \sigma(\bar{\nu} p \rightarrow \mu X)} \quad (36)$$

are of great interest for the search for deviations from SM because of the additional  $Z'$ -boson.

In the parton model we have

$$\Delta_V = \epsilon_L'^2(u) - \epsilon_L'^2(d) + \omega [\epsilon_R'^2(u) - \epsilon_R'^2(d)], \quad (37)$$

$$\Delta_{\bar{\nu}} = \epsilon_R'^2(u) - \epsilon_R'^2(d) + \omega [\epsilon_L'^2(u) - \epsilon_L'^2(d)].$$

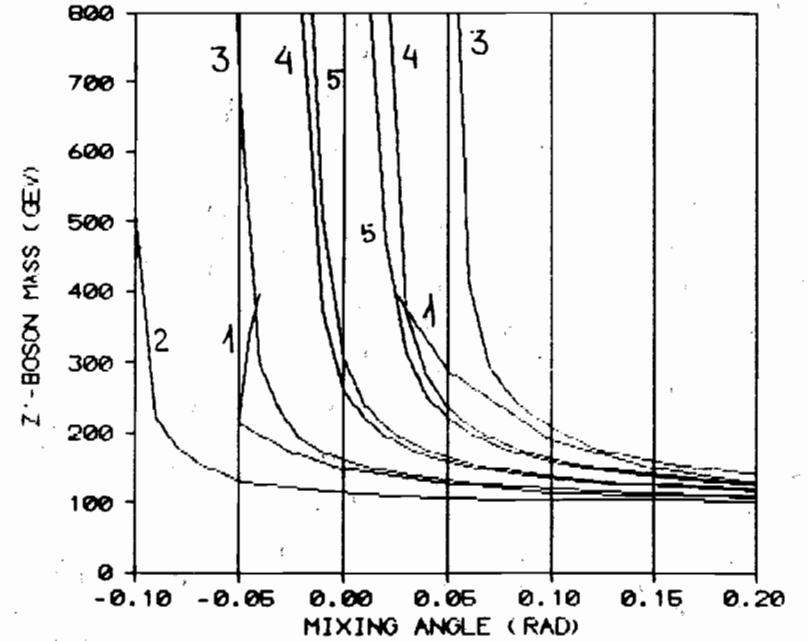


Fig.10. Constraints on the mixing angle  $\theta$  and the  $Z'$ -boson mass  $M_2$  from measurements of  $R_V^{n/p}$  and  $\Delta_{\bar{\nu}}$ , 1 - contour from Ref. <sup>15/</sup> 2,3 - contours corresponding to the measurement of  $R_V^{n/p}$  with an accuracy 3%, 1.5%, 4,5 - contours corresponding to the measurement of  $\Delta_{\bar{\nu}}$  with an accuracy 80%, 60%.

We shall calculate a relative deviation from SM by the formula

$$\delta_{\nu, \bar{\nu}} = \frac{\Delta_{\nu, \bar{\nu}}' - \Delta_{\nu, \bar{\nu}}}{\Delta_{\nu, \bar{\nu}}}.$$

Figs.11 and 12 show the dependence of  $\delta_{\nu, \bar{\nu}}$  on  $M_2$  at different mixing angles. Deviations from SM are large: up to 80% for  $\Delta_V$  and 600% for  $\Delta_{\bar{\nu}}$  at the experimentally achieved accuracies 80% for  $\Delta_V$  and 400% for  $\Delta_{\bar{\nu}}$  <sup>16/</sup>.

This large relative error of  $\Delta_{\bar{\nu}}$  is simply explained by the fact that  $\Delta_{\bar{\nu}}$  is close to zero in SM:

$$\Delta_{\bar{\nu}} = 1 - 4 \sin^2 \theta_W$$

(e.g.  $\Delta_V \approx 0$  at  $\sin^2 \theta_W = 0.22 \pm 0.05$ ).

In other words, a 600% error means that the contribution of the  $Z'$ -boson to  $\Delta_{\bar{\nu}}$  is 7 times larger than that of the conventional  $Z$ -boson. So to study  $\Delta_{\bar{\nu}}$  virtually means to study a practically pure contribution of the  $Z'$ -boson.

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Бедняков В.А., Коваленко С.Г.  
Суперструнный  $Z'$ -бозон при энергиях  
УНК

E2-88-157

В работе изучен вклад  $Z'$ -бозона в нейтральные токи. Учтено  $Z$ - $Z'$  смешивание. Найдены такие величины, составленные из сечений глубокоэластического /анти/ нейтрино-нуклонного рассеяния, которые наиболее чувствительны к вкладу  $Z'$ -бозона. Рассматривается возможность косвенного наблюдения этой экзотической частицы в нейтринных экспериментах на УНК.

Работа выполнена в Лаборатории ядерных проблем ОИЯИ.

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Bednyakov V.A., Kovalenko S.G.  
Superstring  $Z'$ -Boson at UNK Energies

E2-88-157

The contribution of the extra  $Z'$ -boson to neutral currents has been studied.  $Z$ - $Z'$  mixing has been taken into account. The quantities most sensitive to the  $Z'$ -boson contribution are found; they are composed of cross sections for deep inelastic (anti) neutrino-nucleon scattering. Possibility of indirectly observing this exotic particle in UNK neutrino experiments is considered.

The investigation has been performed at the Laboratory of Nuclear Problems, JINR.

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