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ДУБНА**

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**Yu. A. Kulchitsky<sup>1</sup>, I. V. Lutsenko<sup>2</sup>, G. S. Pogosyan<sup>2</sup>,  
A. N. Sissakian, V. M. Ter-Antonyan<sup>2</sup>**

**TABLES AND GRAPHS  
OF OSCILLATOR SPHEROIDAL FUNCTIONS**

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<sup>1</sup> Institute of Physics of the Byelorussian  
Academy of Sciences, Minsk  
<sup>2</sup> Yerevan State University

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## 1. Introduction

In ref. /1/ the problem has been studied of an isotropic quantum oscillator in prolate and oblate spheroidal coordinates and a new class of special functions has been introduced, the class of prolate and oblate spheroidal functions of the oscillator. These functions are related to spheroidal and Coulomb spheroidal functions which have found application in radiophysics, optics and quantum mechanics <sup>x)</sup>. Unlike the classical special functions the oscillator spheroidal functions do not obey recurrence formulae and have no integral representations. This "anomaly" can be explained by a specific feature of the spheroidal coordinate system <sup>/2/</sup>: there cannot be made expansions of the group of motion of a three-dimensional space into one-parameter subgroups. This peculiarity much complicates the study and application of spheroidal functions and puts forward the problem of compilation of tables and graphs of appropriate effective calculation algorithms at computer. In this paper, tables and graphs of prolate and oblate spheroidal functions of the oscillator are obtained only for several of the first values of quantum numbers of these functions. A more complete solution to this problem is still to be looked for.

## 2. Prolate angular spheroidal functions of the oscillator

Let us introduce the operator  $\hat{A}(n, m, c; \varrho)$  dependent on the variable  $\varrho \in [-1, 1]$ , quantum numbers  $n$ ,  $m$  and parameter  $c$ :

$$\hat{A}(n, m, c; \varrho) = \frac{d}{d\varrho}(\varrho^2 - 1) \frac{d}{d\varrho} + 2(n + \frac{1}{2})c\varrho^2 - \frac{m^2}{\varrho^2 - 1} - c^2\varrho^2(\varrho^2 - 1) \quad (1)$$

The quantum number  $n$  assumes only integer nonnegative values,  $|m|$  may equal  $0, 1, 2, \dots, n$ , and parameter  $c \in [0, \infty)$ . The prolate angular spheroidal functions  $Y_q(n, m, c; \varrho)$  are defined as solutions to the following Sturm-Liouville equation:

$$\hat{A}(n, m, c; \varrho) Y_q(n, m, c; \varrho) = A_q(n, m, c) Y_q(n, m, c; \varrho) \quad (2)$$

The quantum number  $q$  enumerates eigenvalues  $A_q$  and coincides with the number of zeros of the functions  $Y_q$  in the interval  $(-1, 1)$ .

<sup>x)</sup>Theory and methods of the calculation of spheroidal and Coulomb spheroidal functions and their most important applications can be found in monograph <sup>/2/</sup>.

In ref.<sup>/1/</sup> it has been shown that the functions  $Y_q$  are divided into two classes,  $Y_q^{(+)}$  and  $Y_q^{(-)}$ , with positive and negative parity in variable  $q$  and are determined by the expressions:

$$Y_q^{(+)}(n, m, c; \eta) = e^{-\frac{c\eta^2}{2}} (1+\eta^2)^{\frac{|m|}{2}} \sum_S a_{2S}(n, m, c) \eta^{2S} \quad (3)$$

$$Y_q^{(-)}(n, m, c; \eta) = e^{-\frac{c\eta^2}{2}} (1+\eta^2)^{\frac{|m|}{2}} \sum_S a_{2S+1}(n, m, c) \eta^{2S+1} \quad (4)$$

Summation in (3) and (4) runs over  $S=0, 1, \dots, \frac{n-|m|}{2}$  and  $S=0, 1, \dots, \frac{n-|m|-1}{2}$  (in the first case  $n-|m|$  is even; in the second, odd). From the meaning of the quantum number  $q$  it is clear that for  $Y_q^{(+)}$  and  $Y_q^{(-)}$   $q=0, 2, \dots, n-|m|$  and  $q=1, 3, \dots, n-|m|$ , respectively. Coefficients  $a_{2S}$  and  $a_{2S+1}$  obey trinomial recurrence formulae:

$$-(2S+1)(2S+2)a_{2S+2} + \{(2S+1)(2S+1)+4cS-A_q^{(+)}+c\}a_{2S} + 2c(n-|m|+2-2S)a_{2S-2} = 0 \quad (5)$$

$$-(2S+2)(2S+3)a_{2S+3} + \{(2S+1)(2S+1)+2c(2S+1)-A_q^{(+)}+c\}a_{2S+1} + 2c(n-|m|+1-2S)a_{2S-1} = 0 \quad (6)$$

and the boundary conditions

$$a_{-2} = a_{-1} = 0, \quad a_0 = a_1 = 1 \quad (7)$$

normalizing the function  $Y_q^{(\pm)}$ .

Therefore, the tables and graphs we are interested in are constructed by solving two systems of homogeneous equations (5) and (6) with boundary conditions (7). Results for particular cases  $0 \leq n-|m| \leq 5$  are given in Table 1 and graphs in Fig. 1.

### 3. Prolate radial spheroidal functions of the oscillator

Let us redenote the variable in operator (1) by  $\xi$  and assume the  $\xi \in [1, \infty)$ . Prolate radial spheroidal functions of

the oscillator will be defined as solutions to the Sturm-Liouville problem:

$$\hat{A}(n, m, c; \xi) X_K(n, m, c; \xi) = B_K(n, m, c) X_K(n, m, c; \xi) \quad (8)$$

The quantum number  $K$  enumerates eigenvalues  $B_K$  and coincides with the number of zeros of the function  $X_K$  in the interval  $(1, \infty)$ . According to<sup>/1/</sup> equation (8) has two classes of solutions, even and odd in the variable  $\xi$ . These solutions can be represented by polynomials:

$$X_K^{(+)}(n, m, c; \xi) = e^{-\frac{c}{2}(\xi^2-1)} (\xi^2-1)^{\frac{|m|}{2}} \sum_S b_S(n, m, c) (\xi^2-1)^S \quad (9)$$

$$X_K^{(-)}(n, m, c; \xi) = e^{-\frac{c}{2}(\xi^2-1)} (\xi^2-1)^{\frac{|m|}{2}} \xi \sum_S g_S(n, m, c) (\xi^2-1)^S \quad (10)$$

The range of summation in (9) and (10) is the same as in (3) and (4). The coefficients  $b_S$  and  $g_S$  satisfy the trinomial recurrence relations:

$$4(S+1)(S+1+m+1)b_{S+1} + \{(2S+1)(2S+1)+2c(n-|m|-2S) - B_K^{(+)}+c\}b_S + 2c(n-|m|+2-2S)b_{S-1} = 0 \quad (11)$$

$$4(S+1)(S+1+m+1)g_{S+1} + \{(2S+1)(2S+1)+2c(n-|m|-2S) - B_K^{(-)}+c\}g_S + 2c(n-|m|+1-2S)g_{S-1} = 0 \quad (12)$$

and the boundary conditions

$$b_{-1} = g_{-1} = 0, \quad b_0 = g_0 = 1 \quad (13)$$

fixing the normalization of functions  $X_K^{(\pm)}$ . Results of the solution of two systems of homogeneous equations (11) and (12) with the boundary condition (13) for  $0 \leq n-|m| \leq 5$  are collected in Tables 2 and graphs in Fig. 2.

### 4. Oblate spheroidal functions of the oscillator

We shall not here discuss these functions in detail; rather we shall note that according to ref.<sup>/1/</sup> these functions follow from analogous functions in prolate spheroidal coordinates by using the formulae

$$\tilde{Y}_+^{(\pm)}(n, m, \rho; \bar{\eta}) = (-1)^{\frac{|m|}{2}} \chi_{\frac{n-1-|m|}{2}}^{(\pm)}(n, m, -\rho; \bar{\eta}) \quad (14)$$

$$\tilde{X}_2^{(+)}(n, m, \rho; \bar{\xi}) = Y_{n-2l-1}^{(+)}(n, m, -\rho; i\bar{\xi}) \quad (15)$$

$$\tilde{X}_2^{(-)}(n, m, \rho; \bar{\xi}) = -i Y_{n-2l-1}^{(-)}(n, m, -\rho; i\bar{\xi}) \quad (16)$$

$$\bar{\eta} \in [-1, 1], \quad \bar{\xi} \in [0, \infty)$$

i.e. they represent analytic continuations of prolate spheroidal oscillator functions into an "unphysical" region of the variables  $\eta$ ,  $\xi$  and parameter  $C$ . Tables 3, 4 and graphs in Figs. 3, 4 are compiled by formulae (14)-(16).

### 5. Particular cases

The explicit form of spheroidal oscillator functions for arbitrary  $n$  and  $|m|$ , when  $0 \leq n-|m| \leq 3$ , is as follows:

$$Y_0^{(+)}(n, n, c; \eta) = \exp\left(-\frac{C\eta^2}{2}\right) (1-\eta^2)^{\frac{n}{2}}$$

$$Y_1^{(+)}(n, n-1, c; \eta) = \exp\left(-\frac{C\eta^2}{2}\right) (1-\eta^2)^{\frac{n-1}{2}} \eta$$

$$Y_0^{(+)}(n, n-2, c; \eta) = \exp\left(-\frac{C\eta^2}{2}\right) (1-\eta^2)^{\frac{n-2}{2}}$$

$$\left\{1 - \frac{(2n-1)+2c - \sqrt{(2n-1)^2 + 4c(2n-3) + 4c^2}}{2} \eta^2\right\}$$

$$Y_2^{(+)}(n, n-2, c; \eta) = \exp\left(-\frac{C\eta^2}{2}\right) (1-\eta^2)^{\frac{n-2}{2}}$$

$$\left\{1 - \frac{(2n-1)+2c + \sqrt{(2n-1)^2 + 4c(2n-3) + 4c^2}}{2} \eta^2\right\}$$

$$Y_1^{(+)}(n, n-3, c; \eta) = \exp\left\{-\frac{C\eta^2}{2}\right\} (1-\eta^2)^{\frac{n-3}{2}} \eta$$

$$\left\{1 - \frac{(2n-1)+2c - \sqrt{(2n-1)^2 + 4c(2n-7) + 4c^2}}{6} \eta^2\right\}$$

$$Y_3^{(-)}(n, n-3, c; \eta) = \exp\left(-\frac{C\eta^2}{2}\right) (1-\eta^2)^{\frac{n-3}{2}} \eta$$

$$\left\{1 - \frac{(2n-1)+2c + \sqrt{(2n-1)^2 + 4c(2n-7) + 4c^2}}{6} \eta^2\right\}$$

$$X_0^{(+)}(n, n, c; \xi) = \exp\left[-\frac{C}{2}(\xi^2-1)\right] (\xi^2-1)^{\frac{n}{2}}$$

$$X_0^{(-)}(n, n-1, c; \xi) = \exp\left[-\frac{C}{2}(\xi^2-1)\right] (\xi^2-1)^{\frac{n-1}{2}} \xi$$

$$X_0^{(+)}(n, n-2, c; \xi) = \exp\left[-\frac{C}{2}(\xi^2-1)\right] (\xi^2-1)^{\frac{n-2}{2}}$$

$$\left\{1 + \frac{(2n-1)-2c + \sqrt{(2n-1)^2 + 4c(2n-3) + 4c^2}}{4(n-1)} (\xi^2-1)\right\}$$

$$X_1^{(+)}(n, n-2, c; \xi) = \exp\left[-\frac{C}{2}(\xi^2-1)\right] (\xi^2-1)^{\frac{n-2}{2}} \xi$$

$$\left\{1 + \frac{(2n-1)-2c - \sqrt{(2n-1)^2 + 4c(2n-3) + 4c^2}}{4(n-1)} (\xi^2-1)\right\}$$

$$X_0^{(-)}(n, n-3, c; \xi) = \exp\left[-\frac{C}{2}(\xi^2-1)\right] (\xi^2-1)^{\frac{n-3}{2}} \xi$$

$$\left\{1 + \frac{(2n-1)-2c + \sqrt{(2n-1)^2 + 4c(2n-7) + 4c^2}}{4(n-2)} (\xi^2-1)\right\}$$

$$X_1^{(-)}(n, n-3, c; \xi) = \exp\left[-\frac{C}{2}(\xi^2-1)\right] (\xi^2-1)^{\frac{n-3}{2}} \xi$$

$$\left\{1 + \frac{(2n-1)-2c - \sqrt{(2n-1)^2 + 4c(2n-7) + 4c^2}}{4(n-2)} (\xi^2-1)\right\}$$

$$\tilde{Y}_0^{(+)}(n, n, \rho; \bar{\eta}) = \exp\left[-\frac{\rho}{2}(1-\bar{\eta}^2)\right](1-\bar{\eta}^2)^{\frac{n}{2}}$$

$$\tilde{Y}_1^{(-)}(n, n-1, \rho; \bar{\eta}) = \exp\left[-\frac{\rho}{2}(1-\bar{\eta}^2)\right](1-\bar{\eta}^2)^{\frac{n-1}{2}} \bar{\eta}$$

$$\tilde{Y}_0^{(+)}(n, n-2, \rho; \bar{\eta}) = \exp\left[-\frac{\rho}{2}(1-\bar{\eta}^2)\right](1-\bar{\eta}^2)^{\frac{n-2}{2}}$$

$$\left\{1 - \frac{(2n-1)+2\rho - \sqrt{(2n-1)^2 - 4\rho(2n-3) + 4\rho^2}}{4(n-1)} (1-\bar{\eta}^2)\right\}$$

$$\tilde{Y}_2^{(+)}(n, n-2, \rho; \bar{\eta}) = \exp\left[-\frac{\rho}{2}(1-\bar{\eta}^2)\right](1-\bar{\eta}^2)^{\frac{n-2}{2}}$$

$$\left\{1 - \frac{(2n-1)+2\rho + \sqrt{(2n-1)^2 - 4\rho(2n-3) + 4\rho^2}}{4(n-1)} (1-\bar{\eta}^2)\right\}$$

$$\tilde{Y}_1^{(-)}(n, n-3, \rho; \bar{\eta}) = \exp\left[-\frac{\rho}{2}(1-\bar{\eta}^2)\right](1-\bar{\eta}^2)^{\frac{n-3}{2}} \bar{\eta}$$

$$\left\{1 - \frac{(2n-1)+2\rho - \sqrt{(2n-1)^2 - 4\rho(2n-7) + 4\rho^2}}{4(n-2)} (1-\bar{\eta}^2)\right\}$$

$$\tilde{Y}_3^{(-)}(n, n-3, \rho; \bar{\eta}) = \exp\left[-\frac{\rho}{2}(1-\bar{\eta}^2)\right](1-\bar{\eta}^2)^{\frac{n-3}{2}} \bar{\eta}^3$$

$$\left\{1 - \frac{(2n-1)+2\rho + \sqrt{(2n-1)^2 - 4\rho(2n-7) + 4\rho^2}}{4(n-2)} (1-\bar{\eta}^2)\right\}$$

$$\tilde{X}_0^{(+)}(n, n, \rho; \bar{\xi}) = \exp\left(-\frac{\rho\bar{\xi}^2}{2}\right)(\bar{\xi}^2+1)^{\frac{n}{2}}$$

$$\tilde{X}_1^{(-)}(n, n-1, \rho; \bar{\xi}) = \exp\left(-\frac{\rho\bar{\xi}^2}{2}\right)(\bar{\xi}^2+1)^{\frac{n-1}{2}} \bar{\xi}$$

$$\tilde{X}_0^{(+)}(n, n-2, \rho; \bar{\xi}) = \exp\left(-\frac{\rho\bar{\xi}^2}{2}\right)(\bar{\xi}^2+1)^{\frac{n-2}{2}}$$

$$\left\{1 + \frac{(2n-1)-2\rho + \sqrt{(2n-1)^2 - 4\rho(2n-3) + 4\rho^2}}{2} \bar{\xi}^2\right\}$$

$$\tilde{X}_1^{(+)}(n, n-2, \rho; \bar{\xi}) = \exp\left(-\frac{\rho\bar{\xi}^2}{2}\right)(\bar{\xi}^2+1)^{\frac{n-2}{2}}$$

$$\left\{1 + \frac{(2n-1)-2\rho - \sqrt{(2n-1)^2 - 4\rho(2n-3) + 4\rho^2}}{2} \bar{\xi}^2\right\}$$

$$\tilde{X}_0^{(-)}(n, n-3, \rho; \bar{\xi}) = \exp\left(-\frac{\rho\bar{\xi}^2}{2}\right)(\bar{\xi}^2+1)^{\frac{n-3}{2}} \bar{\xi}$$

$$\left\{1 + \frac{(2n-1)-2\rho + \sqrt{(2n-1)^2 - 4\rho(2n-7) + 4\rho^2}}{6} \bar{\xi}^2\right\}$$

$$\tilde{X}_1^{(-)}(n, n-1, \rho; \bar{\xi}) = \exp\left(-\frac{\rho\bar{\xi}^2}{2}\right)(\bar{\xi}^2+1)^{\frac{n-1}{2}} \bar{\xi}$$

$$\left\{1 + \frac{(2n-1)-2\rho - \sqrt{(2n-1)^2 - 4\rho(2n-7) + 4\rho^2}}{6} \bar{\xi}^2\right\}$$

## 6. Eigenvalues $A_q^{(\pm)}$ and $B_k^{(\pm)}$

Eigenvalues  $A_q^{(\pm)}$  and  $B_k^{(\pm)}$  are determined from the requirement that the determinants for homogeneous systems of equations (5), (6), and (11), (12) equal zero. The dependence of  $A_q^{(\pm)}$  and  $B_k^{(\pm)}$  on  $C$  at given  $n$  and  $|m|$  is shown in Tables 5, 6 and graphs in Figs. 5. There is also given their analytic continuation into a "physical" region of oblate functions. Note that the quantum numbers  $q$  and  $k$  are related by  $n-|m|-q=2k/11$ , and

$$A_q^{(\pm)}(n, m, c) = B_k^{(\pm)}(n, m, c)$$

## 7. Conclusion

The functions studied above naturally arise when the variables are separated in the Schrödinger equation for an isotropic oscillator in prolate and oblate spheroidal coordinates. The latter are connected with rectangular coordinates as follows:

$$x = \frac{R}{2} \sqrt{(\bar{\xi}^2+1)(1-\bar{\eta}^2)} \cos \varphi, \quad y = \frac{R}{2} \sqrt{(\bar{\xi}^2+1)(1-\bar{\eta}^2)} \sin \varphi, \quad z = \frac{R}{2} \bar{\xi} \bar{\eta}$$

$$X = \frac{\bar{R}}{2} \sqrt{(\bar{\xi}^2 + 1)(1 - \bar{\eta}^2)} \cos \varphi, \quad Y = \frac{\bar{R}}{2} \sqrt{(\bar{\xi}^2 + 1)(1 - \bar{\eta}^2)} \sin \varphi, \quad Z = \frac{\bar{R}}{2} \bar{\xi} \bar{\eta}.$$

Here the angle  $\varphi$  changes within the interval  $0 \leq \varphi < 2\pi$ ; the range of variation of the coordinates  $(\bar{\xi}, \bar{\eta})$  and  $(\bar{R}, \bar{\eta})$  has been indicated in the main body of the manuscript. The parameter  $R$  is expressed through  $C$  by the formula

$$C = \frac{\mu \omega}{4\pi} R^2$$

in which  $\mu$  is the mass,  $\omega$  is a cyclic velocity of an isotropic oscillator. An analogous relation is valid for parameters  $\bar{R}$  and  $\rho$ . Total wave functions of an isotropic oscillator in prolate spheroidal coordinates have the form

$$\Psi_{nqkm}^{(\pm)}(\bar{\xi}, \bar{\eta}, \varphi; C) = N_{nqm}^{(\pm)}(C) Y_q^{(\pm)}(n, m, c; \bar{\eta}) X_\kappa^{(\pm)}(n, m, c; \bar{\xi}) \frac{e^{im\varphi}}{\sqrt{2\pi}}$$

where  $N_{nqm}^{(\pm)}(C)$  is a normalization constant. The oblate basis follows from this formula by the change  $\bar{\eta} \rightarrow \bar{\xi}$ ,  $\bar{\xi} \rightarrow \bar{\eta}$ ,  $C \rightarrow \rho$ . Indices of the total wave functions of the oscillator are related by  $n = 2\kappa + |m| + q$ .

We are grateful to Yu.A. Budagov, A.A. Bogush, and L.I. Ponomarev for interest in the work.

#### References

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2. I.V. Komarov, L.I. Ponomarev, S.Yu. Slavyanov. Spheroidal and Coulomb Spheroidal Functions, Nauka, Moscow, 1976 (in Russian).

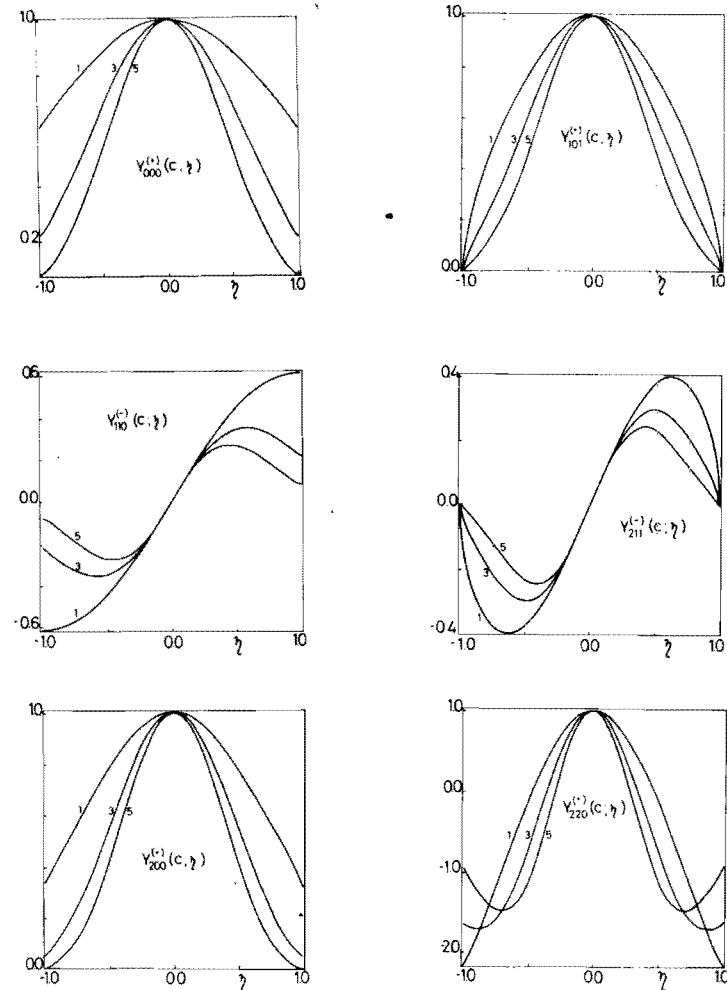


Fig. 1a. Prolate angular spheroidal functions  $Y_{nqm}^{(\pm)}(c; \eta)$ ,  $Y_q^{(\pm)}(n, m, c; \eta)$ ,  $c = 1, 3, 5$

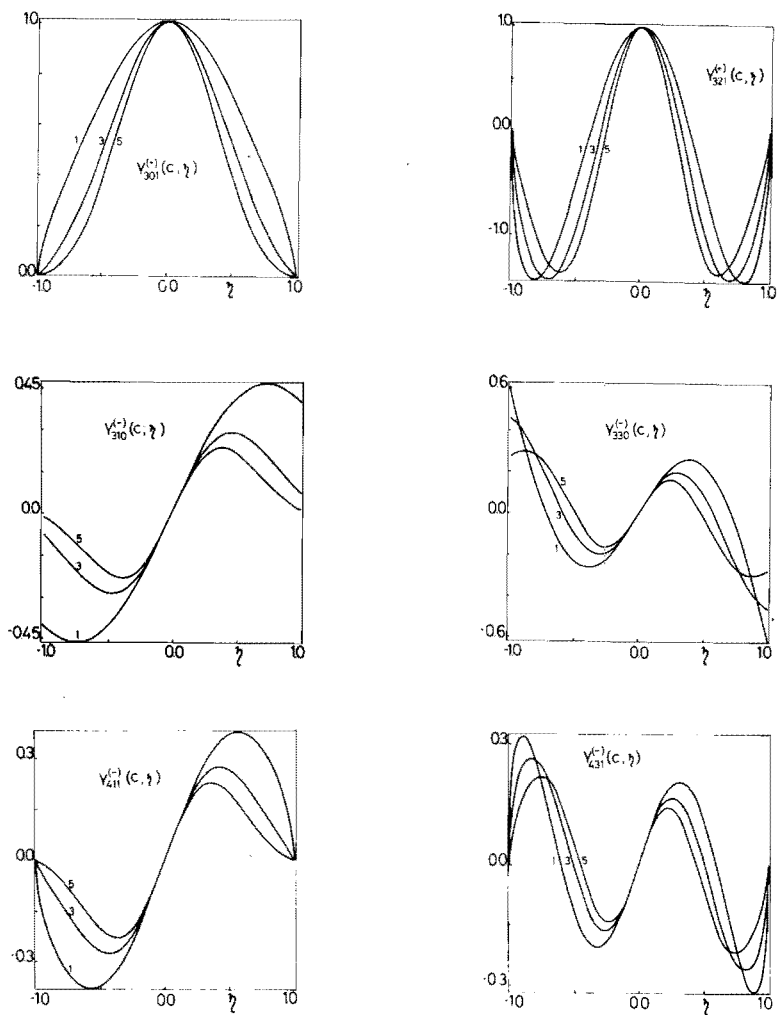


Fig. 1b. Prolate angular spheroidal functions  
 $Y_{nqm}(c, \eta) \equiv Y_q(n, m, c; \eta)$ ,  $c = 1, 3, 5$

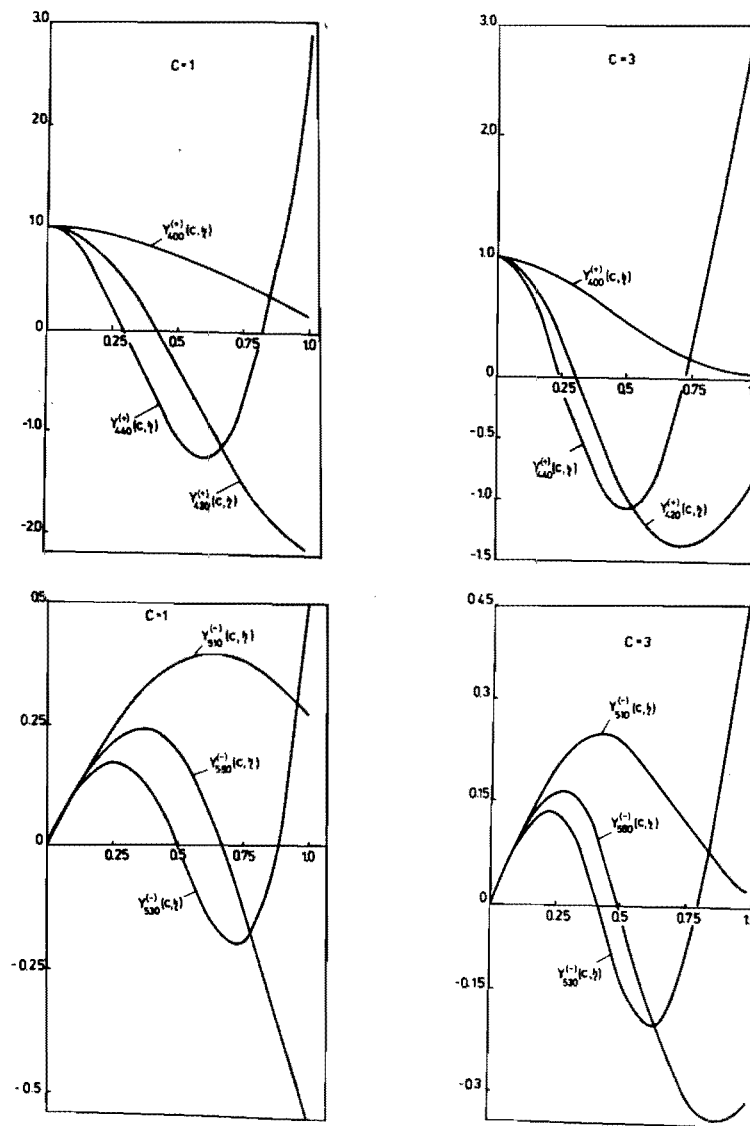


Fig. 1c. Prolate angular spheroidal functions  
 $Y_{nqm}(c; \eta) \equiv Y_q(n, m, c; \eta)$

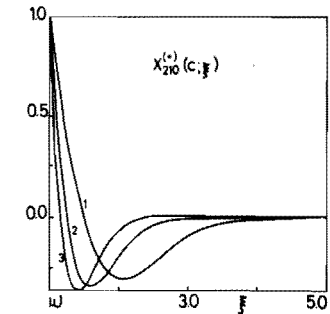
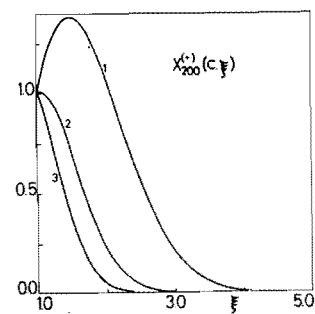
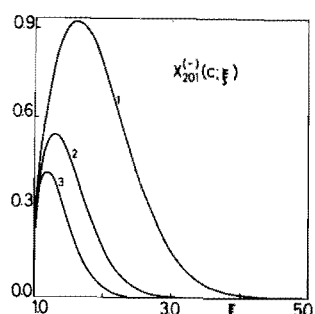
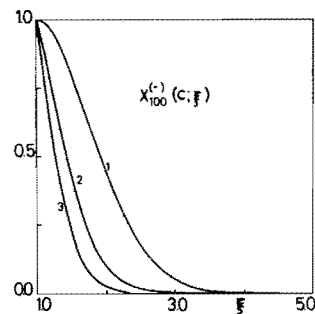
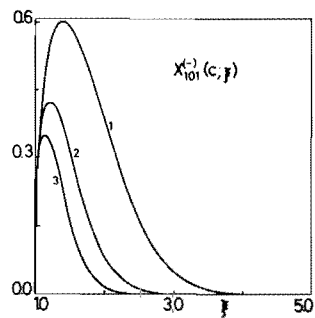
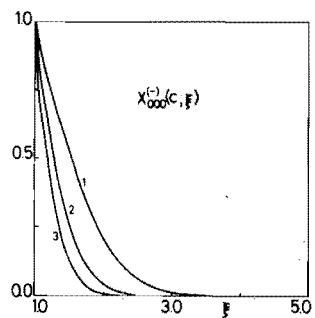


Fig. 2a. Prolate radial spheroidal functions  
 $X_{nkm}^{(-)}(c; \xi) \equiv X_k(n, m, c; \xi)$ ;  $c = 1, 2, 3$

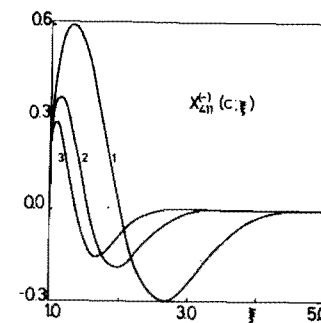
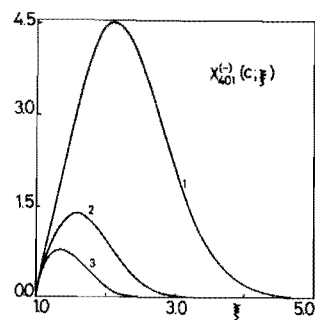
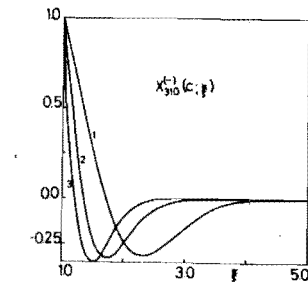
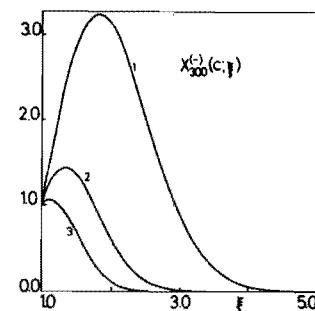
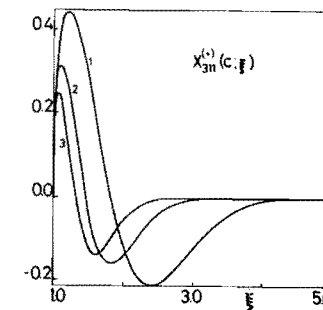
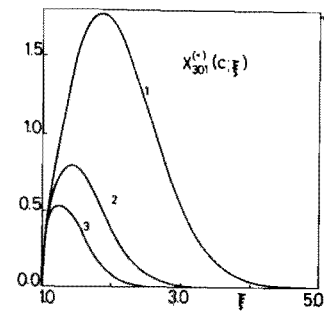


Fig. 2b. Prolate radial spheroidal functions  
 $X_{nkm}^{(-)}(c; \xi) \equiv X_k(n, m, c; \xi)$ ;  $c = 1, 2, 3$



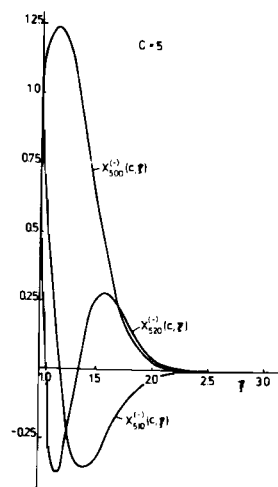
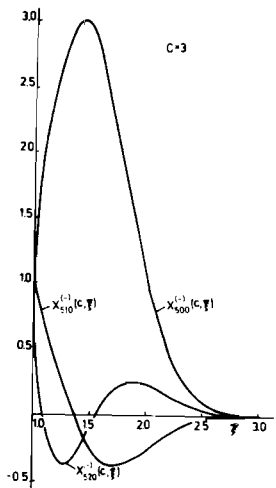
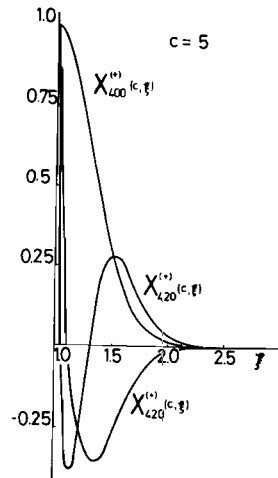
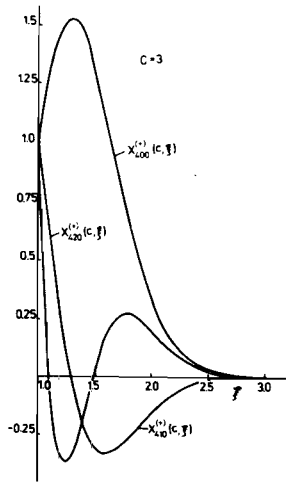


Fig. 2c. Prolate radial spheroidal functions

$$X_{nlm}(c; \xi) \equiv X_k(n, m, c; \xi)$$

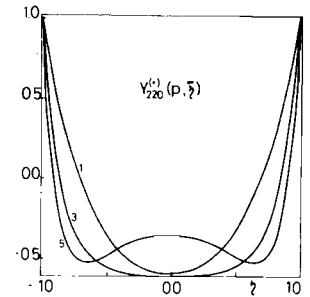
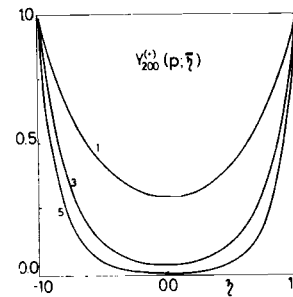
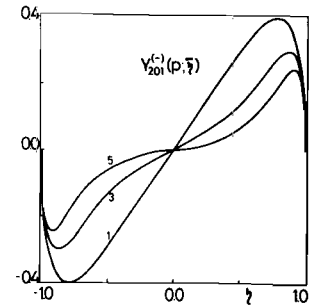
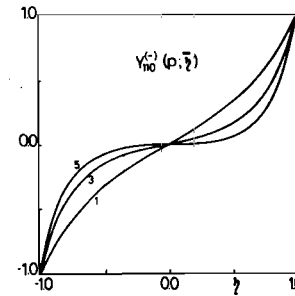
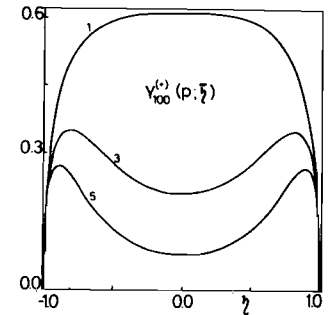
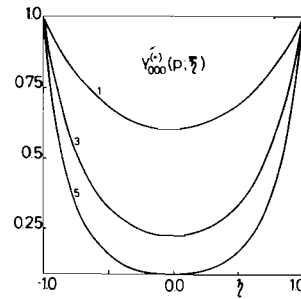


Fig. 3a. Oblate angular spheroidal functions  
 $Y_{ntm}(p; \bar{\eta}) \equiv \tilde{Y}_t(n, m, p; \bar{\eta}), p = 1, 3, 5$

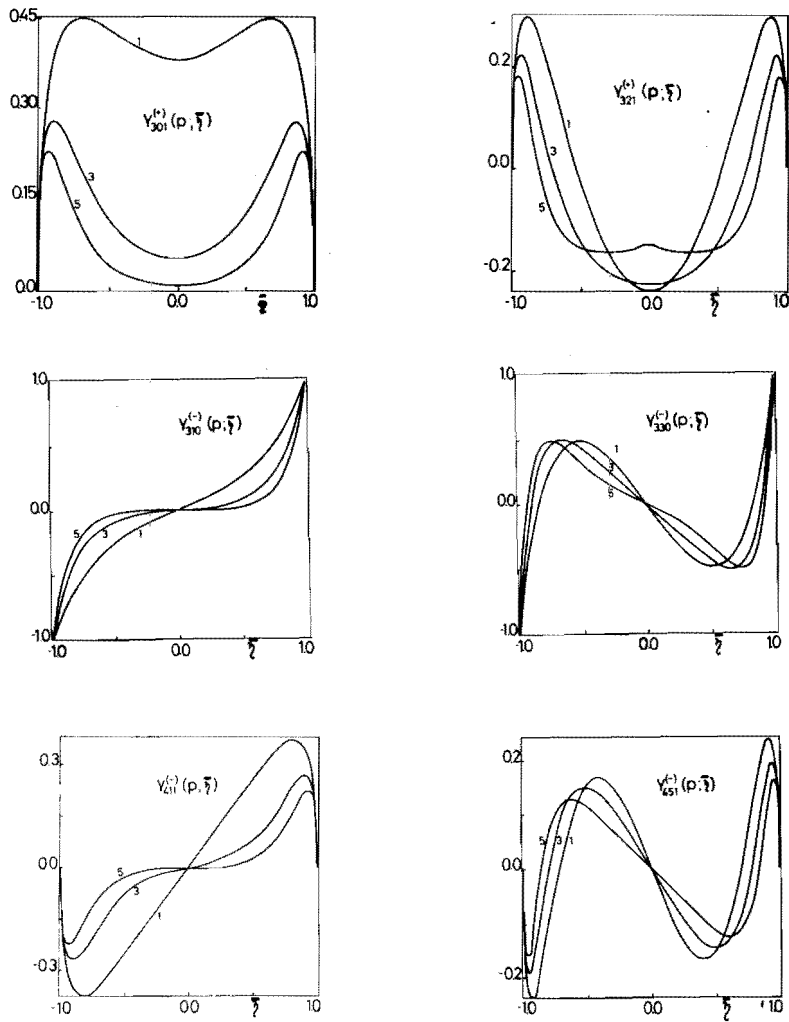


Fig. 3b. Oblate angular spheroidal functions  
 $Y_{ntm}(p; \bar{\eta}) \equiv \tilde{Y}_t(n, m, p; \bar{\eta}), p = 1, 3, 5$

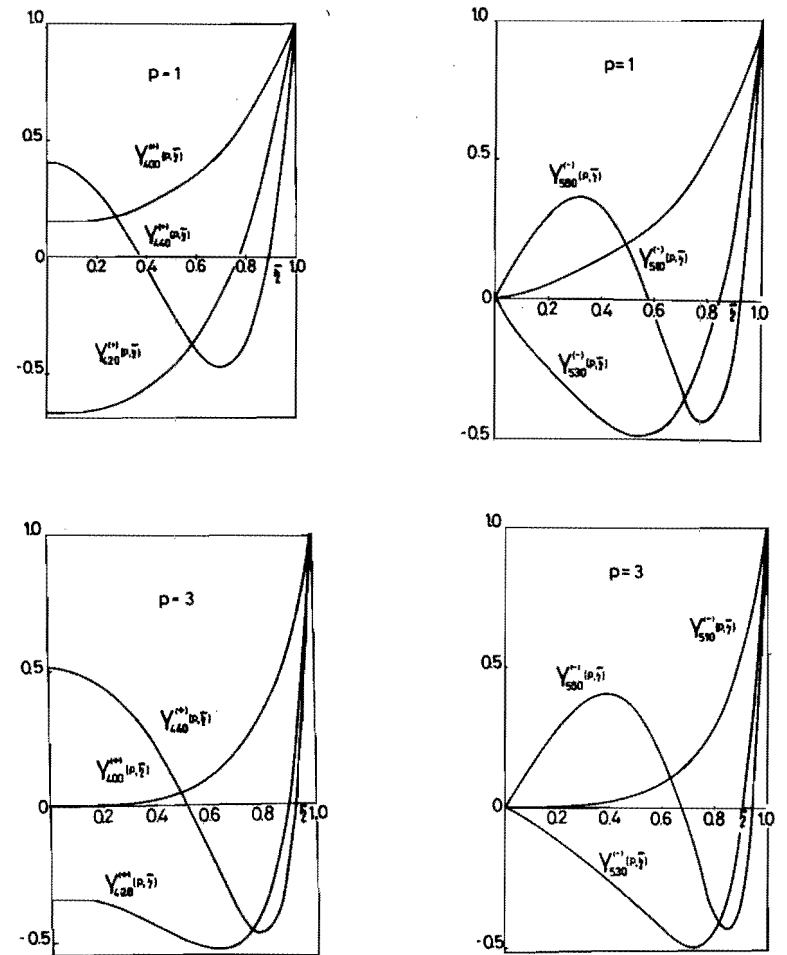


Fig. 3c. Oblate angular spheroidal functions  
 $Y_{ntm}(p; \bar{\eta}) = \tilde{Y}_t(n, m, p; \bar{\eta})$

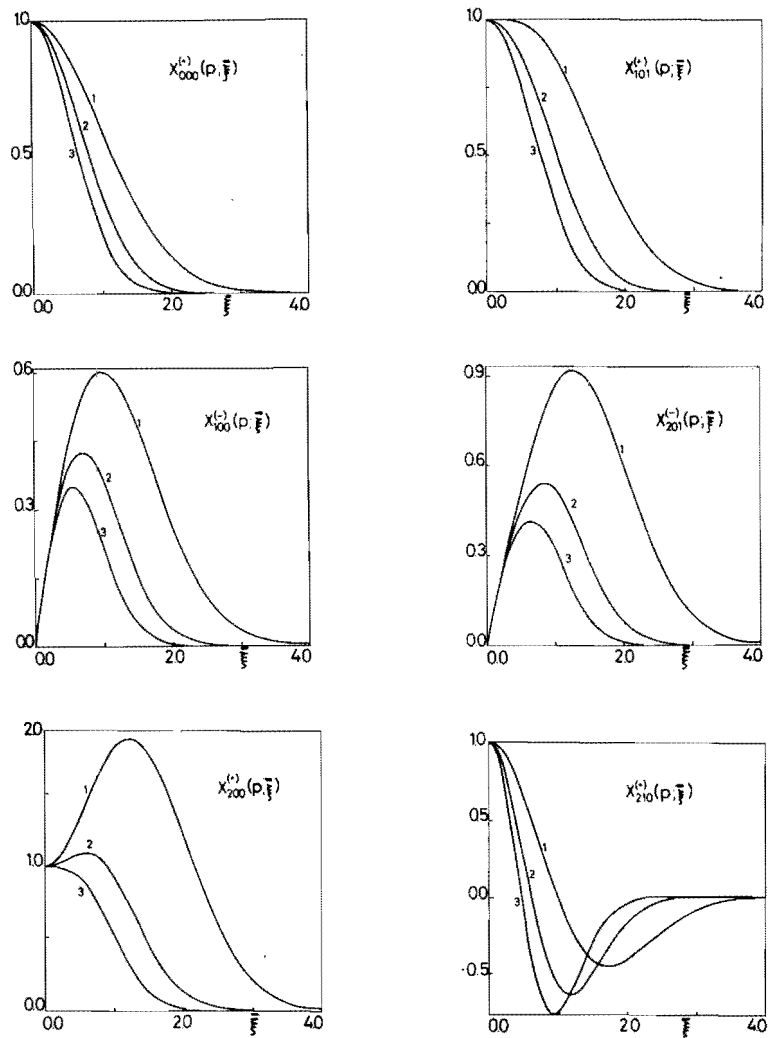


Fig. 4a. Oblate radial spheroidal functions  
 $X_{nmn}(p; \xi) \equiv \tilde{X}_r(n, m, p; \xi)$ ;  $p = 1, 2, 3$

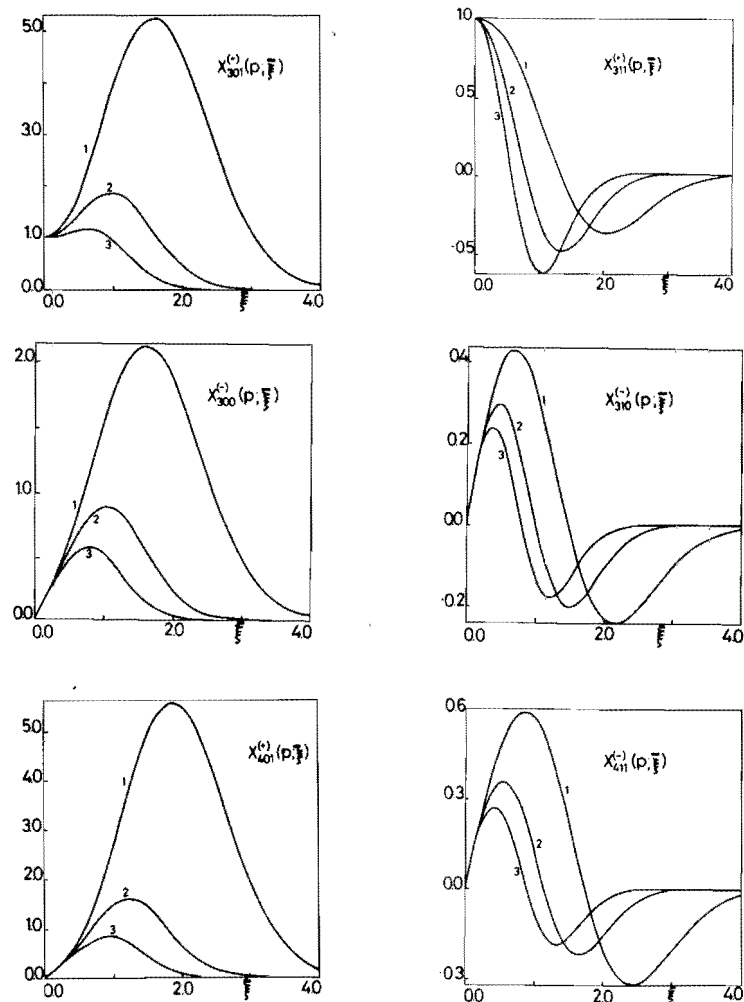


Fig. 4b. Oblate radial spheroidal functions  
 $X_{nmn}(p; \xi) \equiv \tilde{X}_r(n, m, p; \xi)$ ;  $p = 1, 2, 3$

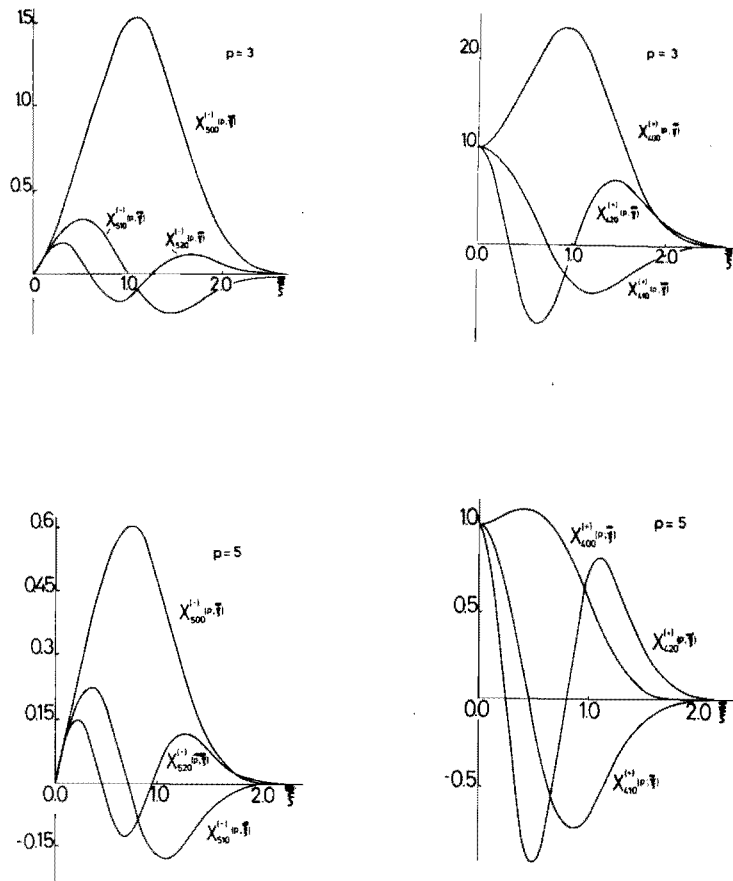


Fig. 4c. Oblate radial spheroidal functions  $X_{nm}^{(1)}(p; \xi) \sim \tilde{X}_r(n, m, p; \xi)$ ;

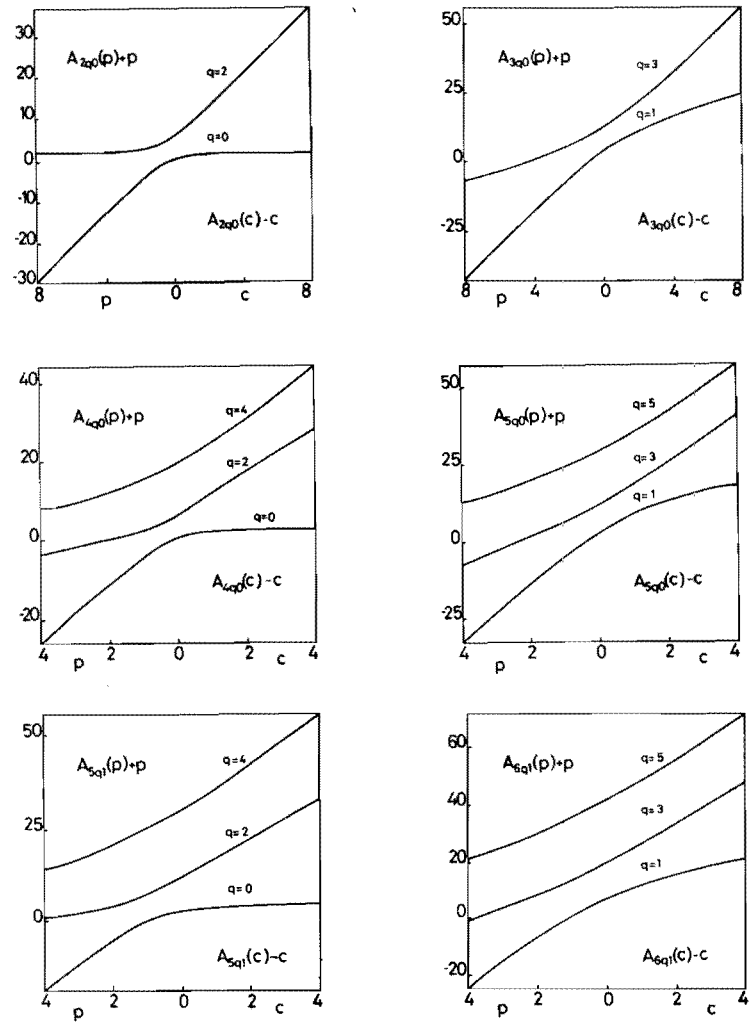


Fig. 5. Eigenvalues of the separation constants  $A_{nqm}(c) \equiv A_q(n, m, c)$  and  $A_{nqm}(p) \equiv A_q(n, m, p)$

Table 1a. Prolate angular spheroidal functions  $Y_0^{(+)}(m, n, c; \eta)$

$n$	$c\eta$	.0	.1	.2	.3	.4	.5	.6	.7	.8	.9	1.0
0	1	1.0000	.9950	.9882	.9558	.9231	.8825	.8353	.7827	.7261	.6678	.6065
	1	1.0000	.9900	.9606	.8737	.7866	.6988	.6127	.5295	.4499	.3739	.3019
	1	1.0000	.9851	.9418	.8337	.7066	.5788	.4527	.3329	.2219	.1199	.0281
1	1	1.0000	.9900	.9604	.8710	.7810	.6943	.6102	.5295	.4527	.3800	.3119
	1	1.0000	.9851	.9414	.8335	.7210	.6085	.5062	.4149	.3342	.2649	.2071
	1	1.0000	.9802	.9227	.8335	.7210	.6085	.5062	.4149	.3342	.2649	.2071
2	1	1.0000	.9851	.9410	.8317	.7158	.6019	.4896	.3992	.3244	.2649	.2171
	1	1.0000	.9802	.9224	.8317	.7158	.6019	.4896	.3992	.3244	.2649	.2171
	1	1.0000	.9753	.9041	.7951	.6608	.5155	.3730	.2445	.1378	.0564	.0000
3	1	1.0000	.9802	.9228	.8299	.7107	.5732	.4477	.3451	.2651	.2052	.1568
	1	1.0000	.9753	.9039	.7934	.6560	.5272	.4149	.3221	.2421	.1826	.1349
	1	1.0000	.9704	.8950	.7805	.6356	.5064	.3984	.3084	.2287	.1686	.1209
4	1	1.0000	.9704	.8934	.7817	.6314	.5021	.3941	.3036	.2236	.1635	.1158
	1	1.0000	.9655	.8855	.7735	.6233	.4940	.3860	.2955	.2155	.1554	.1077
	1	1.0000	.9607	.8779	.7655	.6153	.4860	.3780	.2875	.2075	.1474	.0997
5	1	1.0000	.9607	.8751	.7622	.6120	.4827	.3747	.2842	.2042	.1441	.0964
	1	1.0000	.9555	.8687	.7552	.6050	.4757	.3677	.2772	.1972	.1371	.0894
	1	1.0000	.9506	.8616	.7482	.5980	.4687	.3607	.2702	.1902	.1301	.0824
6	1	1.0000	.9506	.8597	.7462	.5960	.4667	.3587	.2682	.1882	.1281	.0804
	1	1.0000	.9456	.8527	.7392	.5890	.4597	.3517	.2612	.1812	.1211	.0734
	1	1.0000	.9407	.8458	.7323	.5821	.4528	.3448	.2543	.1743	.1142	.0665
7	1	1.0000	.9407	.8438	.7303	.5801	.4508	.3428	.2523	.1723	.1122	.0645
	1	1.0000	.9357	.8368	.7233	.5731	.4438	.3358	.2453	.1653	.1052	.0575
	1	1.0000	.9308	.8299	.7164	.5662	.4369	.3289	.2384	.1584	.0983	.0506
8	1	1.0000	.9308	.8299	.7164	.5662	.4369	.3289	.2384	.1584	.0983	.0506
	1	1.0000	.9258	.8229	.7094	.5592	.4299	.3219	.2314	.1514	.0913	.0436
	1	1.0000	.9209	.8160	.7025	.5523	.4230	.3150	.2245	.1445	.0844	.0367
9	1	1.0000	.9209	.8160	.7025	.5523	.4230	.3150	.2245	.1445	.0844	.0367
	1	1.0000	.9159	.8090	.6955	.5453	.4160	.3080	.2175	.1375	.0774	.0297
	1	1.0000	.9110	.8021	.6886	.5384	.4091	.3011	.2106	.1306	.0705	.0228

Table 1b. Prolate angular spheroidal functions  $Y_1^{(-)}(m, n-1, c; \eta)$

$n$	$c\eta$	0.0	.1	.2	.3	.4	.5	.6	.7	.8	.9	1.0
1	1	0.0000	.3995	.1960	.2868	.3692	.4412	.5012	.5479	.5809	.6083	.6295
	1	0.0000	.3995	.1922	.2742	.3409	.3994	.4494	.4928	.5218	.5394	.5494
	1	0.0000	.3980	.1884	.2621	.3147	.3586	.3963	.4267	.4500	.4662	.4749
2	1	0.0000	.3990	.1921	.2736	.3304	.3821	.4209	.4493	.4686	.4797	.4830
	1	0.0000	.3985	.1883	.2616	.3184	.3701	.4189	.4572	.4856	.5040	.5127
	1	0.0000	.3980	.1845	.2578	.3146	.3663	.4151	.4534	.4818	.4999	.5086
3	1	0.0000	.3985	.1882	.2610	.3178	.3695	.4183	.4566	.4850	.5031	.5118
	1	0.0000	.3979	.1848	.2585	.3153	.3670	.4158	.4541	.4825	.5006	.5093
	1	0.0000	.3973	.1810	.2547	.3115	.3632	.4120	.4503	.4787	.4968	.5055
4	1	0.0000	.3973	.1847	.2575	.3143	.3660	.4148	.4531	.4815	.5000	.5087
	1	0.0000	.3967	.1807	.2544	.3112	.3629	.4117	.4500	.4784	.4965	.5052
	1	0.0000	.3961	.1772	.2513	.3081	.3598	.4086	.4469	.4753	.4934	.5021
5	1	0.0000	.3961	.1807	.2535	.3103	.3620	.4108	.4491	.4775	.4960	.5047
	1	0.0000	.3955	.1771	.2504	.3072	.3589	.4077	.4460	.4744	.4929	.5016
	1	0.0000	.3949	.1736	.2473	.3041	.3558	.4046	.4429	.4713	.4898	.4985
6	1	0.0000	.3949	.1773	.2466	.3034	.3551	.4039	.4422	.4706	.4891	.4978
	1	0.0000	.3943	.1737	.2435	.3003	.3520	.4008	.4391	.4675	.4860	.4947
	1	0.0000	.3937	.1701	.2404	.2972	.3489	.3974	.4357	.4641	.4826	.4913
7	1	0.0000	.3937	.1734	.2397	.2965	.3482	.3967	.4350	.4634	.4819	.4906
	1	0.0000	.3931	.1700	.2366	.2934	.3451	.3936	.4319	.4603	.4788	.4875
	1	0.0000	.3925	.1666	.2335	.2903	.3420	.3905	.4288	.4572	.4757	.4844
8	1	0.0000	.3925	.1703	.2328	.2872	.3389	.3874	.4257	.4541	.4726	.4813
	1	0.0000	.3919	.1669	.2297	.2841	.3358	.3843	.4226	.4510	.4695	.4782
	1	0.0000	.3913	.1635	.2266	.2810	.3327	.3812	.4195	.4479	.4664	.4751
9	1	0.0000	.3913	.1699	.2259	.2803	.3320	.3805	.4188	.4472	.4657	.4744
	1	0.0000	.3907	.1665	.2228	.2772	.3289	.3774	.4157	.4441	.4626	.4713
	1	0.0000	.3901	.1631	.2197	.2741	.3258	.3743	.4126	.4410	.4595	.4682
10	1	0.0000	.3901	.1697	.2190	.2734	.3251	.3736	.4119	.4403	.4588	.4675
	1	0.0000	.3895	.1663	.2159	.2703	.3218	.3703	.4086	.4370	.4555	.4642
	1	0.0000	.3889	.1629	.2128	.2672	.3187	.3672	.4055	.4339	.4524	.4611

Table 1c. Prolate angular spheroidal functions  $Y_q^{(+)}(n, n-2, 0; \eta)$

n	q	$\eta$	0.0	.1	.2	.3	.4	.5	.6	.7	.8	.9	1.0
2	0	1 2 3	1.0000	.9530	.9183	.8884	.8584	.8258	.7834	.6445	.5244	.4341	.3486
2	2	1 2 3	1.0000	.9145	.8633	.8167	.7696	.7266	.6800	.4422	.3155	.2187	.1370
2	2	1 2 3	1.0000	.9145	.8633	.8167	.7696	.7266	.6800	.4422	.3155	.2187	.1370
3	0	1 2 3	1.0000	.9489	.9129	.8755	.8377	.8000	.7624	.5964	.4772	.3825	.3000
3	2	1 2 3	1.0000	.9110	.8633	.8167	.7696	.7266	.6800	.4422	.3155	.2187	.1370
3	2	1 2 3	1.0000	.9110	.8633	.8167	.7696	.7266	.6800	.4422	.3155	.2187	.1370
4	0	1 2 3	1.0000	.9324	.9021	.8708	.8385	.8052	.7720	.6241	.5041	.4033	.3200
4	2	1 2 3	1.0000	.8987	.8552	.8117	.7682	.7247	.6812	.4933	.3733	.2844	.2000
4	2	1 2 3	1.0000	.8987	.8552	.8117	.7682	.7247	.6812	.4933	.3733	.2844	.2000
5	0	1 2 3	1.0000	.9152	.8923	.8684	.8435	.8176	.7917	.6660	.5560	.4614	.3700
5	2	1 2 3	1.0000	.8828	.8389	.7950	.7511	.7072	.6633	.5154	.4154	.3300	.2400
5	2	1 2 3	1.0000	.8828	.8389	.7950	.7511	.7072	.6633	.5154	.4154	.3300	.2400
6	0	1 2 3	1.0000	.9377	.9115	.8843	.8561	.8270	.7978	.6829	.5829	.4975	.4100
6	2	1 2 3	1.0000	.8950	.8501	.8052	.7603	.7154	.6705	.5456	.4556	.3800	.2900
6	2	1 2 3	1.0000	.8950	.8501	.8052	.7603	.7154	.6705	.5456	.4556	.3800	.2900

Table 1d. Prolate angular spheroidal functions  $Y_q(n, n-3, c; \eta)$

n	q	$\eta$	0.0	.1	.2	.3	.4	.5	.6	.7	.8	.9	1.0
3	1	1 2 3	0.0000	.0992	.1934	.2782	.3496	.4045	.4410	.4584	.4570	.4382	.4044
3	3	1 2 3	0.0000	.0985	.1883	.2664	.3311	.3866	.4257	.4480	.4554	.4328	.3844
4	1	1 2 3	0.0000	.0975	.1884	.2652	.3288	.3843	.4234	.4457	.4521	.4282	.3805
4	3	1 2 3	0.0000	.0975	.1884	.2652	.3288	.3843	.4234	.4457	.4521	.4282	.3805
5	1	1 2 3	0.0000	.0977	.1888	.2655	.3291	.3846	.4237	.4460	.4524	.4285	.3808
5	3	1 2 3	0.0000	.0977	.1888	.2655	.3291	.3846	.4237	.4460	.4524	.4285	.3808
6	1	1 2 3	0.0000	.0979	.1892	.2659	.3295	.3850	.4241	.4464	.4528	.4289	.3810
6	3	1 2 3	0.0000	.0979	.1892	.2659	.3295	.3850	.4241	.4464	.4528	.4289	.3810
7	1	1 2 3	0.0000	.0982	.1897	.2666	.3302	.3857	.4248	.4471	.4535	.4296	.3817
7	3	1 2 3	0.0000	.0982	.1897	.2666	.3302	.3857	.4248	.4471	.4535	.4296	.3817

Table 1e. Prolate angular spheroidal functions  $Y_q^{(+)}(n, n-4, c; \eta)$

n	q	c/2	η					η					
			0.0	.1	.2	.3	.4	.5	.6	.7	.8	.9	1.0
4	4	1	1.0000	.3727	.5171	-.3092	-.5352	-.9751	-1.1624	-.9600	-.2598	1.0040	2.0460
		2	1.0000	.3611	.4083	-.1765	-.7416	-1.1049	-1.1138	-.6789	-.2085	1.4757	2.0980
		3	1.0000	.3859	.2942	-.3563	-.3049	-1.1493	-.9452	-.2862	.7223	1.5345	2.0190
		4	1.0000	.7211	.1784	-.5223	-1.0285	-1.1072	-.6798	.1606	1.1973	2.1767	2.0818
		5	1.0000	.7323	.6643	-.6681	-1.0958	-.9902	-.3555	.5978	1.5661	2.2841	2.6125
4	2	1	1.0000	.3373	.7565	.4710	-.1050	-.3117	-.7461	-1.1645	-1.5358	-1.8340	-2.0401
		2	1.0000	.9649	.6349	-.2308	-.2450	-.7232	-1.1380	-1.4374	-1.5905	-1.5904	-1.4521
		3	1.0000	.3774	.5255	-.0297	-.5084	-.9826	-1.3098	-1.4464	-1.3927	-1.1856	-.8842
		4	1.0000	.3463	.4284	-.1381	-.7052	-1.1388	-1.3569	-1.3446	-1.1462	-.8401	-.5099
		5	1.0000	.3173	.3433	-.2810	-.8543	-1.1220	-1.3369	-1.2053	-.9205	-.5874	-.2966
4	0	1	1.0000	.3873	.9438	.8838	.8107	.7169	.6135	.5057	.3987	.2972	.2050
		2	1.0000	.3793	.9132	.8260	.7089	.5788	.4468	.3229	.2146	.1268	.0613
		3	1.0000	.3737	.8946	.7767	.6345	.4853	.3446	.2240	.1299	.0635	.0222
		4	1.0000	.3667	.8727	.7343	.5738	.4138	.2727	.1614	.0831	.0345	.0090
		5	1.0000	.3611	.8525	.6964	.5218	.3562	.2190	.1189	.0549	.0197	.0039
5	4	1	1.0000	.3264	.3580	-.2596	-.8196	-1.1030	-.9384	-.2687	.7697	1.6989	0.0000
		2	1.0000	.7291	.2534	-.4237	-.9556	-1.1022	-.7338	.1996	1.1313	1.9230	0.0000
		3	1.0000	.7231	.1434	-.5735	-1.0474	-1.1030	-.4639	.4801	1.4298	1.8560	0.0000
		4	1.0000	.7213	.0325	-.7051	-1.0941	-.8985	-.1570	.8341	1.6381	1.7991	0.0000
		5	1.0000	.5843	-.0717	-.8165	-1.0981	-.7203	.1592	1.1332	1.7481	1.6694	0.0000
5	2	1	1.0000	.3146	.6694	.2963	-1.1554	-.6239	-1.3406	-1.3342	-1.4300	-1.2260	0.0000
		2	1.0000	.3843	.5601	-.0910	-.9319	-.9909	-1.2515	-1.3957	-1.3088	-.9733	0.0000
		3	1.0000	.3524	.4594	-.0864	-.6468	-1.0914	-1.3289	-1.3256	-1.1039	-.7175	0.0000
		4	1.0000	.3213	.3663	-.2333	-.8119	-1.1998	-1.3226	-1.1987	-.8942	-.5407	0.0000
		5	1.0000	.3617	.2813	-.3721	-.3393	-1.2565	-1.2762	-1.0545	-.7092	-.3577	0.0000
5	0	1	1.0000	.9845	.9389	.6664	.7715	.6601	.5388	.4139	.2907	.1708	0.0000
		2	1.0000	.3736	.9011	.6053	.6765	.5299	.3929	.2697	.1589	.0782	0.0000
		3	1.0000	.3639	.8842	.7561	.6041	.4687	.3069	.1867	.0849	.0480	0.0000
		4	1.0000	.3637	.8623	.7138	.5447	.3802	.2396	.1333	.0626	.0220	0.0000
		5	1.0000	.3553	.8415	.6766	.4841	.3259	.1912	.0974	.0409	.0124	0.0000
6	4	1	1.0000	.7823	.2148	-.4719	-.9767	-1.0331	-.5245	.4185	1.3534	1.5524	0.0000
		2	1.0000	.7281	.1132	-.6086	-1.0435	-.9306	-.2408	.7609	1.5558	1.4994	0.0000
		3	1.0000	.7129	-.0773	-.7242	-1.0703	-.7803	.0598	1.0587	1.6663	1.3925	0.0000
		4	1.0000	.6774	-.1926	-.8293	-1.0593	-.5941	.3671	1.2971	1.6966	1.2500	0.0000
		5	1.0000	.5442	-.1883	-.9110	-1.0147	-.3848	.6345	1.4695	1.6593	1.0894	0.0000
6	2	1	1.0000	.3942	.5846	.1358	-.3717	-.8402	-1.1729	-1.2888	-1.1356	-.6978	0.0000
		2	1.0000	.3643	.4836	-.3431	-.5896	-1.0260	-1.2530	-1.2240	-.9543	-.6122	0.0000
		3	1.0000	.3373	.3835	-.1995	-.7598	-1.1394	-1.2536	-1.1042	-.7677	-.3610	0.0000
		4	1.0000	.3113	.3025	-.3329	-.8909	-1.1999	-1.2069	-.9664	-.6024	-.2488	0.0000
		5	1.0000	.2819	.2202	-.4853	-.9905	-1.2227	-1.1340	-.8301	-.4656	-.1693	0.0000
6	0	1	1.0000	.3813	.9250	.8362	.7284	.6348	.4761	.3492	.2261	.1128	0.0000
		2	1.0000	.3732	.8972	.7836	.6485	.5086	.3772	.2619	.1639	.0799	0.0000
		3	1.0000	.3656	.8733	.7333	.5857	.4377	.3095	.2063	.1254	.0591	0.0000
		4	1.0000	.3605	.8517	.6939	.5378	.3820	.2591	.1669	.0986	.0451	0.0000
		5	1.0000	.3547	.8316	.6635	.4885	.3362	.2197	.1370	.0783	.0344	0.0000
7	4	1	1.0000	.7374	.1826	-.6457	-1.0578	-.8810	-.1175	.8813	1.4894	1.1060	0.0000
		2	1.0000	.7078	-.0175	-.7534	-1.0778	-.7309	.1575	1.1527	1.5272	.9949	0.0000
		3	1.0000	.6696	-.1147	-.8551	-1.0608	-.5489	.4275	1.3010	1.5099	.8726	0.0000
		4	1.0000	.6333	-.2081	-.9326	-1.0131	-.3463	.6781	1.4302	1.4468	.7477	0.0000
		5	1.0000	.5981	-.2963	-.9919	-.9385	-.1338	.8993	1.5050	1.3497	.6273	0.0000
7	2	1	1.0000	.3673	.5610	-.3168	-.5657	-1.0149	-1.2518	-1.2100	-.8938	-.4013	0.0000
		2	1.0000	.8339	.4056	-.1781	-.7467	-1.1847	-1.2728	-1.1131	-.7391	-.2948	0.0000
		3	1.0000	.3123	.3162	-.3201	-.8879	-1.2183	-1.2726	-.9884	-.5928	-.2108	0.0000
		4	1.0000	.2892	.2324	-.4447	-.9962	-1.2506	-1.2325	-.8581	-.5655	-.1481	0.0000
		5	1.0000	.2612	.1536	-.5541	-1.0776	-1.2526	-1.0900	-.8338	-.3626	-.1031	0.0000
7	0	1	1.0000	.3736	.9087	.8035	.6702	.5226	.3738	.2367	.1225	.0401	0.0000
		2	1.0000	.3639	.8826	.7597	.6239	.4319	.2832	.1613	.0736	.0208	0.0000
		3	1.0000	.3623	.8586	.7054	.5318	.3628	.2196	.1135	.0460	.0112	0.0000
		4	1.0000	.3557	.8365	.6662	.4795	.3081	.1730	.0815	.0295	.0063	0.0000
		5	1.0000	.3513	.8164	.6334	.4344	.2637	.1378	.0595	.0194	.0036	0.0000

Table 1f. Prolate angular spheroidal functions  $Y_q^{(-)}(n, n-5, c; \eta)$

n	q	c/k	c/k				c/k													
			0.0	.1	.2	.3	.4	.5	.6	.7	.8	.9	1.0							
5	5	1	0.0000	.09-3	.1560	.1616														
		2	0.0000	.0931	.1475	.1387	.1041	-.0028	-.1229	-.2012	-.1694	.0444	.5063							
		3	0.0000	.0918	.1385	.1156	.0657	-.0458	-.1494	-.1890	-.1137	.1087	.4828							
		4	0.0000	.0924	.1292	.0927	.0300	-.0803	-.1608	-.1605	-.0502	.1674	.4590							
		5	0.0000	.0864	.1196	.0706	-.0021	-.1352	-.1578	-.1194	.0151	.2152	.4294							
5	3	1	0.0000	.0971	.1774	.2261														
		2	0.0000	.0958	.1672	.1955	.2321	.1896	.0984	-.0361	-.2031	-.3886	-.5761							
		3	0.0000	.0944	.1572	.1667	.1710	.0958	-.0480	-.1504	-.2762	-.4111	-.4423							
		4	0.0000	.0933	.1473	.1411	.1177	.0222	-.0351	-.2050	-.2825	-.3129	-.2948							
		5	0.0000	.0923	.1391	.1187	.0739	-.0310	-.1393	-.2190	-.2509	-.2334	-.1792							
5	1	1	0.0000	.0939	.1911	.2707														
		2	0.0000	.0930	.1847	.2504	.3328	.3739	.3926	.3891	.3654	.3249	.2720							
		3	0.0000	.0923	.1795	.2348	.2892	.2989	.2820	.2439	.1926	.1364	.0828							
		4	0.0000	.0917	.1750	.2216	.2575	.2485	.2147	.1661	.1135	.0660	.0222							
		5	0.0000	.0912	.1708	.2099	.2321	.2108	.1685	.1182	.0713	.0349	.0115							
6	5	1	0.0000	.0924	.1425	.1247														
		2	0.0000	.0911	.1337	.1027	.0415	-.0723	-.1575	-.4494	-.0106	.2112	0.0000							
		3	0.0000	.0897	.1247	.0814	.0098	-.0981	-.1563	-.1120	-.0422	.2284	0.0000							
		4	0.0000	.0883	.1156	.0611	-.0181	-.1151	-.1442	-.1691	.0891	.2354	0.0000							
		5	0.0000	.0868	.1066	.0420	-.0417	-.1239	-.1236	-.1247	.1271	.2323	0.0000							
6	3	1	0.0000	.0959	.1685	.1985														
		2	0.0000	.0947	.1591	.1715	.1752	.0983	-.0202	-.1560	-.2720	-.3104	0.0000							
		3	0.0000	.0934	.1499	.1464	.1251	.0296	-.0903	-.2015	-.2682	-.2539	0.0000							
		4	0.0000	.0921	.1412	.1237	.0818	-.0233	-.1344	-.2155	-.2399	-.1940	0.0000							
		5	0.0000	.0909	.1329	.1033	.0456	-.0621	-.1583	-.2097	-.2023	-.1418	0.0000							
6	1	1	0.0000	.0935	.1885	.2622														
		2	0.0000	.0923	.1825	.2437	.3135	.3386	.3359	.3051	.2509	.1705	0.0000							
		3	0.0000	.0911	.1774	.2285	.2749	.2757	.2476	.1801	.1417	.0804	0.0000							
		4	0.0000	.0904	.1728	.2154	.2449	.2290	.1892	.1374	.0852	.0408	0.0000							
		5	0.0000	.0900	.1687	.2038	.2204	.1937	.1480	.0976	.0535	.0219	0.0000							
7	5	1	0.0000	.0935	.1300	.0929														
		2	0.0000	.0922	.1212	.0727	-.0049	-.1085	-.1462	-.0691	.0998	.2195	0.0000							
		3	0.0000	.0908	.1124	.0536	-.0297	-.1202	-.1289	-.0283	.1308	.0886	0.0000							
		4	0.0000	.0894	.1037	.0387	-.0504	-.1245	-.1056	.0114	.1531	.1929	0.0000							
		5	0.0000	.0883	.0950	.0192	-.0795	-.1226	-.0785	.0467	.1665	.1738	0.0000							
7	3	1	0.0000	.0943	.1600	.1736														
		2	0.0000	.0935	.1511	.1492	.1273	.0299	-.0928	-.1018	-.2511	-.1955	0.0000							
		3	0.0000	.0923	.1425	.1266	.0853	-.0240	-.1337	-.2019	-.2223	-.1494	0.0000							
		4	0.0000	.0911	.1342	.1061	.0492	-.0595	-.1569	-.2019	-.1876	-.1101	0.0000							
		5	0.0000	.0899	.1263	.0874	.0189	-.0874	-.1669	-.1859	-.1531	-.0791	0.0000							
7	1	1	0.0000	.0931	.1854	.2523														
		2	0.0000	.0917	.1798	.2353	.2918	.3006	.2788	.2302	.1616	.1817	0.0000							
		3	0.0000	.0907	.1748	.2209	.2577	.2470	.2094	.1549	.0954	.0412	0.0000							
		4	0.0000	.0901	.1704	.2084	.2302	.2066	.1613	.1078	.0587	.0218	0.0000							
		5	0.0000	.0895	.1662	.1971	.2072	.1753	.1265	.0769	.0372	.0120	0.0000							
8	5	1	0.0000	.0953	.1133	.0654														
		2	0.0000	.0944	.1097	.0472	-.0389	-.1225	-.1132	.0054	.1529	.1697	0.0000							
		3	0.0000	.0933	.1011	.0302	-.0574	-.1236	-.0884	.0396	.1638	.1509	0.0000							
		4	0.0000	.0926	.0927	.0146	-.0719	-.1192	-.0613	.0692	.1676	.1317	0.0000							
		5	0.0000	.0911	.0844	.0004	-.0827	-.1104	-.0337	.0933	.1654	.1127	0.0000							
8	3	1	0.0000	.0937	.1519	.1507														
		2	0.0000	.0924	.1434	.1285	.0866	.0214	-.1351	-.2083	-.2031	-.1114	0.0000							
		3	0.0000	.0912	.1352	.1080	.0511	-.0589	-.1565	-.2003	-.1706	-.0822	0.0000							
		4	0.0000	.0903	.1273	.0893	.0209	-.0865	-.1559	-.1843	-.1391	-.0592	0.0000							
		5	0.0000	.0888	.1197	.0722	-.0045	-.1359	-.1668	-.1646	-.1111	-.0420	0.0000							
8	1	1	0.0000	.0927	.1821	.2620														
		2	0.0000	.0910	.1768	.2264	.2702	.2645	.2283	.1699	.1014	.0778	0.0000							
		3	0.0000	.0903	.1720	.2129	.2399	.2193	.1739	.1168	.0617	.0369	0.0000							
		4	0.0000	.0897	.1677	.2008	.2148	.1843	.1360	.0822	.0387	.0109	0.0000							
		5	0.0000	.0891	.1636	.1900	.1936	.1564	.1062	.0590	.0248	.0061	0.0000							



Table 2a. Prolate radial spheroidal functions  $X_0^{(+)}(n, n, c; \xi)$

$n$	$c$	1.0	1.2	1.4	1.6	1.8	2.0	2.2	2.4	2.6	2.8	3.0
0	1 0 0 0	1.000	.603	.519	.450	.326	.223	.147	.093	.059	.033	.016
0	1 0 0 0	1.000	.644	.517	.410	.316	.250	.201	.169	.146	.122	.100
0	1 0 0 0	1.000	.517	.237	.096	.035	.011	.003	.001	.000	.000	.000
1	0 0 0 0	0.000	.532	.606	.573	.488	.386	.287	.202	.135	.085	.052
1	0 0 0 0	0.000	.427	.375	.262	.159	.086	.042	.019	.004	.000	.000
1	0 0 0 0	0.000	.343	.232	.120	.052	.019	.006	.002	.000	.000	.000
2	0 0 0 0	0.000	.353	.594	.715	.731	.669	.563	.441	.323	.224	.147
2	0 0 0 0	0.000	.283	.360	.328	.238	.149	.083	.041	.010	.000	.000
2	0 0 0 0	0.000	.227	.227	.150	.078	.033	.012	.004	.001	.000	.000
3	0 0 0 0	0.000	.234	.502	.693	1.094	1.359	1.103	.961	.776	.585	.414
3	0 0 0 0	0.000	.150	.360	.409	.357	.259	.162	.089	.044	.019	.000
3	0 0 0 0	0.000	.151	.223	.188	.116	.058	.024	.008	.002	.001	.000
4	0 0 0 0	0.000	.152	.416	1.115	1.637	2.008	2.162	2.097	1.862	1.530	1.172
4	0 0 0 0	0.000	.100	.216	.234	.174	.100	.046	.010	.005	.002	.000
5	0 0 0 0	0.000	.103	.346	1.193	2.450	3.478	4.236	4.575	4.470	4.003	3.315
5	0 0 0 0	0.000	.056	.214	.293	.261	.173	.091	.039	.014	.004	.001
6	0 0 0 0	0.000	.055	.339	1.248	3.667	6.325	8.304	9.982	10.728	10.460	9.370
6	0 0 0 0	0.000	.044	.210	.366	1.197	2.300	3.177	3.924	4.602	5.342	6.172
7	0 0 0 0	0.000	.045	.336	1.245	3.660	6.320	8.300	9.980	10.720	10.460	9.370
7	0 0 0 0	0.000	.029	.285	.457	1.296	2.520	3.590	4.517	5.345	6.172	7.172
8	0 0 0 0	0.000	.030	.325	1.245	3.660	6.320	8.300	9.980	10.720	10.460	9.370
8	0 0 0 0	0.000	.024	.225	.425	1.245	2.520	3.590	4.517	5.345	6.172	7.172
8	0 0 0 0	0.000	.019	.201	.378	1.245	2.520	3.590	4.517	5.345	6.172	7.172
9	0 0 0 0	0.000	.028	.315	1.245	3.660	6.320	8.300	9.980	10.720	10.460	9.370
9	0 0 0 0	0.000	.016	.249	1.245	3.660	6.320	8.300	9.980	10.720	10.460	9.370
9	0 0 0 0	0.000	.013	.197	1.245	3.660	6.320	8.300	9.980	10.720	10.460	9.370

Table 2b. Prolate radial spheroidal functions  $X_0^{(-)}(n, n-1, c; \xi)$

$n$	$c$	1.0	1.2	1.4	1.6	1.8	2.0	2.2	2.4	2.6	2.8	3.0
1	1 0 0 0	1.000	.563	.666	.733	.807	.846	.823	.722	.546	.322	.146
1	1 0 0 0	1.000	.673	.836	.932	1.022	1.000	.947	.821	.600	.322	.146
1	1 0 0 0	1.000	.620	.832	.954	1.063	1.022	.907	.722	.500	.280	.155
2	0 0 0 0	0.000	.639	.849	.946	.979	.773	.632	.485	.350	.280	.155
2	0 0 0 0	0.000	.513	.625	.680	.628	.472	.314	.245	.201	.180	.083
2	0 0 0 0	0.000	.411	.493	.519	.408	.286	.193	.145	.101	.080	.030
3	0 0 0 0	0.000	.424	.632	1.174	1.315	1.339	1.239	1.057	.847	.637	.440
3	0 0 0 0	0.000	.273	.318	.240	.140	.067	.027	.009	.003	.001	.000
4	0 0 0 0	0.000	.281	.515	1.429	1.969	2.319	2.427	2.307	2.018	1.639	1.243
4	0 0 0 0	0.000	.226	.304	.255	.162	.082	.035	.013	.006	.002	.000
4	0 0 0 0	0.000	.151	.212	.180	.115	.057	.020	.006	.002	.000	.000
5	0 0 0 0	0.000	.186	.438	1.285	2.047	4.016	6.755	5.033	4.842	4.285	3.517
5	0 0 0 0	0.000	.120	.306	.315	.206	.106	.037	.015	.005	.001	.000
6	0 0 0 0	0.000	.124	.384	1.029	1.438	1.552	1.366	1.116	1.120	1.120	1.243
6	0 0 0 0	0.000	.080	.300	.448	1.029	1.346	1.200	1.094	.837	.602	.403
7	0 0 0 0	0.000	.082	.466	1.276	1.604	12.049	18.263	23.956	27.892	29.312	28.133
7	0 0 0 0	0.000	.053	.393	.585	1.029	1.600	1.393	1.205	1.088	.831	.609
8	0 0 0 0	0.000	.054	.451	1.478	1.979	20.870	35.700	52.265	66.940	76.600	79.572
8	0 0 0 0	0.000	.035	.388	.573	1.029	1.600	1.393	1.205	1.088	.831	.609
9	0 0 0 0	0.000	.036	.436	1.344	1.786	36.147	70.130	114.030	160.655	200.491	225.063
9	0 0 0 0	0.000	.029	.355	1.029	1.600	1.393	1.205	1.088	.831	.609	.412
9	0 0 0 0	0.000	.023	.282	.913	1.574	1.000	1.000	1.000	1.000	1.000	1.000
10	0 0 0 0	0.000	.024	.425	1.211	1.600	62.609	137.426	240.784	395.573	524.353	636.573
10	0 0 0 0	0.000	.019	.346	1.029	1.600	1.393	1.205	1.088	.831	.609	.412
10	0 0 0 0	0.000	.015	.276	1.148	1.600	1.393	1.205	1.088	.831	.609	.412

Table 2c. Prolate radial spheroidal functions  $X_k^{(+)}$  (n,n-2,c;ξ)

n	k	1.0	1.2	1.4	1.6	1.8	2.0	2.2	2.4	2.6	2.8	3.0
2	0	1.000	1.255	1.380	1.374	1.262	1.000	.668	.657	.470	.319	.206
2	1	1.000	.980	.496	.819	.369	.227	.119	.057	.025	.010	.000
3	0	1.000	.527	.155	.244	.296	.300	.293	.251	.196	.142	.096
3	1	1.000	.166	.363	.343	.170	.202	.110	.009	.027	.001	.000
4	0	1.000	.858	1.290	1.622	1.774	1.749	1.504	1.332	1.047	.773	.539
4	1	1.000	.510	.479	.726	.504	.379	.225	.119	.057	.024	.000
4	2	1.000	.433	.359	.193	.023	.107	.102	.207	.195	.163	.124
4	3	1.000	.251	.138	.134	.106	.142	.101	.060	.031	.014	.000
5	0	1.000	.528	1.328	1.974	2.579	2.936	3.003	2.807	2.425	1.951	1.478
5	1	1.000	.356	.465	.892	.627	.644	.432	.255	.134	.062	.000
5	2	1.000	.307	.426	.386	.247	.076	.075	.179	.227	.226	.200
5	3	1.000	.204	.135	.119	.083	.121	.109	.076	.045	.023	.010
6	0	1.000	.348	1.198	2.428	3.794	4.992	5.771	6.002	5.701	4.996	4.068
6	1	1.000	.222	.453	1.103	1.818	1.871	.856	.549	.316	.161	.074
6	2	1.000	.211	.455	.577	.538	.370	.122	.077	.272	.323	.338
6	3	1.000	.150	.301	.415	.466	.409	.274	.169	.087	.041	.020
6	4	1.000	.104	.227	.3624	.441	.419	.233	.105	.042	.017	.004
6	5	1.000	.075	.100	.214	.288	.283	.137	.054	.016	.000	.000
6	6	1.000	.075	.100	.214	.288	.283	.137	.054	.016	.000	.000

Table 2d. Prolate radial spheroidal functions  $X_k^{(-)}$  (n,n-3,c;ξ)

n	k	1.0	1.2	1.4	1.6	1.8	2.0	2.2	2.4	2.6	2.8	3.0
3	0	1.000	1.810	2.530	3.022	3.210	3.124	2.800	2.337	1.827	1.345	.934
3	1	1.000	1.486	1.484	1.211	.915	.683	.353	.086	.004	.000	.000
3	2	1.000	.751	.650	.441	.270	.122	.047	.015	.000	.000	.000
4	0	1.000	.894	1.805	2.527	2.910	2.525	.297	.307	.274	.222	.165
4	1	1.000	.549	.478	.358	.218	.111	.046	.016	.005	.001	.000
4	2	1.000	.327	.253	.188	.115	.066	.031	.010	.000	.000	.000
5	0	1.000	1.980	2.827	3.158	3.968	4.411	4.539	4.103	3.515	2.810	2.106
5	1	1.000	1.549	1.376	.974	.615	.344	.142	.051	.023	.009	.003
5	2	1.000	.821	.620	.410	.251	.106	.044	.018	.006	.002	.000
6	0	1.000	1.953	2.933	3.658	5.453	6.978	7.916	8.124	7.646	6.547	5.377
6	1	1.000	1.427	1.210	.771	.542	.323	.158	.064	.022	.007	.002
6	2	1.000	.829	.628	.415	.252	.109	.047	.019	.009	.003	.001
6	3	1.000	.519	.383	.252	.145	.063	.025	.009	.003	.001	.000
7	0	1.000	1.844	2.844	3.651	5.469	7.467	14.680	16.747	17.301	16.378	14.324
7	1	1.000	1.418	1.118	.761	.543	.323	.158	.064	.022	.007	.002
7	2	1.000	.829	.628	.415	.252	.109	.047	.019	.009	.003	.001
7	3	1.000	.519	.383	.252	.145	.063	.025	.009	.003	.001	.000
7	4	1.000	.327	.253	.188	.115	.066	.031	.010	.000	.000	.000
7	5	1.000	.211	.150	.100	.066	.031	.010	.000	.000	.000	.000
7	6	1.000	.173	.128	.083	.058	.029	.012	.005	.002	.001	.000
7	7	1.000	.138	.094	.063	.046	.025	.010	.004	.002	.001	.000

Table 2e. Prolate radial spheroidal functions  $X_k^{(+)}(n, n-4, c; \xi)$

$n$	$k$	$c/\xi$	1.	1.2	1.4	1.6	1.8
4	0	1	1.0	2.837	5.693	7.322	9.051
		2	1.0	2.013	2.693	2.813	2.447
		3	1.0	1.477	1.468	1.116	.684
		4	1.0	1.108	.826	.758	.498
		5	1.0	.848	.477	.194	.059
4	1	1	1.0	1.049	.905	.625	.289
		2	1.0	.519	-.170	-.264	-.317
		3	1.0	.278	-.192	-.331	-.271
		4	1.0	-.019	-.334	-.290	-.153
		5	1.0	-.165	-.353	-.202	-.073
4	2	1	1.0	.288	-.138	-.303	-.279
		2	1.0	-.141	-.339	-.129	.111
		3	1.0	-.335	-.179	-.154	.260
		4	1.0	-.374	.135	.270	.212
		5	1.0	-.325	.192	.263	.128
5	0	1	0.0	1.517	3.745	6.612	9.583
		2	0.0	1.152	2.143	2.769	2.835
		3	0.0	.885	1.245	1.179	.854
		4	0.0	.686	.733	.510	.261
		5	0.0	.536	.436	.223	.081
5	1	1	0.0	.716	.976	.986	.783
		2	0.0	.484	.369	-.107	-.124
		3	0.0	.308	.368	-.127	-.178
		4	0.0	.178	-.066	-.146	-.107
		5	0.0	.093	-.112	-.110	-.052
5	2	1	0.0	.344	.177	-.017	-.139
		2	0.0	.037	-.080	-.043	.043
		3	0.0	-.014	-.106	-.023	.064
		4	0.0	-.050	-.061	.047	.073
		5	0.0	-.076	-.009	.067	.050
6	0	1	0.0	.922	3.241	7.151	12.269
		2	0.0	.716	1.910	3.097	3.761
		3	0.0	.559	1.136	1.354	1.165
		4	0.0	.439	.680	.597	.364
		5	0.0	.346	.410	.265	.115
6	1	1	0.0	.482	1.001	1.366	1.942
		2	0.0	.343	.552	.310	.055
		3	0.0	.234	.165	-.012	-.127
		4	0.0	.159	.132	-.081	-.092
		5	0.0	.101	-.127	-.073	-.047
6	2	1	0.0	.266	.293	-.171	.007
		2	0.0	.147	.134	-.069	-.074
		3	0.0	.071	-.040	-.046	.009
		4	0.0	-.024	-.044	-.002	.133
		5	0.0	-.003	-.026	.020	.027
7	0	1	0.0	.583	2.158	5.216	16.758
		2	0.0	.457	1.770	3.519	5.234
		3	0.0	.360	1.165	1.316	1.646
		4	0.0	.285	.644	.521	.921
		5	0.0	.225	.391	.320	.166
7	1	1	0.0	.323	1.009	1.809	2.409
		2	0.0	.236	.494	.517	.293
		3	0.0	.170	.222	.087	-.074
		4	0.0	.123	.083	-.032	-.082
		5	0.0	.083	.017	-.049	-.046
7	2	1	0.0	.189	.350	.351	.210
		2	0.0	.113	.098	-.009	-.073
		3	0.0	.069	.004	-.042	-.018
		4	0.0	.037	-.021	-.017	.014
		5	0.0	.017	-.026	.002	.017

2.0	2.2	2.4	2.6	2.8	3.0
9.965	9.968	9.173	7.833	6.246	4.672
1.429	1.196	.692	.358	.166	.066
.847	.148	.054	.017	.005	.001
.068	.019	.004	.001	.000	.000
.014	.003	.000	.000	.000	.000
-.022	-.257	-.391	-.434	-.407	-.340
-.322	-.248	-.160	-.083	-.043	-.019
-.160	-.075	-.029	-.010	-.003	-.001
-.059	-.018	-.004	-.001	-.000	-.000
-.019	-.004	-.001	-.000	-.000	-.000
-.153	-.005	.116	.186	.207	.192
-.229	.228	.169	.103	.053	.024
-.241	.110	.047	.016	.005	.001
-.189	.034	.009	.000	.000	.000
-.039	.009	.001	.000	.000	.000
12.037	13.488	13.721	12.821	11.995	8.946
2.821	1.779	1.039	.614	.324	.146
.827	.239	.056	.033	.010	.002
.184	.033	.008	.002	.000	.000
.022	.005	.001	.000	.000	.000
-.447	.081	-.231	-.436	-.525	-.518
-.243	-.188	-.120	-.056	-.026	-.012
-.138	-.078	-.035	-.013	-.004	-.001
-.081	-.018	-.005	-.001	-.000	-.000
-.016	-.004	-.001	-.000	-.000	-.000
-.165	-.119	-.039	.039	.095	.120
.046	.091	.090	.066	.040	.020
.081	.057	.029	.012	.004	.001
.046	.019	.006	.001	.000	.000
.019	.005	.001	.000	.000	.000
17.692	22.302	25.155	25.775	24.246	21.102
3.696	3.054	2.178	1.347	.737	.359
.781	.423	.169	.071	.023	.006
.166	.059	.017	.004	.001	.000
.036	.008	.001	.000	.000	.000
1.208	.746	.197	-.300	-.650	-.820
-.160	-.257	-.125	-.115	-.115	-.061
-.138	-.095	-.050	-.021	-.007	-.002
-.055	-.023	-.007	-.002	-.000	-.000
-.018	-.005	-.001	-.000	-.000	-.000
-.115	-.159	-.129	-.057	.023	.085
-.017	.040	.065	.061	.043	.025
.043	.042	.026	.012	.004	.001
.031	.016	.006	.001	.000	.000
.014	.004	.001	.000	.000	.000
27.819	39.526	49.499	55.676	56.981	53.562
5.926	5.521	4.359	2.973	1.770	.931
1.271	.777	.387	.160	.055	.016
.274	.110	.035	.009	.002	.000
.060	.016	.003	.000	.000	.000
2.557	2.173	1.368	.380	-.538	-1.199
-.020	-.252	-.336	-.303	-.212	-.125
-.143	-.125	-.076	-.036	-.014	-.004
-.064	-.032	-.011	-.003	-.001	-.000
-.022	-.007	-.001	-.000	-.000	-.000
.016	-.140	-.205	-.175	-.065	.021
-.056	-.000	.046	.061	.053	.035
.021	.039	.027	.015	.006	.002
.023	.015	.006	.002	.000	.000
.012	.004	.001	.000	.000	.000

Table 2f. Prolate radial spheroidal functions  $X_k^{(-)}(n, n-5, c; \xi)$

n	k	$\Delta k$	$\xi$					$\xi$							
			1.0	1.2	1.4	1.6	1.8	2.0	2.2	2.4	2.6	2.8	3.0		
5	0	1	1.000												
		1	3.641	1.752	1.568	2.609									
		1	2.234	1.560	1.987	7.053									
		1	2.285	2.319	2.568	1.897									
		1	1.651	1.567	1.043	1.522									
5	1	1	1.815	1.720	1.720	1.305									
		1	1.954	1.571	1.086	1.274									
		1	1.535	1.004	1.342	1.342									
		1	2.221	1.260	1.328	1.210									
		1	1.017	1.344	1.250	1.106									
5	2	1	1.548	1.128	1.163	1.288									
		1	1.053	1.313	1.242	1.014									
		1	1.240	1.271	1.049	1.232									
		1	1.353	1.373	1.232	1.236									
		1	1.360	1.112	1.271	1.159									
6	0	1	2.221	6.924	14.586	24.420									
		1	1.655	3.674	5.964	7.350									
		1	1.245	2.195	2.472	2.963									
		1	1.943	1.260	1.039	1.613									
		1	1.723	1.732	1.443	1.185									
6	1	1	1.972	1.687	2.127	2.143									
		1	1.665	1.708	1.419	1.021									
		1	1.441	1.224	1.073	1.226									
		1	1.274	1.002	1.165	1.156									
		1	1.154	1.095	1.140	1.080									
6	2	1	1.465	1.389	1.162	1.055									
		1	1.224	1.016	1.141	1.105									
		1	1.077	1.112	1.066	1.042									
		1	1.018	1.083	1.024	1.079									
		1	1.064	1.036	1.064	1.061									
7	0	1	1.281	5.609	14.574	23.985									
		1	1.934	3.249	6.233	8.708									
		1	1.754	1.899	2.573	2.643									
		1	1.587	1.110	1.157	1.843									
		1	1.458	1.664	1.505	1.250									
7	1	1	1.632	1.629	2.582	3.399									
		1	1.452	1.767	1.717	1.356									
		1	1.313	1.323	1.088	1.137									
		1	1.213	1.102	1.075	1.132									
		1	1.145	1.000	1.090	1.073									
7	2	1	1.353	1.484	1.416	1.206									
		1	1.207	1.111	1.047	1.110									
		1	1.169	1.023	1.068	1.014									
		1	1.043	1.043	1.019	1.032									
		1	1.011	1.037	1.014	1.033									
8	0	1	1.736	1.913	16.120	37.750									
		1	1.610	2.904	6.394	11.600									
		1	1.475	1.724	3.955	3.590									
		1	1.373	1.530	1.543	1.119									
		1	1.297	1.613	1.593	1.351									
8	1	1	1.417	1.586	3.333	5.286									
		1	1.304	1.795	1.828	1.828									
		1	1.224	1.375	1.030	1.030									
		1	1.153	1.197	1.111	1.111									
		1	1.112	1.050	1.054	1.070									
8	2	1	1.237	1.539	1.583	1.584									
		1	1.102	1.480	1.080	1.080									
		1	1.091	1.393	1.069	1.069									
		1	1.054	1.215	1.130	1.130									
		1	1.023	1.023	1.005	1.005									

Table 3a. Oblate angular spheroidal functions  $\tilde{Y}_0(n, n, p; \tilde{\eta})$

$n$	$m$	.0	.1	.2	.3	.4	.5	.6	.7	.8	.9	1.0
0	0	6.065	.6096	.6168	.6344	.6570	.6873	.7261	.7749	.8353	.9094	1.0000
	1	3.679	.3716	.3829	.4025	.4237	.4474	.4741	.5035	.5347	.5677	1.0000
	2	.2231	.2265	.2369	.2554	.2837	.3224	.3629	.4053	.4497	.4962	1.0000
1	0	6.065	.6065	.6063	.6052	.6022	.5952	.5809	.5594	.5312	.4964	0.0000
	1	3.679	.3697	.3752	.3840	.3957	.4091	.4240	.4398	.4566	.4744	0.0000
	2	.2231	.2254	.2321	.2436	.2600	.2812	.3063	.3323	.3596	.3876	0.0000
2	0	6.065	.6035	.5940	.5773	.5519	.5155	.4687	.4122	.3467	.2720	0.0000
	1	3.679	.3673	.3676	.3663	.3626	.3543	.3375	.3127	.2802	.2412	0.0000
	2	.2231	.2242	.2275	.2324	.2383	.2455	.2541	.2633	.2730	.2833	0.0000
3	0	6.065	.6005	.5820	.5508	.5050	.4464	.3748	.2882	.1984	.1064	0.0000
	1	3.679	.3660	.3602	.3494	.3324	.3068	.2700	.2237	.1685	.1159	0.0000
	2	.2231	.2231	.2229	.2217	.2184	.2109	.1960	.1735	.1435	.1072	0.0000
4	0	6.065	.5974	.5703	.5254	.4636	.3866	.2974	.2066	.1153	.0238	0.0000
	1	3.679	.3642	.3529	.3333	.3046	.2657	.2160	.1562	.0974	.0409	0.0000
	2	.2231	.2220	.2218	.2184	.2115	.2026	.1868	.1640	.1352	.1014	0.0000
5	0	6.065	.5914	.5597	.5012	.4242	.3378	.2479	.1579	.0680	.0183	0.0000
	1	3.679	.3604	.3433	.3189	.2832	.2384	.1866	.1294	.0779	.0325	0.0000
	2	.2231	.2209	.2209	.2177	.2124	.2052	.1959	.1847	.1717	.1567	0.0000
6	0	6.065	.5825	.5475	.4781	.3894	.2900	.1904	.0924	.0062	.0000	0.0000
	1	3.679	.3552	.3348	.3033	.2559	.2007	.1482	.0997	.0552	.0143	0.0000
	2	.2231	.2198	.2198	.2166	.2124	.2070	.2004	.1927	.1838	.1735	0.0000
7	0	6.065	.5685	.5316	.4561	.3569	.2511	.1523	.0559	.0025	.0000	0.0000
	1	3.679	.3457	.3204	.2836	.2345	.1726	.1106	.0524	.0117	.0000	0.0000
	2	.2231	.2187	.2187	.2154	.2112	.2059	.2003	.1941	.1875	.1802	0.0000
8	0	6.065	.5566	.5156	.4351	.3271	.2175	.1148	.0234	.0000	.0000	0.0000
	1	3.679	.3359	.3056	.2650	.2141	.1495	.0865	.0315	.0098	.0000	0.0000
	2	.2231	.2176	.2176	.2142	.2100	.2042	.1984	.1927	.1870	.1810	0.0000
9	0	6.065	.5431	.4981	.4150	.2998	.1883	.0975	.0340	.0000	.0000	0.0000
	1	3.679	.3236	.2886	.2430	.1870	.1294	.0708	.0230	.0074	.0000	0.0000
	2	.2231	.2165	.2165	.2131	.2090	.2032	.1975	.1925	.1879	.1834	0.0000

Table 3b. Oblate angular spheroidal functions  $\tilde{Y}_1(n, n-1, p; \tilde{\eta})$

$n$	$m$	.0	.1	.2	.3	.4	.5	.6	.7	.8	.9	1.0
1	1	0.0000	.0610	.1236	.1903	.2628	.3436	.4357	.5424	.6682	.8184	1.0000
	2	0.0000	.0227	.0474	.0766	.1135	.1623	.2297	.3257	.4562	.6268	1.0000
2	0	0.0000	.0607	.1213	.1816	.2409	.2976	.3486	.3874	.4009	.3967	0.0000
	1	0.0000	.0225	.0464	.0731	.1040	.1406	.1838	.2326	.2797	.3250	0.0000
3	0	0.0000	.0603	.1188	.1732	.2208	.2577	.2788	.2766	.2406	.1955	0.0000
	1	0.0000	.0224	.0455	.0697	.0953	.1217	.1470	.1661	.1678	.1286	0.0000
4	0	0.0000	.0600	.1164	.1652	.2023	.2232	.2231	.2076	.1443	.0879	0.0000
	1	0.0000	.0223	.0446	.0665	.0929	.1204	.1470	.1661	.1678	.1286	0.0000
5	0	0.0000	.0597	.1141	.1576	.1854	.1933	.1785	.1411	.0966	.0595	0.0000
	1	0.0000	.0222	.0437	.0634	.0801	.0941	.0941	.0847	.0804	.0524	0.0000
6	0	0.0000	.0594	.1117	.1504	.1709	.1624	.1439	.1006	.0520	.0129	0.0000
	1	0.0000	.0221	.0428	.0605	.0734	.0791	.0753	.0605	.0434	.0117	0.0000
7	0	0.0000	.0591	.1095	.1470	.1598	.1450	.1142	.0720	.0312	.0056	0.0000
	1	0.0000	.0221	.0419	.0577	.0672	.0685	.0614	.0432	.0268	.0046	0.0000
8	0	0.0000	.0589	.1073	.1368	.1428	.1256	.0914	.0514	.0187	.0024	0.0000
	1	0.0000	.0219	.0411	.0551	.0616	.0593	.0482	.0309	.0156	.0020	0.0000
9	0	0.0000	.0586	.1051	.1305	.1308	.1087	.0731	.0367	.0112	.0000	0.0000
	1	0.0000	.0218	.0402	.0525	.0565	.0514	.0385	.0220	.0078	.0000	0.0000
10	0	0.0000	.0583	.1030	.1245	.1199	.0942	.0586	.0262	.0067	.0000	0.0000
	1	0.0000	.0216	.0394	.0501	.0518	.0445	.0306	.0157	.0047	.0000	0.0000

Table 3c. Oblate angular spheroidal functions  $\tilde{Y}_t(n, n-2, p; \bar{\eta})$

n	t	p	$\bar{\eta}$	0.0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1.0
2	0	1	2	3	4	5	6	7	8	9	0	1	0	0
2	0	1	2	3	4	5	6	7	8	9	0	1	0	0
2	2	1	2	3	4	5	6	7	8	9	0	1	0	0
3	0	1	2	3	4	5	6	7	8	9	0	1	0	0
3	2	1	2	3	4	5	6	7	8	9	0	1	0	0
4	0	1	2	3	4	5	6	7	8	9	0	1	0	0
4	2	1	2	3	4	5	6	7	8	9	0	1	0	0
5	0	1	2	3	4	5	6	7	8	9	0	1	0	0
5	2	1	2	3	4	5	6	7	8	9	0	1	0	0
6	0	1	2	3	4	5	6	7	8	9	0	1	0	0
6	2	1	2	3	4	5	6	7	8	9	0	1	0	0

Table 3d. Oblate angular spheroidal functions  $\tilde{Y}_t(n, n-3, p; \bar{\eta})$

n	t	p	$\bar{\eta}$	0.0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1.0
3	1	2	3	4	5	6	7	8	9	0	1	0	0	0
3	3	1	2	3	4	5	6	7	8	9	0	1	0	0
4	1	2	3	4	5	6	7	8	9	0	1	0	0	0
4	3	1	2	3	4	5	6	7	8	9	0	1	0	0
5	1	2	3	4	5	6	7	8	9	0	1	0	0	0
5	3	1	2	3	4	5	6	7	8	9	0	1	0	0
6	1	2	3	4	5	6	7	8	9	0	1	0	0	0
6	3	1	2	3	4	5	6	7	8	9	0	1	0	0
7	1	2	3	4	5	6	7	8	9	0	1	0	0	0
7	3	1	2	3	4	5	6	7	8	9	0	1	0	0

Table 3e. Oblate angular spheroidal functions  $\tilde{Y}_t^{(+)}(n, n-4, p; \bar{\eta})$

n	t	p	0.0					0.1					0.2					0.3					0.4					0.5					0.6					0.7					0.8					0.9					1.0				
			0.0	0.1	0.2	0.3	0.4	0.0	0.1	0.2	0.3	0.4	0.0	0.1	0.2	0.3	0.4	0.0	0.1	0.2	0.3	0.4	0.0	0.1	0.2	0.3	0.4	0.0	0.1	0.2	0.3	0.4	0.0	0.1	0.2	0.3	0.4	0.0	0.1	0.2	0.3	0.4	0.0	0.1	0.2	0.3	0.4	0.0	0.1	0.2	0.3	0.4					
4	4	1	.4064	.3755	.2894	.1524	-.0206	.4515	.4234	.3593	.2455	-.0912	.5104	.4935	.4416	.3520	-.2211	.5610	.5511	.5155	.4519	-.3509	.5737	.5684	.5507	.5142	-.4475	-.2059	-.3660	-.4421	-.3438	.0671	1.0000	-.0927	-.2816	-.4238	-.4170	-.0651	1.0000	-.0485	-.1561	-.3555	-.4477	-.1851	1.0000	-.2012	-.0018	-.2419	-.4318	-.0867	1.0000	.3337	.1532	-.1018	-.3732	-.4628	1.0000
4	2	1	-.6424	-.5383	-.6192	-.5857	-.5342	-.5361	-.5624	-.5864	-.5641	-.4288	-.3276	-.3343	-.3864	-.3864	-.2932	-.1766	-.1835	-.2046	-.2410	-.2936	.0934	.0993	-.1167	-.1486	-.1981	-.4541	-.3346	-.1590	.0967	.4668	1.0000	-.5555	-.5177	-.4186	-.2050	-.2148	1.0000	-.4749	-.5097	-.4997	-.4997	-.3730	1.0000	-.3616	-.4368	-.4919	-.4506	-.1162	1.0000	-.2683	-.3587	-.4522	-.4791	-.2159	1.0000
4	0	1	.1603	.1647	.1783	.2022	.2383	.0386	.1411	.0493	.0644	.0832	.0125	.1779	.0183	.0270	.0324	.0047	.0034	.0079	.0129	.0254	.0019	.0033	.0037	.0066	.0125	.2095	.3502	.4563	.5864	.7621	1.0000	.1279	.1877	.2800	.4232	.6470	1.0000	.0667	.1438	.1916	.3273	.5677	1.0000	.1401	.0734	.1368	.2606	.5044	1.0000	.0244	.0468	.0999	.1999	.4912	1.0000
5	4	1	.1196	.1001	.0677	.0111	-.0521	.1173	.1072	.0776	.0318	-.0238	.1183	.1103	.0885	.0523	-.0047	.1217	.1154	.1002	.0725	.0333	.1243	.1203	.1099	.0901	.0596	-.1054	-.1279	-.1972	-.0023	.1489	0.0000	-.0784	-.1150	-.1833	-.0513	.1124	0.0000	-.1462	-.0941	-.1101	-.0611	.0761	0.0000	-.1156	-.0867	-.1008	-.0793	.0464	0.0000	-.0171	-.0349	-.0825	-.0878	.0178	0.0000
5	2	1	-.2381	-.2314	-.2112	-.1767	-.1267	-.2228	-.2207	-.2139	-.2006	-.1778	-.1641	-.1649	-.1669	-.1607	-.1673	-.0999	-.1013	-.1078	-.1169	-.1275	-.0550	-.0571	-.0635	-.0741	-.0887	-.0601	.3228	-.1186	.2151	.2731	0.0000	-.1410	-.0844	-.0825	.1045	.1045	0.0000	-.1577	-.1316	-.1787	.0197	.1499	0.0000	-.1358	-.1341	-.1078	.0340	.0020	0.0000	-.1053	-.1183	-.1140	-.0646	.0649	0.0000
5	0	1	.2448	.2479	.2571	.2723	.2932	.0595	.1623	.0627	.0834	.1040	.0179	.1133	.0238	.0461	.0634	.0064	.0071	.0097	.0146	.0234	.0025	.0029	.0043	.0072	.0127	.3189	.3472	.3726	.3832	.3460	0.0000	.1331	.1717	.2192	.2686	.2894	0.0000	.0676	.0997	.1495	.2039	.2517	0.0000	.0382	.0628	.1023	.1604	.2207	0.0000	.0228	.0413	.0740	.1285	.1986	0.0000
6	4	1	.0552	.1467	.0233	-.0086	-.0396	.0498	.0436	.0261	.0007	-.0264	.0461	.0418	.0285	.0087	-.0146	.0437	.0418	.0305	.0157	-.0088	.0423	.0401	.0343	.0218	.0080	-.0575	-.0511	-.0144	.0435	.0820	0.0000	-.0467	-.0498	-.0261	.0238	.0690	0.0000	-.0355	-.0452	-.0329	.0079	.0568	0.0000	-.0240	-.0381	-.0354	-.0043	.0454	0.0000	-.0126	-.0293	-.0344	-.0134	.0349	0.0000
6	2	1	-.1327	-.1259	-.1059	-.0731	-.0285	-.1163	-.1133	-.1034	-.0864	-.0610	-.0956	-.0947	-.0915	-.0851	-.0748	-.0667	-.0670	-.0677	-.0680	-.0661	-.0405	-.0413	-.0437	-.0478	-.0504	-.0236	.0794	.1285	.1540	.1271	0.0000	-.0544	-.0470	-.0163	.0627	.1066	0.0000	-.0593	-.0435	-.0137	.0304	.0863	0.0000	-.0516	-.0465	-.0285	.0086	.0528	0.0000						
6	0	1	.3176	.3135	.3211	.3244	.3269	.0895	.1916	.0979	.1085	.1231	.0263	.1277	.0321	.0398	.0516	.0089	.0097	.0122	.0170	.0249	.0034	.0039	.0052	.0081	.0131	.3258	.3170	.2936	.2452	.1556	0.0000	.1449	.1596	.1739	.1720	.1301	0.0000	.0680	.0889	.1119	.1279	.1120	0.0000	.0369	.0544	.0770	.0994	.0985	0.0000	.0215	.0351	.0551	.0790	.0876	0.0000
7	4	1	.0313	.1253	.0090	-.0146	-.0283	.0266	.0222	.0103	.0057	-.0263	.0231	.1250	.0113	.0011	-.0133	.0205	.1193	.0120	.0024	-.0084	.0187	.1171	.0126	.0053	-.0034	-.0326	-.1191	.0097	.0386	.0394	0.0000	-.0276	-.0210	-.0004	.0274	.0343	0.0000	-.0223	-.0269	-.0060	.0182	.0295	0.0000	-.0172	-.0193	-.0099	.0107	.0251	0.0000	-.0122	-.0167	-.0119	.0048	.0210	0.0000
7	2	1	-.0904	-.0836	-.0638	-.0329	-.0060	-.0714	-.0674	-.0575	-.0402	-.0166	-.0587	-.0587	-.0522	-.0434	-.0336	-.0450	-.0450	-.0430	-.0436	-.0436	-.0304	-.0304	-.0308	-.0308	-.0308	.0474	.0837	.1048	.0987	.0569	0.0000	-.0119	.0419	.0664	.0738	.0493	0.0000	-.0113	.0119	.0363	.0522	.0419	0.0000	-.0230	-.0069	.0142	.0341	.0349	0.0000	-.0250	-.0156	.0004	.0204	.0287	0.0000
7	0	1	.3700	.3634	.3633	.3536	.3376	.1229	.2241	.1336	.1408	.1489	.0384	.1334	.0415	.0500	.0599	.0126	.1114	.0159	.0203	.0271	.0046	.0055	.0065	.0092	.0137	.3127	.2758	.2234	.1535	.0693	0.0000	.1458	.1465	.1370	.1099	.0384	0.0000	.0698	.0805	.0870	.0809	.0500	0.0000	.0364	.0477	.0586	.0619	.0437	0.0000	.0206	.0301	.0412	.0488	.0387	0.0000





Table 4a. Oblate radial spheroidal functions  $\tilde{X}_0^{(+)}(n, n, p; \xi)$

$n$	$p \backslash \xi$	0.0	.3	.6	.9	1.2	1.5	1.8	2.1	2.4	2.7	3.0
0	1.000	.956	.835	.667	.487	.325	.198	.110	.056	.026	.011	.000
	1.000	.914	.805	.637	.467	.305	.178	.090	.046	.019	.007	.000
	1.000	.874	.783	.617	.447	.285	.158	.070	.032	.013	.003	.000
1	1.000	.998	.974	.937	.897	.850	.807	.766	.726	.687	.649	.611
	1.000	.974	.964	.930	.891	.844	.801	.760	.720	.681	.642	.603
	1.000	.952	.952	.918	.879	.832	.789	.748	.708	.669	.630	.591
2	1.000	1.042	1.136	1.207	1.253	1.290	1.320	1.343	1.359	1.367	1.371	1.371
	1.000	.996	.993	.987	.981	.975	.969	.963	.957	.951	.945	.939
	1.000	.952	.952	.918	.879	.832	.789	.748	.708	.669	.630	.591
3	1.000	1.088	1.225	1.324	1.383	1.420	1.443	1.452	1.457	1.459	1.460	1.460
	1.000	1.040	1.187	1.283	1.342	1.379	1.402	1.411	1.415	1.416	1.416	1.416
	1.000	.994	.994	.959	.920	.873	.826	.780	.734	.688	.642	.596
4	1.000	1.136	1.316	1.445	1.504	1.531	1.546	1.550	1.550	1.550	1.550	1.550
	1.000	1.088	1.287	1.436	1.495	1.522	1.537	1.541	1.541	1.541	1.541	1.541
	1.000	1.040	1.257	1.424	1.483	1.510	1.525	1.529	1.530	1.530	1.530	1.530
5	1.000	1.186	1.404	1.582	1.681	1.718	1.733	1.737	1.737	1.737	1.737	1.737
	1.000	1.134	1.374	1.571	1.670	1.707	1.722	1.726	1.726	1.726	1.726	1.726
	1.000	1.084	1.357	1.574	1.673	1.710	1.725	1.729	1.729	1.729	1.729	1.729
6	1.000	1.238	1.494	1.711	1.810	1.847	1.862	1.866	1.866	1.866	1.866	1.866
	1.000	1.186	1.477	1.704	1.803	1.840	1.855	1.859	1.859	1.859	1.859	1.859
	1.000	1.134	1.447	1.684	1.783	1.820	1.835	1.839	1.839	1.839	1.839	1.839
7	1.000	1.293	1.579	1.826	1.925	1.962	1.966	1.966	1.966	1.966	1.966	1.966
	1.000	1.238	1.550	1.807	1.906	1.943	1.958	1.962	1.962	1.962	1.962	1.962
	1.000	1.186	1.483	1.740	1.839	1.876	1.891	1.895	1.895	1.895	1.895	1.895
8	1.000	1.349	1.667	1.934	2.033	2.070	2.074	2.074	2.074	2.074	2.074	2.074
	1.000	1.293	1.609	1.894	1.993	2.030	2.045	2.049	2.049	2.049	2.049	2.049
	1.000	1.238	1.550	1.826	1.925	1.962	1.977	1.981	1.981	1.981	1.981	1.981
9	1.000	1.409	1.767	2.063	2.162	2.199	2.203	2.203	2.203	2.203	2.203	2.203
	1.000	1.349	1.667	1.963	2.062	2.100	2.115	2.119	2.119	2.119	2.119	2.119
	1.000	1.293	1.609	1.894	1.993	2.030	2.045	2.049	2.049	2.049	2.049	2.049

Table 4b. Oblate radial spheroidal functions  $\tilde{X}_0^{(-)}(n, n-1, p; \xi)$

$n$	$p \backslash \xi$	0.0	.3	.6	.9	1.2	1.5	1.8	2.1	2.4	2.7	3.0
1	1.000	.297	.501	.600	.657	.684	.700	.715	.722	.726	.727	.727
	1.000	.262	.459	.567	.624	.651	.666	.679	.685	.687	.687	.687
	1.000	.226	.404	.512	.569	.600	.615	.628	.635	.637	.637	.637
2	1.000	.299	.584	.688	.745	.772	.787	.799	.807	.811	.811	.811
	1.000	.274	.480	.584	.641	.668	.683	.695	.702	.705	.705	.705
	1.000	.249	.444	.548	.605	.632	.647	.659	.666	.668	.668	.668
3	1.000	.313	.602	.705	.762	.789	.804	.816	.823	.826	.826	.826
	1.000	.286	.492	.596	.653	.680	.695	.707	.714	.717	.717	.717
	1.000	.266	.462	.566	.623	.650	.665	.677	.684	.687	.687	.687
4	1.000	.326	.615	.718	.775	.802	.817	.829	.835	.837	.837	.837
	1.000	.298	.504	.607	.664	.691	.706	.718	.725	.727	.727	.727
	1.000	.278	.474	.577	.634	.661	.676	.688	.695	.697	.697	.697
5	1.000	.341	.630	.733	.790	.817	.832	.844	.851	.853	.853	.853
	1.000	.312	.518	.621	.678	.705	.720	.732	.739	.741	.741	.741
	1.000	.290	.486	.589	.646	.673	.688	.699	.706	.708	.708	.708
6	1.000	.356	.645	.748	.805	.832	.847	.859	.866	.868	.868	.868
	1.000	.325	.531	.634	.691	.718	.733	.745	.752	.754	.754	.754
	1.000	.303	.509	.612	.669	.696	.711	.723	.730	.732	.732	.732
7	1.000	.371	.660	.763	.820	.847	.862	.874	.881	.883	.883	.883
	1.000	.340	.546	.649	.706	.733	.748	.760	.767	.769	.769	.769
	1.000	.318	.524	.627	.684	.711	.726	.738	.745	.747	.747	.747
8	1.000	.388	.677	.780	.837	.864	.879	.891	.898	.899	.899	.899
	1.000	.357	.563	.666	.723	.750	.765	.777	.784	.786	.786	.786
	1.000	.335	.541	.644	.701	.728	.743	.755	.762	.764	.764	.764
9	1.000	.405	.694	.797	.854	.881	.896	.908	.915	.917	.917	.917
	1.000	.374	.580	.683	.740	.767	.782	.794	.801	.803	.803	.803
	1.000	.352	.558	.661	.718	.745	.760	.772	.779	.781	.781	.781
10	1.000	.423	.712	.815	.872	.899	.914	.926	.933	.935	.935	.935
	1.000	.404	.600	.703	.760	.787	.802	.814	.821	.823	.823	.823
	1.000	.386	.592	.695	.752	.779	.794	.806	.813	.815	.815	.815

Table 4a. Oblate radial spheroidal functions  $\tilde{X}_{n, n-2, p}^{(+)}(\eta, n-2, p; \bar{\xi})$

n	l	λ	0.0	.3	.6	.9	1.2	1.5	1.8	2.1	2.4	2.7	3.0
2	0	1	1.000	1.042	1.437	1.747	1.889	1.786	1.480	1.083	.703	.407	.211
2	0	1	1.000	1.042	1.437	1.747	1.889	1.786	1.480	1.083	.703	.407	.211
2	1	1	1.000	.870	.535	.127	-.244	-.406	-.443	-.376	-.267	-.164	-.089
2	1	1	1.000	.870	.535	.127	-.244	-.406	-.443	-.376	-.267	-.164	-.089
3	0	1	1.000	1.174	2.223	3.486	4.660	5.275	5.110	4.284	3.140	2.028	1.161
3	0	1	1.000	1.174	2.223	3.486	4.660	5.275	5.110	4.284	3.140	2.028	1.161
3	1	1	1.000	.848	.377	-.489	-.846	-.954	-.729	-.379	-.026	.333	.145
3	1	1	1.000	.848	.377	-.489	-.846	-.954	-.729	-.379	-.026	.333	.145
4	0	1	1.000	1.546	3.325	6.461	10.376	13.809	15.444	14.738	12.122	8.697	5.482
4	0	1	1.000	1.546	3.325	6.461	10.376	13.809	15.444	14.738	12.122	8.697	5.482
4	1	1	1.000	1.007	.604	-.473	-.844	-.922	-.732	-.403	-.022	.303	.088
4	1	1	1.000	1.007	.604	-.473	-.844	-.922	-.732	-.403	-.022	.303	.088
5	0	1	1.000	1.800	4.794	11.195	21.230	33.038	42.453	45.496	42.330	33.690	23.352
5	0	1	1.000	1.800	4.794	11.195	21.230	33.038	42.453	45.496	42.330	33.690	23.352
5	1	1	1.000	1.254	.827	-.468	-.829	-.849	-.633	-.295	-.076	.266	.080
5	1	1	1.000	1.254	.827	-.468	-.829	-.849	-.633	-.295	-.076	.266	.080
6	0	1	1.000	2.078	6.671	18.498	41.361	74.543	109.803	134.387	139.753	122.116	93.263
6	0	1	1.000	2.078	6.671	18.498	41.361	74.543	109.803	134.387	139.753	122.116	93.263
6	1	1	1.000	1.414	1.424	1.801	1.992	1.755	1.056	.439	-.641	-1.045	-1.059
6	1	1	1.000	1.414	1.424	1.801	1.992	1.755	1.056	.439	-.641	-1.045	-1.059

Table 4d. Oblate radial spheroidal functions  $\tilde{X}_{n, n-3, p}^{(-)}(\eta, n-3, p; \bar{\xi})$

n	l	λ	0.0	.3	.6	.9	1.2	1.5	1.8	2.1	2.4	2.7	3.0
3	0	1	0.000	.324	.764	1.309	1.810	2.004	2.038	1.728	1.266	.820	.478
3	0	1	0.000	.324	.764	1.309	1.810	2.004	2.038	1.728	1.266	.820	.478
3	1	1	0.000	.292	.508	.539	.369	.197	.071	.018	.003	.000	.000
3	1	1	0.000	.292	.508	.539	.369	.197	.071	.018	.003	.000	.000
4	0	1	0.000	.245	.419	.378	.199	-.034	-.172	-.236	-.220	-.165	-.094
4	0	1	0.000	.245	.419	.378	.199	-.034	-.172	-.236	-.220	-.165	-.094
4	1	1	0.000	.225	.149	-.077	-.179	-.132	-.058	-.017	-.003	-.001	-.000
4	1	1	0.000	.225	.149	-.077	-.179	-.132	-.058	-.017	-.003	-.001	-.000
5	0	1	0.000	.352	1.095	2.116	3.540	4.829	5.487	5.288	4.386	3.164	2.002
5	0	1	0.000	.352	1.095	2.116	3.540	4.829	5.487	5.288	4.386	3.164	2.002
5	1	1	0.000	.323	.797	1.366	1.969	1.913	.922	.520	.219	.073	.000
5	1	1	0.000	.323	.797	1.366	1.969	1.913	.922	.520	.219	.073	.000
5	2	1	0.000	.290	.514	.590	.474	.219	-.059	-.253	-.322	-.298	-.211
5	2	1	0.000	.290	.514	.590	.474	.219	-.059	-.253	-.322	-.298	-.211
5	3	1	0.000	.243	.223	-.007	-.175	-.169	-.068	-.030	-.007	-.001	-.000
5	3	1	0.000	.243	.223	-.007	-.175	-.169	-.068	-.030	-.007	-.001	-.000
6	0	1	0.000	.355	1.312	3.058	6.742	13.888	19.888	15.563	14.501	11.627	8.104
6	0	1	0.000	.355	1.312	3.058	6.742	13.888	19.888	15.563	14.501	11.627	8.104
6	1	1	0.000	.337	.816	1.268	1.810	1.917	.942	.515	.216	.086	.001
6	1	1	0.000	.337	.816	1.268	1.810	1.917	.942	.515	.216	.086	.001
6	2	1	0.000	.305	.618	.660	.497	.266	.051	-.193	-.439	-.512	-.439
6	2	1	0.000	.305	.618	.660	.497	.266	.051	-.193	-.439	-.512	-.439
6	3	1	0.000	.288	.304	.092	-.149	-.289	-.152	-.052	-.014	-.003	-.000
6	3	1	0.000	.288	.304	.092	-.149	-.289	-.152	-.052	-.014	-.003	-.000
7	0	1	0.000	.421	1.713	5.260	12.510	23.447	35.434	44.127	46.120	41.050	31.480
7	0	1	0.000	.421	1.713	5.260	12.510	23.447	35.434	44.127	46.120	41.050	31.480
7	1	1	0.000	.385	1.049	1.954	2.407	1.975	1.088	.422	.114	.022	.003
7	1	1	0.000	.385	1.049	1.954	2.407	1.975	1.088	.422	.114	.022	.003
7	2	1	0.000	.229	.735	1.216	1.560	1.519	.816	.243	-.467	-.867	-.917
7	2	1	0.000	.229	.735	1.216	1.560	1.519	.816	.243	-.467	-.867	-.917
7	3	1	0.000	.277	.393	.225	-.085	-.246	-.197	-.091	-.027	-.006	-.001
7	3	1	0.000	.277	.393	.225	-.085	-.246	-.197	-.091	-.027	-.006	-.001
7	4	1	0.000	.159	2.288	8.084	22.708	49.458	86.005	121.537	148.339	148.548	118.166
7	4	1	0.000	.159	2.288	8.084	22.708	49.458	86.005	121.537	148.339	148.548	118.166
7	5	1	0.000	.125	1.720	5.917	9.963	14.418	15.199	11.126	7.355	3.076	.012
7	5	1	0.000	.125	1.720	5.917	9.963	14.418	15.199	11.126	7.355	3.076	.012
7	6	1	0.000	.335	.689	1.690	2.600	3.135	2.802	1.589	.407	-1.287	-1.094
7	6	1	0.000	.335	.689	1.690	2.600	3.135	2.802	1.589	.407	-1.287	-1.094
7	7	1	0.000	.344	.482	.894	.735	.193	-.346	-.568	-.477	-.336	-.000
7	7	1	0.000	.344	.482	.894	.735	.193	-.346	-.568	-.477	-.336	-.000

Table 4e. Oblate radial spheroidal functions  $\tilde{X}_l^{(+)}(n, n-4, p; \xi)$

n	l	p	0.	.3	.6	.9	1.2
4	0	1	1.	1.699	4.112	8.590	14.465
		2	1.	1.462	2.773	4.365	5.245
		3	1.	1.281	1.909	2.274	1.925
		4	1.	1.151	1.373	1.237	.741
		5	1.	1.058	1.036	.713	.304
4	1	1	1.	1.068	1.180	1.145	.848
		2	1.	.943	.705	-.257	-.203
		3	1.	.815	-.302	-.266	-.506
		4	1.	.669	-.072	-.576	-.520
		5	1.	.513	-.368	-.707	-.415
4	2	1	1.	.767	.220	-.306	-.535
		2	1.	.476	-.440	-.710	-.223
		3	1.	.203	-.781	-.438	.408
		4	1.	-.045	-.864	.031	.726
		5	1.	-.257	-.774	.419	.752
5	0	1	1.	2.155	6.961	18.391	37.836
		2	1.	1.835	4.203	9.253	14.037
		3	1.	1.637	2.505	4.336	5.166
		4	1.	1.377	2.202	2.369	1.910
		5	1.	1.221	1.560	1.379	.728
5	1	1	1.	1.241	1.851	2.464	2.589
		2	1.	1.066	1.098	.800	.177
		3	1.	.937	.631	.061	-.199
		4	1.	.810	.247	-.352	-.504
		5	1.	.669	-.097	-.582	-.448
5	2	1	1.	.887	.562	.417	-.262
		2	1.	.651	-.100	-.583	-.419
		3	1.	.386	-.583	-.594	.142
		4	1.	.132	-.811	-.226	.589
		5	1.	-.096	-.832	.212	.736
6	0	1	1.	2.678	11.016	35.775	88.441
		2	1.	2.279	7.533	18.770	33.147
		3	1.	1.944	5.112	9.711	12.202
		4	1.	1.666	3.451	4.950	4.397
		5	1.	1.444	2.337	2.501	1.555
6	1	1	1.	1.462	2.822	4.562	5.819
		2	1.	1.225	1.605	1.430	-.254
		3	1.	1.053	.906	-.144	-.824
		4	1.	.921	.444	-.614	-.870
		5	1.	.783	.075	-.630	-.705
6	2	1	1.	.967	.775	.245	-.737
		2	1.	.786	.158	-.577	-.1264
		3	1.	.552	-.410	-.370	-.695
		4	1.	.302	-.784	-.243	.016
		5	1.	.063	-.936	-.295	.437
7	0	1	1.	3.280	16.818	66.515	196.604
		2	1.	2.804	11.741	35.385	76.435
		3	1.	2.398	8.149	19.310	29.346
		4	1.	2.053	5.626	10.277	11.236
		5	1.	1.767	3.474	5.435	4.252
7	1	1	1.	1.720	4.257	9.033	14.969
		2	1.	1.432	2.581	3.619	3.183
		3	1.	1.214	1.546	1.248	.147
		4	1.	1.053	.923	-.241	-.473
		5	1.	.923	.489	-.238	-.517
7	2	1	1.	1.032	1.260	.331	-.552
		2	1.	.893	-.533	-.319	-.397
		3	1.	.703	-.001	-.211	-.298
		4	1.	.483	-.453	-.213	.169
		5	1.	.243	-.721	-.255	.542

1.5	1.8	2.1	2.4	2.7	3.0
19.847	22.651	21.900	18.202	13.153	8.335
4.727	3.258	1.745	.735	.247	.066
1.137	.473	.140	.030	.005	.001
.287	.072	.012	.001	.000	.000
.077	.012	.001	.000	.000	.000
.355	-.147	-.484	-.595	-.528	-.340
-.434	-.403	-.251	-.116	-.041	-.012
-.392	-.187	-.060	-.013	-.002	-.000
-.241	-.066	-.012	-.001	-.000	-.000
-.123	-.020	-.002	-.000	-.000	-.000
-.418	-.109	.187	.341	.354	.276
.351	.541	.409	.211	.080	.023
.647	.398	.146	.036	.006	.001
.518	.175	.034	.004	.000	.000
.314	.062	.007	.000	.000	.000
61.762	82.064	90.768	85.074	68.506	47.901
15.096	12.136	7.441	3.530	1.323	.393
3.656	1.777	.604	.146	.025	.007
.388	.261	.049	.006	.000	.000
.222	.039	.004	.000	.000	.000
1.964	.784	-.439	-1.244	-1.477	-1.276
-.393	-.595	-.474	-.261	-.107	-.034
-.460	-.275	-.104	-.027	-.005	-.001
-.296	-.098	-.020	-.003	-.000	-.000
-.161	-.031	-.003	-.000	-.000	-.000
-.406	-.295	-.050	.171	.278	.273
.382	.407	.405	.248	.108	.035
.563	.440	.191	.053	.010	.001
.561	.227	.051	.007	.001	.000
.379	.087	.011	.001	.000	.000
169.394	261.236	329.071	346.714	311.416	239.091
41.963	39.013	27.240	14.563	6.052	1.979
10.182	5.699	2.203	.597	.115	.016
2.384	.809	.173	.024	.002	.000
.550	.111	.013	.001	.000	.000
4.964	1.788	-2.518	-6.075	-7.610	-7.086
-1.293	-2.115	-1.888	-1.166	-.526	-.183
-1.159	-.812	-.355	-.064	-.021	-.003
-.634	-.248	-.058	-.008	-.001	-.000
-.312	-.071	-.000	-.001	-.000	-.000
-2.050	-3.322	-4.122	-5.206	-3.638	-2.715
-1.305	-.934	-.405	-.200	-.063	-.015
-.153	-.097	.089	.034	.008	.001
.318	.185	.051	.008	.001	.000
.338	.096	.014	.001	.000	.000
443.612	736.863	1127.303	1337.899	1326.901	1125.214
114.035	122.649	97.557	58.639	27.099	9.761
29.031	18.927	8.357	2.551	.548	.084
7.315	2.890	.708	.113	.011	.001
1.826	.437	.059	.005	.000	.000
14.935	17.659	10.578	.724	-7.564	-11.545
1.124	-1.312	-2.278	-1.871	-1.028	-.413
-.796	-.385	-.494	-1.730	-.043	-.006
-.565	-.283	-.079	-.012	-.001	-.000
-.299	-.033	-.012	-.001	-.000	-.000
.031	-.376	-.467	-.259	.059	.295
-.313	.446	.294	.297	.180	.077
.221	.402	.260	.093	.024	.004
.511	.106	.309	.013	.002	.000
.474	.154	.325	.002	.000	.000

Table 4f. Oblate radial spheroidal functions  $\tilde{X}_l^{(-)}(n, n-5, p; \xi)$

n	l	p	$\xi$					$\xi$					
			0.	.3	.6	.9	1.2	1.5	1.8	2.1	2.4	2.7	3.0
5	0	1	.494	1.471	3.373	3.257		13.562	18.393	20.667	18.645	15.197	10.637
		3	.373	1.132	2.362	3.512		3.831	3.568	1.887	1.399	.337	.100
		5	.345	.384	1.429	1.522		1.087	.631	.181	.347	.068	.001
		7	.323	.709	.880	.674		.318	.194	.018	.002	.000	.000
		9	.355	.561	.552	.304		.395	.017	.002	.000	.000	.000
5	1	1	.315	.685	1.020	1.125		.382	.372	-.172	-.539	-.650	-.566
		3	.221	.485	.439	.426		-.179	-.303	-.254	-.143	-.059	-.019
		5	.267	.328	.117	-.145		-.221	-.145	-.058	-.015	-.003	.000
		7	.241	.262	-.052	-.189		-.133	-.048	-.010	-.001	-.000	.000
		9	.213	.164	-.130	-.155		-.065	-.014	-.002	-.000	-.000	.000
5	2	1	.267	.341	.201	-.029		-.181	-.180	-.068	.061	.137	.147
		3	.227	.145	-.089	-.160		-.033	.101	.130	.088	.046	.014
		5	.139	.313	.147	-.085		.106	.110	.053	.016	.003	.000
		7	.153	.063	-.147	-.068		.175	.023	.013	.002	.000	.000
		9	.127	.161	-.039	.107		.075	.020	.003	.000	.000	.000
5	0	1	.455	2.115	7.165	18.175		35.520	55.188	70.043	74.190	65.679	51.506
		3	.413	1.605	4.796	7.621		3.821	9.236	6.501	3.495	1.458	.473
		5	.381	1.231	2.486	3.233		2.748	1.564	.611	.167	.032	.004
		7	.359	.955	1.493	1.392		.781	.263	.058	.009	.001	.000
		9	.335	.750	.911	.610		.226	.047	.006	.000	.000	.000
6	1	1	.344	.913	1.718	2.424		2.539	1.832	.573	-.662	-1.406	-1.546
		3	.315	.650	1.796	.525		-.016	-.417	-.479	-.356	-.159	-.056
		5	.289	.454	.304	-.062		-.282	-.242	-.116	-.035	-.007	-.001
		7	.264	.302	.042	-.197		-.190	-.083	-.020	-.003	-.000	-.000
		9	.247	.183	-.089	-.186		-.097	-.024	-.003	-.000	-.000	-.000
6	2	1	.281	.446	.403	.171		-.100	-.241	-.198	-.042	.109	.184
		3	.246	.237	-.061	-.174		-.142	.054	.140	.120	.065	.025
		5	.211	.182	-.138	-.093		.077	.127	.075	.327	.006	.001
		7	.179	-.023	-.134	.330		.120	.072	.021	.003	.000	.000
		9	.147	-.180	-.076	.196		.391	.029	.004	.000	.000	.000
7	0	1	.517	2.987	12.483	38.211		48.187	158.777	229.805	273.882	273.872	233.150
		3	.477	2.254	7.282	15.984		24.354	26.560	21.328	12.906	5.993	2.167
		5	.443	1.712	4.277	6.729		6.767	4.470	1.991	.612	.132	.020
		7	.409	1.311	2.534	2.859		1.398	.759	.103	.029	.003	.000
		9	.377	1.114	1.519	1.229		.539	.130	.018	.001	.000	.000
7	1	1	.377	1.211	2.921	4.931		6.463	6.197	3.848	.422	-2.531	-3.998
		3	.347	.864	1.353	1.293		-.481	-.471	-.899	-.758	-.423	-.172
		5	.321	.612	.596	.133		-.334	-.411	-.238	-.085	-.020	-.003
		7	.289	.423	.191	-.180		-.273	-.147	-.042	-.007	-.001	-.000
		9	.263	.277	-.018	-.216		-.147	-.643	-.307	-.001	-.000	-.000
7	2	1	.291	.557	.560	.509		.132	-.221	-.353	-.233	.009	.205
		3	.265	.436	.431	-.141		-.191	-.023	.135	.161	.104	.046
		5	.237	.161	-.098	-.147		.329	.136	.103	.042	.011	.002
		7	.207	.135	-.148	-.120		.123	.033	.032	.006	.001	.000
		9	.183	-.146	-.111	.073		.107	.041	.007	.001	.000	.000
8	0	1	.647	3.151	21.444	77.486		211.123	436.366	719.616	963.493	1070.726	1003.741
		3	.617	2.427	12.350	32.309		34.264	73.452	67.417	45.682	23.572	9.386
		5	.588	1.866	7.238	13.680		16.204	12.378	6.980	2.169	.823	.088
		7	.555	1.399	4.264	5.785		4.526	2.935	.500	.103	.012	.001
		9	.511	1.173	2.531	2.464		1.273	.757	.056	.005	.000	.000
8	1	1	.410	1.592	4.621	9.664		15.300	18.181	15.380	7.380	-2.212	-4.218
		3	.377	1.141	3.359	2.309		1.836	-.145	-.158	-1.753	-1.151	-.530
		5	.347	.814	1.958	.556		-.116	-.595	-.902	-.204	-.056	-.010
		7	.317	.574	.426	-.106		-.389	-.267	-.351	-.018	-.002	-.000
		9	.291	.393	.197	-.240		-.223	-.080	-.014	-.001	-.000	-.000
8	2	1	.311	.677	.394	1.333		.653	.721	-.477	-.359	-.244	.141
		3	.274	.443	.313	-.039		-.254	-.146	.058	.203	.123	.087
		5	.237	.251	-.023	-.186		-.141	.132	.067	.007	.000	.004
		7	.207	.104	-.140	-.186		.106	.117	.048	.010	.001	.000
		9	.183	-.001	-.078	.139		.121	.057	.012	.001	.000	.000

Table 5a. Eigenvalues of the separation constant  $\Lambda_0(n, n-2, c) - c$

c \ n	2	3	4	5	6
.00	0.0000	2.0000	6.0000	12.0000	20.0000
.20	.2441	.1523	6.1039	12.1745	20.0770
.40	.4474	.2323	6.2079	12.3481	20.1544
.60	.6167	.2903	6.3119	12.5217	20.2318
.80	.7581	.3304	6.4159	12.6953	20.3092
1.00	.8765	.3563	6.5199	12.8689	20.3866
1.20	.9773	.3733	6.6239	13.0425	20.4640
1.40	1.0629	.3824	6.7279	13.2161	20.5414
1.60	1.1364	.3847	6.8319	13.3897	20.6188
1.80	1.2000	.3802	6.9359	13.5633	20.6962
2.00	1.2554	.3697	7.0399	13.7369	20.7736
2.20	1.3041	.3534	7.1439	13.9105	20.8510
2.40	1.3471	.3324	7.2479	14.0841	20.9284
2.60	1.3853	.3076	7.3519	14.2577	21.0058
2.80	1.4195	.2793	7.4559	14.4313	21.0832
3.00	1.4512	.2471	7.5599	14.6049	21.1606
3.20	1.4779	.2114	7.6639	14.7785	21.2380
3.40	1.5030	.1724	7.7679	14.9521	21.3154
3.60	1.5259	.1304	7.8719	15.1257	21.3928
3.80	1.5468	.0864	7.9759	15.2993	21.4702
4.00	1.5661	.0404	8.0799	15.4729	21.5476
4.20	1.5837	.0034	8.1839	15.6465	21.6250
4.40	1.6000	.0000	8.2879	15.8201	21.7024
4.60	1.6151	.0000	8.3919	16.0000	21.7798
4.80	1.6291	.0000	8.4959	16.1736	21.8572
5.00	1.6422	.0000	8.6000	16.3500	21.9346

Table 5b. Eigenvalues of the separation constant  $\Lambda_2(n, n-2, c) - c$

c \ n	2	3	4	5	6
.00	6.0000	12.0000	20.0000	30.0000	42.0000
.20	6.0559	12.6438	20.6911	30.7445	42.7296
.40	6.1526	13.3172	21.3921	31.4854	43.4636
.60	6.2833	14.0000	22.1019	32.2219	44.2017
.80	6.4419	14.6953	22.8195	32.9537	44.9434
1.00	6.6231	15.4031	23.5440	33.6811	45.6886
1.20	6.8227	16.1201	24.2747	34.4049	46.4369
1.40	7.0371	16.8456	25.0109	35.1255	47.1881
1.60	7.2636	17.5783	25.7520	35.8436	47.9419
1.80	7.5000	18.3175	26.4975	36.5595	48.6982
2.00	7.7466	19.0623	27.2470	37.2733	49.4568
2.20	8.0000	19.8119	28.0000	37.9854	50.2176
2.40	8.2599	20.5658	28.7563	38.6959	50.9803
2.60	8.5229	21.3236	29.5155	39.4047	51.7448
2.80	8.7885	22.0847	30.2773	40.1116	52.5110
3.00	9.0549	22.8483	31.0416	40.8164	53.2788
3.20	9.3221	23.6157	31.8081	41.5191	54.0481
3.40	9.5900	24.3843	32.5765	42.2194	54.8188
3.60	9.8584	25.1531	33.3469	42.9174	55.5908
3.80	10.1272	25.9226	34.1189	43.6131	56.3640
4.00	10.3964	26.6927	34.8924	44.3066	57.1384
4.20	10.6660	27.4634	35.6674	45.0000	57.9138
4.40	10.9360	28.2346	36.4438	45.6933	58.6902
4.60	11.2064	29.0063	37.2213	46.3866	59.4676
4.80	11.4771	29.7785	38.0000	47.0800	60.2459
5.00	11.7481	30.6015	38.7737	47.7733	61.0250

$\{\Lambda_0(n, n-2, c) - c\}/c$

(1/c) \ n	2	3	4	5	6
.20	.3284	.6797	1.4444	2.6167	4.1950
.19	.3150	.6530	1.3706	2.4902	3.9902
.18	.3013	.6133	1.3089	2.3647	3.7853
.17	.2874	.5835	1.2408	2.2382	3.5799
.16	.2731	.5533	1.1724	2.1114	3.3743
.15	.2585	.5226	1.1035	1.9842	3.1683
.14	.2437	.4914	1.0343	1.8566	2.9619
.13	.2285	.4604	.9645	1.7285	2.7551
.12	.2131	.4294	.8944	1.6000	2.5479
.11	.1972	.3984	.8237	1.4710	2.3401
.10	.1810	.3675	.7525	1.3414	2.1318
.09	.1646	.3366	.6818	1.2122	1.9230
.08	.1477	.3057	.6108	1.0833	1.7137
.07	.1306	.2748	.5391	.9547	1.5039
.06	.1130	.2439	.4673	.8263	1.2938
.05	.0951	.2130	.3957	.6983	1.0837
.04	.0769	.1821	.3243	.5708	.8735
.03	.0582	.1512	.2530	.4435	.6634
.02	.0392	.1203	.1817	.3162	.4532
.01	.0198	.0894	.1104	.1892	.2430
.00	.0000	.0000	.0000	.0000	.0000

$\{\Lambda_2(n, n-2, c) - c\}/c$

(1/c) \ n	2	3	4	5	6
.20	.8716	6.1203	7.7559	9.7833	12.2050
.19	.8250	6.0100	7.5634	9.4882	11.7898
.18	.7787	5.9001	7.3711	9.1953	11.3748
.17	.7326	5.7903	7.1792	8.9018	10.9601
.16	.6869	5.6812	6.9876	8.6086	10.5457
.15	.6415	5.5724	6.7959	8.3158	10.1317
.14	.5963	5.4633	6.6043	8.0234	9.7181
.13	.5515	5.3533	6.4127	7.7315	9.3049
.12	.5070	5.2433	6.2213	7.4400	8.8921
.11	.4628	5.1342	6.0300	7.1490	8.4799
.10	.4190	5.0245	5.8385	6.8575	8.0682
.09	.3754	4.9145	5.6471	6.5660	7.6574
.08	.3320	4.8043	5.4557	6.2749	7.2467
.07	.2887	4.6943	5.2643	5.9833	6.8370
.06	.2457	4.5840	5.0728	5.6913	6.4282
.05	.2029	4.4735	4.8813	5.3987	6.0203
.04	.1604	4.3628	4.6898	5.1061	5.6135
.03	.1181	4.2519	4.4983	4.8135	5.2079
.02	.0760	4.1409	4.3068	4.5209	4.8037
.01	.0342	4.0300	4.1154	4.2283	4.4000
.00	.0000	4.0000	4.0000	4.0000	4.0000

Table 5c. Eigenvalues of the separation constant  $\Lambda_1(n, n-3, c) - c$

c \ n	3	4	5	6	7
.00	2.00000	6.00000	12.00000	20.00000	30.00000
.20	2.86444	6.73133	12.65889	20.61255	30.68033
.40	3.89699	7.44433	13.30227	21.21400	31.35233
.60	4.96699	8.13333	13.93222	21.80552	32.01664
.80	5.26444	8.80000	14.54881	22.38664	32.67330
1.00	5.00000	9.45000	15.15111	22.95884	33.32226
1.20	6.70499	10.08000	15.74222	23.52216	33.96553
1.40	7.78088	10.69000	16.32119	24.07664	34.60117
1.60	8.12997	11.29000	16.89116	24.62335	34.43320
1.80	8.65338	11.88000	17.45001	25.16331	34.95666
2.00	9.25554	12.45000	18.00000	25.69559	35.47558
2.20	9.83668	13.01500	18.54112	26.22221	35.98999
2.40	10.40000	13.56500	19.07444	26.74222	36.49991
2.60	10.94711	14.10200	19.60000	27.25555	37.00337
2.80	11.47999	14.63100	20.11886	27.76553	37.50339
3.00	12.00000	15.15111	20.63007	28.26991	38.00000
3.20	12.50889	15.66222	21.13667	28.76880	38.49222
3.40	13.00777	16.16444	21.63770	29.26225	38.98077
3.60	13.49981	16.66000	22.13220	29.75000	39.46557
3.80	13.98505	17.15000	22.62221	30.23338	39.94773
4.00	14.45600	17.64222	23.10776	30.71222	40.42558
4.20	14.92253	18.12777	23.58887	31.18660	40.90013
4.40	15.38491	18.60666	24.06556	31.65665	41.37400
4.60	15.84300	19.07999	24.53993	32.12333	41.84439
4.80	15.30225	19.54667	25.00992	32.58667	42.31113
5.00	15.75330	20.00000	25.47558	33.04885	42.77663

$\{\Lambda_1(n, n-3, c) - c\}/c$

(1/c) \ n	3	4	5	6	7
.20	3.35006	4.00000	5.00000	6.51667	8.55553
.19	3.29477	3.91433	4.93255	6.40117	8.24331
.18	3.23766	3.82853	4.86756	6.28558	7.93111
.17	3.17944	3.74273	4.80277	6.16990	7.61662
.16	3.12000	3.65693	4.73798	6.05416	7.30114
.15	3.05934	3.57113	4.67319	5.93845	6.98555
.14	2.99766	3.48533	4.60840	5.82275	6.66885
.13	2.93455	3.40000	4.54361	5.70705	6.35222
.12	2.87000	3.31467	4.47882	5.59135	6.03555
.11	2.80444	3.22933	4.41403	5.47565	5.71885
.10	2.73779	3.14400	4.34924	5.36000	5.40222
.09	2.67000	3.05867	4.28445	5.24430	5.08555
.08	2.60111	2.97333	4.21966	5.12860	4.76885
.07	2.53111	2.88800	4.15487	5.01290	4.45222
.06	2.46000	2.80267	4.09008	4.89720	4.13555
.05	2.38447	2.71733	4.02529	4.78150	3.81885
.04	2.31000	2.63200	3.96050	4.66580	3.50222
.03	2.23455	2.54667	3.89571	4.55010	3.18555
.02	2.15776	2.46133	3.83092	4.43440	2.86885
.01	2.07999	2.37600	3.76613	4.31870	2.55222
.00	2.00000	2.29067	3.70134	4.20300	2.23555

Table 5d. Eigenvalues of the separation constant  $\Lambda_2(n, n-3, c) - c$

c \ n	3	4	5	6	7
.00	12.00000	20.00000	30.00000	42.00000	56.00000
.20	12.73356	20.86822	30.94111	42.98875	57.01997
.40	13.50331	21.75833	31.88373	43.98869	58.04777
.60	14.30331	22.66691	32.84678	44.99944	59.08336
.80	15.13556	23.60000	33.82119	46.01136	60.12770
1.00	15.00000	24.54438	34.80889	47.04116	61.17774
1.20	15.89554	25.50000	35.81773	48.08784	62.23447
1.40	16.81992	26.46666	36.83773	49.14116	63.29883
1.60	17.77000	27.44444	37.86773	50.20116	64.36880
1.80	18.74662	28.43333	38.90773	51.26669	65.44434
2.00	20.74446	29.54444	40.00000	52.33881	66.52442
2.20	21.76332	30.66666	41.05333	53.41779	67.60881
2.40	22.80000	31.80000	42.12000	54.50333	68.70000
2.60	23.85229	32.95229	43.20000	55.59333	69.79663
2.80	24.92001	34.12001	44.28000	56.68666	70.89881
3.00	26.00000	34.84889	45.36933	57.78333	72.00000
3.20	27.09111	35.59371	46.46333	58.88333	73.10778
3.40	28.19221	36.35226	47.56333	59.98666	74.21993
3.60	29.30119	37.12500	48.66889	61.09333	75.33443
3.80	30.41995	37.90000	49.77779	62.20333	76.45227
4.00	31.54440	40.35773	50.89334	63.31666	77.57442
4.20	32.67447	41.47773	52.01111	64.43333	78.69887
4.40	33.81009	42.60117	53.13111	65.55333	79.82660
4.60	34.95226	43.73005	54.25333	66.67666	80.95664
4.80	36.09775	44.86333	55.38000	67.80333	82.08887
5.00	37.24770	46.00000	56.52442	68.93665	83.22337

$\{\Lambda_2(n, n-3, c) - c\}/c$

(1/c) \ n	3	4	5	6	7
.20	7.44944	9.20000	11.30000	13.73333	16.64447
.19	7.36533	9.02222	11.10222	13.53833	16.09669
.18	7.28122	8.85000	10.90000	13.34333	15.54999
.17	7.20000	8.67999	10.70000	13.14833	14.99336
.16	7.12000	8.50773	10.50000	12.95333	14.43666
.15	7.04366	8.33889	9.91000	11.76881	13.91445
.14	6.96224	8.16999	9.70000	11.57333	13.37445
.13	6.88555	8.00000	9.50000	11.37833	12.82998
.12	6.80998	7.83555	9.30000	11.18333	12.28666
.11	6.73553	7.67333	9.10000	10.98833	11.74337
.10	6.66221	7.51111	8.90000	10.79333	11.20000
.09	6.59000	7.35000	8.70000	10.59833	10.65666
.08	6.51966	7.19000	8.50000	10.40333	10.11333
.07	6.45000	7.03000	8.30000	10.20833	9.57000
.06	6.38221	6.87111	8.10000	10.01333	9.02666
.05	6.31553	6.71222	7.90000	9.81833	8.48333
.04	6.24998	6.55333	7.70000	9.62333	7.94000
.03	6.18555	6.40000	7.50000	9.42833	7.39666
.02	6.12224	6.24889	7.30000	9.23333	6.85333
.01	6.06000	6.10000	7.10000	9.03833	6.31000
.00	6.00000	6.00000	6.00000	6.00000	6.00000

Table 5e. Eigenvalues of the separation constant  $\{A_0(n, n-4, c) - c\}$

c \ n	4	5	6	7	8
0.00	.0000	2.0000	6.0000	12.0000	20.0000
.20	.4718	2.2954	6.2156	12.4198	20.1403
.40	.8400	2.5480	6.4000	12.8161	20.2703
.60	1.1313	2.7668	6.5806	12.4676	20.3915
.80	1.3664	2.9558	6.7362	12.5989	20.5048
1.00	1.5602	3.1223	6.8774	12.7202	20.6107
1.20	1.7236	3.2702	7.0060	12.8326	20.7102
1.40	1.8623	3.4021	7.1237	12.9372	20.8036
1.60	1.9831	3.5287	7.2318	13.0347	20.8917
1.80	2.0893	3.6513	7.3319	13.1258	20.9746
2.00	2.1835	3.7725	7.4238	13.2111	21.0533
2.20	2.2679	3.8914	7.5095	13.2913	21.1277
2.40	2.3441	4.0087	7.5904	13.3667	21.1982
2.60	2.4133	4.1242	7.6648	13.4379	21.2652
2.80	2.4765	4.2382	7.7339	13.5051	21.3299
3.00	2.5346	4.3507	7.7995	13.5687	21.3897
3.20	2.5881	4.4618	7.8611	13.6290	21.4447
3.40	2.6376	4.5714	7.9194	13.6862	21.4952
3.60	2.6831	4.6794	7.9742	13.7406	21.5417
3.80	2.7256	4.7857	8.0262	13.7925	21.5846
4.00	2.7666	4.8904	8.0754	13.8419	21.6247
4.20	2.8051	4.9933	8.1222	13.8890	21.7012
4.40	2.8414	5.0941	8.1666	13.9341	21.7488
4.60	2.8758	5.1935	8.2090	13.9772	21.7886
4.80	2.9035	5.2911	8.2493	14.0185	21.8296
5.00	2.9334	5.3727	8.2878	14.0581	21.8694

Table 5f. Eigenvalues of the separation constant  $\{A_2(n, n-4, c) - c\}$

c \ n	4	5	6	7	8
0.00	6.0000	12.0000	20.0000	30.0000	42.0000
.20	7.0004	13.0264	22.0138	30.9923	42.9742
.40	8.0773	14.0733	22.0294	31.9853	43.9471
.60	9.2035	15.1335	23.0495	32.9775	44.9181
.80	10.3579	16.1995	24.0639	33.9679	45.8866
1.00	11.5253	17.2672	25.0836	34.9556	46.8522
1.20	12.6946	18.3329	26.1142	35.9400	47.8146
1.40	13.8589	19.3933	27.1154	36.9205	48.7735
1.60	15.0123	20.4483	28.1215	37.8966	49.7287
1.80	16.1515	21.4947	29.1218	38.8682	50.6801
2.00	17.2741	22.5322	30.1159	39.8350	51.6276
2.20	18.3786	23.5600	31.1133	40.7968	52.5711
2.40	19.4643	24.5780	32.0885	41.7537	53.5107
2.60	20.5316	25.5853	33.0538	42.7056	54.4462
2.80	21.5789	26.5837	34.0264	43.6525	55.3779
3.00	22.6086	27.5716	34.9874	44.5935	56.3056
3.20	23.6209	28.5433	35.9449	45.5281	57.2235
3.40	24.6167	29.5133	36.8930	46.4564	58.1346
3.60	25.5971	30.4783	37.8319	47.3791	59.0361
3.80	26.5631	31.4333	38.7679	48.2951	59.9299
4.00	27.5159	32.3716	39.6982	49.2033	60.8883
4.20	28.4555	33.3001	40.6189	50.1038	61.7947
4.40	29.3828	34.2147	41.5274	51.0064	62.6969
4.60	30.3050	35.1155	42.4235	51.9111	63.5963
4.80	31.2148	36.0033	43.3080	52.8178	64.4927
5.00	32.1162	36.8813	44.2737	53.7265	65.3850

$\{A_0(n, n-4, c) - c\}/c$

(1/c) \ n	4	5	6	7	8
.20	.5867	.9145	1.6576	2.8116	4.3739
.19	.5843	.8772	1.5838	2.6805	4.1647
.18	.5814	.8393	1.5095	2.5488	3.9550
.17	.5779	.8008	1.4346	2.4165	3.7447
.16	.4939	.7617	1.3590	2.2837	3.5339
.15	.4693	.7218	1.2828	2.1501	3.3225
.14	.4440	.6813	1.2057	2.0158	3.1103
.13	.4181	.6400	1.1279	1.8807	2.8974
.12	.3915	.5973	1.0493	1.7448	2.6836
.11	.3642	.5548	.9697	1.6079	2.4690
.10	.3361	.5103	.8891	1.4700	2.2533
.09	.3072	.4653	.8073	1.3310	2.0364
.08	.2774	.4193	.7244	1.1907	1.8183
.07	.2467	.3723	.6402	1.0490	1.5988
.06	.2150	.3243	.5546	.9057	1.3776
.05	.1822	.2745	.4673	.7607	1.1546
.04	.1483	.2231	.3783	.6137	.9295
.03	.1133	.1700	.2873	.4645	.7013
.02	.0770	.1134	.1941	.3128	.4715
.01	.0392	.0533	.1085	.1581	.2377
.00	.0000	.0000	.0000	.0000	.0000

$\{A_2(n, n-4, c) - c\}/c$

(1/c) \ n	4	5	6	7	8
.20	6.4232	7.3964	8.8541	10.7535	13.0772
.19	6.3252	7.2522	8.6384	10.4396	12.6458
.18	6.2247	7.1057	8.4171	10.1244	12.2135
.17	6.1216	6.9574	8.1961	9.8079	11.7799
.16	6.0159	6.8063	7.9733	9.4899	11.3452
.15	5.9076	6.6533	7.7486	9.1703	10.9099
.14	5.7967	6.4934	7.5216	8.8497	10.4712
.13	5.6833	6.3373	7.2923	8.5252	10.0316
.12	5.5669	6.1733	7.0605	8.1993	9.5910
.11	5.4481	6.0155	6.8258	7.8719	9.1461
.10	5.3268	5.8435	6.5881	7.5397	8.6936
.09	5.2036	5.6731	6.3472	7.2053	8.2502
.08	5.0788	5.5037	6.1026	6.8675	7.7975
.07	4.9485	5.3293	5.8546	6.5259	7.3411
.06	4.8180	5.1492	5.6026	6.1802	6.8805
.05	4.6855	4.9647	5.3463	5.8299	6.4152
.04	4.5513	4.7731	5.0819	5.4748	5.9446
.03	4.4154	4.5779	4.8114	5.1144	5.4683
.02	4.2781	4.3793	4.5417	4.7486	4.9857
.01	4.1396	4.1793	4.2700	4.3772	4.4964
.00	4.0000	4.0000	4.0000	4.0000	4.0000

Table 5g. Eigenvalues of the separation constant  $\{\Lambda_4(n, n-4, c) - c\}$

c \ n	4	5	6	7	8
0.00	20.00000	36.00000	42.00000	56.00000	72.00000
0.20	20.00000	36.00000	42.00000	56.00000	72.00000
0.40	20.00000	36.00000	42.00000	56.00000	72.00000
0.60	20.00000	36.00000	42.00000	56.00000	72.00000
0.80	20.00000	36.00000	42.00000	56.00000	72.00000
1.00	24.91455	35.61133	48.03340	62.3241	78.5370
1.20	25.98222	35.79633	49.28998	63.6273	79.8752
1.40	27.07888	38.00000	50.56009	64.9423	81.2229
1.60	28.20466	39.23333	51.84667	66.2687	82.5796
1.80	29.35922	46.47777	53.14667	67.6161	83.9451
2.00	30.54244	41.74222	54.46003	68.9539	85.3191
2.20	31.75335	43.02222	55.78669	70.3119	86.7012
2.40	32.99166	44.32222	57.12660	71.6795	88.0911
2.60	34.25577	45.64444	58.47772	73.0565	89.4885
2.80	35.54466	46.97444	59.83977	74.4424	90.8932
3.00	36.85669	48.32222	61.21322	75.8368	92.3047
3.20	38.19100	49.68888	62.59770	77.2394	93.7229
3.40	39.54577	51.05555	63.99077	78.6497	95.1475
3.60	40.91933	52.42222	65.39339	80.0575	96.5782
3.80	42.31044	53.84444	66.80559	81.4925	98.0148
4.00	43.71755	55.26222	68.22664	82.9224	99.4570
4.20	45.13994	56.68888	69.66550	84.3624	100.9045
4.40	46.57748	58.10000	71.10911	85.8068	102.3573
4.60	48.02244	59.54111	72.55345	87.2572	103.8150
4.80	49.48613	60.98966	73.98847	88.7131	105.2775
5.00	50.95044	62.44455	75.44415	90.1744	106.7445

$\{\Lambda_4(n, n-4, c) - c\}/c$

(1/c) \ n	4	5	6	7	8
0.20	10.00000	12.00000	15.00000	18.00000	21.00000
0.19	10.00000	12.00000	15.00000	18.00000	21.00000
0.18	10.00000	12.00000	15.00000	18.00000	21.00000
0.17	9.97800	11.97213	14.92933	17.93555	20.92533
0.16	9.95600	11.94775	14.85477	17.85064	20.85069
0.15	9.93400	11.92247	14.78087	17.76586	20.76586
0.14	9.91200	11.89733	14.70799	17.68125	20.68125
0.13	9.89000	11.87222	14.63541	17.59681	20.59681
0.12	9.86800	11.84722	14.56323	17.51254	20.51254
0.11	9.84600	11.82222	14.49145	17.42844	20.42844
0.10	9.82400	11.79722	14.42007	17.34451	20.34451
0.09	9.80200	11.77222	14.34910	17.26075	20.26075
0.08	9.78000	11.74722	14.27853	17.17716	20.17716
0.07	9.75800	11.72222	14.20836	17.09373	20.09373
0.06	9.73600	11.69722	14.13859	17.01046	20.01046
0.05	9.71400	11.67222	14.06922	16.92734	19.92734
0.04	9.69200	11.64722	13.99925	16.84437	19.84437
0.03	9.67000	11.62222	13.92968	16.76154	19.76154
0.02	9.64800	11.59722	13.86041	16.67885	19.67885
0.01	9.62600	11.57222	13.79144	16.59630	19.59630
0.00	9.60400	11.54722	13.72277	16.51389	19.51389

Table 5h. Eigenvalues of the separation constant  $\Lambda_1(n, n-5, c) - c$

c \ n	5	6	7	8	9
0.00	2.00000	6.00000	12.00000	20.00000	30.00000
0.20	2.00000	6.00000	12.00000	20.00000	30.00000
0.40	2.00000	6.00000	12.00000	20.00000	30.00000
0.60	2.00000	6.00000	12.00000	20.00000	30.00000
0.80	2.00000	6.00000	12.00000	20.00000	30.00000
1.00	7.77811	10.80000	16.2471	23.8828	33.6226
1.20	8.70592	11.62294	17.0095	24.5969	34.2999
1.40	9.57255	12.42322	17.7479	25.2934	34.9636
1.60	10.38966	13.18533	18.4554	25.9736	35.6148
1.80	11.15922	13.91885	19.1407	26.6386	36.2541
2.00	11.88449	14.62263	19.8034	27.2896	36.8824
2.20	12.56294	15.30177	20.4439	27.9275	37.5002
2.40	13.20494	15.95743	21.1442	28.5532	38.1083
2.60	13.81928	16.61193	21.7750	29.1677	38.7072
2.80	14.41499	17.24773	22.3926	29.7716	39.2975
3.00	15.01185	17.86331	22.9980	30.3657	39.8798
3.20	15.60960	18.45922	23.5923	30.9506	40.4544
3.40	16.20799	19.04557	24.1762	31.5270	41.0218
3.60	16.80657	19.62258	24.7506	32.0953	41.5826
3.80	17.40570	20.18956	25.3161	32.6552	42.1369
4.00	18.00553	20.74733	25.8734	33.2071	42.6853
4.20	18.60594	21.29592	26.4231	33.7514	43.2273
4.40	19.20691	21.83533	26.9657	34.2886	43.7652
4.60	19.80842	22.36557	27.5117	34.8194	44.2975
4.80	20.41046	22.88721	28.0316	35.3439	44.8249
5.00	20.5052	23.4004	28.5557	35.8686	45.3478

$\{\Lambda_1(n, n-5, c) - c\}/c$

(1/c) \ n	5	6	7	8	9
0.20	4.00000	4.00000	5.71111	7.17777	9.0696
0.19	4.00000	4.00000	5.71111	7.17777	9.0696
0.18	4.00000	4.00000	5.71111	7.17777	9.0696
0.17	3.97600	4.35666	5.53722	6.9436	8.7456
0.16	3.95200	4.33500	5.52374	6.9179	8.7201
0.15	3.92800	4.31333	5.51026	6.8924	8.6946
0.14	3.90400	4.29166	5.49678	6.8669	8.6691
0.13	3.88000	4.27000	5.48330	6.8414	8.6436
0.12	3.85600	4.24833	5.46982	6.8159	8.6181
0.11	3.83200	4.22666	5.45634	6.7904	8.5926
0.10	3.80800	4.20500	5.44286	6.7649	8.5671
0.09	3.78400	4.18333	5.42938	6.7394	8.5416
0.08	3.76000	4.16166	5.41590	6.7139	8.5161
0.07	3.73600	4.14000	5.40242	6.6884	8.4906
0.06	3.71200	4.11833	5.38894	6.6629	8.4651
0.05	3.68800	4.09666	5.37546	6.6374	8.4396
0.04	3.66400	4.07500	5.36198	6.6119	8.4141
0.03	3.64000	4.05333	5.34850	6.5864	8.3886
0.02	3.61600	4.03166	5.33502	6.5609	8.3631
0.01	3.59200	4.01000	5.32154	6.5354	8.3376
0.00	3.56800	3.98833	5.30806	6.5099	8.3121



Table 5i. Eigenvalues of the separation constant  $A_3(n, n-5, c) - c$

C \ N	5	6	7	8	9
0.00	12.00000	20.00000	30.00000	42.00000	56.00000
.20	13.15660	21.25749	31.29009	43.20030	57.20043
.40	14.31378	22.41539	32.45804	44.36843	58.36856
.60	15.47116	23.57456	33.62614	45.53653	59.53666
.80	16.62861	24.73396	34.79430	46.70462	60.70475
1.00	18.35503	26.55779	36.59666	48.58922	62.58929
1.20	19.77717	27.93444	37.94855	49.92466	63.92470
1.40	21.22275	29.32455	39.30770	51.26033	65.26036
1.60	22.70997	30.71923	40.67403	52.59644	66.59647
1.80	24.21866	32.11333	42.03771	53.93271	67.93274
2.00	25.72344	33.50660	43.40060	55.26905	69.26908
2.20	27.24233	34.96155	44.77559	56.60342	70.60345
2.40	28.78233	36.46777	46.14588	57.93774	71.93777
2.60	30.34798	37.97928	47.51448	59.27197	73.27200
2.80	31.94966	39.49544	48.88221	60.60610	74.60613
3.00	33.59333	40.96144	50.24773	62.00000	75.95000
3.20	35.28599	42.41833	51.60997	63.33373	77.29373
3.40	37.02466	43.86111	52.96889	64.66723	78.63723
3.60	38.80433	44.81112	54.32466	65.99043	79.98043
3.80	39.62933	46.19322	55.67666	67.31343	81.32343
4.00	40.50233	47.57336	57.02445	68.63620	82.66620
4.20	42.42466	48.95111	58.38997	69.95943	84.00943
4.40	44.39333	50.32444	59.13997	71.28266	85.35266
4.60	46.41111	51.69777	60.08444	72.60589	86.69589
4.80	48.48000	53.06666	61.03333	73.92912	88.03912
5.00	47.60996	54.37889	63.70114	75.25233	88.92665

$$\{A_3(n, n-5, c) - c\}/c$$

(1/C) \ N	5	6	7	8	9
.20	3.52219	10.87553	12.74033	15.05507	17.78553
.19	3.38855	10.66667	12.43337	14.62253	17.22066
.18	3.24444	10.45554	12.12577	14.19888	16.65511
.17	3.09999	10.24445	11.81599	13.77111	16.08866
.16	2.94993	10.02247	11.50441	13.34419	15.52110
.15	2.79447	9.80047	11.19331	12.91410	14.95220
.14	2.63333	9.58113	10.88335	12.47944	14.38260
.13	2.46666	9.35944	10.57334	12.04000	13.81220
.12	2.30000	9.13551	10.26334	11.60556	13.24180
.11	2.12444	8.90999	9.95335	11.17665	12.67140
.10	1.94888	8.68463	9.57448	10.72004	12.10000
.09	1.76555	8.44017	9.24011	10.23724	11.61494
.08	1.57888	8.18113	8.93337	9.82001	11.10666
.07	1.38883	7.90999	8.55662	9.36229	10.57111
.06	1.19444	7.63773	8.20665	8.93005	9.71882
.05	9.99877	7.37332	7.85113	8.43222	9.11555
.04	6.80007	7.10447	7.49006	7.95779	8.50666
.03	5.60012	6.83225	7.12446	7.47773	7.89005
.02	5.40009	6.55773	6.75338	6.99005	7.26773
.01	5.20003	6.27336	6.37886	6.49773	6.63770
.00	6.00000	6.00000	6.00000	6.00000	6.00000

Table 5j. Eigenvalues of the separation constant  $A_5(n, n-5, c) - c$

C \ N	5	6	7	8	9
0.00	30.00000	42.00000	56.00000	72.00000	90.00000
.20	31.12337	43.20033	57.20043	73.47466	91.53361
.40	32.27225	44.36843	58.36856	74.96551	93.08556
.60	33.44666	45.53653	59.53666	76.47229	94.64430
.80	34.64662	46.70462	60.70475	77.99220	96.22331
1.00	35.87115	48.00000	63.15663	79.53280	97.81196
1.20	37.12227	49.33373	64.64554	81.09785	99.41133
1.40	38.40000	50.70338	66.14554	82.68433	101.02148
1.60	39.70338	52.08889	67.68666	84.29223	102.64449
1.80	41.03342	53.46883	69.19331	85.92143	104.27922
2.00	42.39117	55.82773	70.75566	87.57199	105.92445
2.20	43.77633	57.32220	72.32550	89.23383	107.58335
2.40	45.18883	58.86630	73.91000	90.90694	109.24668
2.60	46.62777	60.38551	75.51022	92.59326	110.92331
2.80	48.09443	61.94773	77.12533	94.29677	112.60995
3.00	49.58882	63.52255	78.75447	95.96343	114.30553
3.20	51.10888	65.12223	80.39880	97.59121	116.01012
3.40	52.65559	66.73544	82.05449	99.18007	117.72442
3.60	54.22887	68.36661	83.72448	100.73998	119.44668
3.80	55.82665	70.01662	85.43774	102.27440	121.17778
4.00	57.44885	71.68000	87.18221	104.02779	122.91669
4.20	59.09338	73.36622	88.95885	105.80000	124.66339
4.40	60.76112	75.07446	90.75262	107.59339	126.41885
4.60	62.44997	76.79333	92.75448	109.40002	128.18005
4.80	64.15881	78.53335	93.99339	111.21991	129.94996
5.00	65.88553	80.22227	95.74229	112.85881	131.72556

$$\{A_5(n, n-5, c) - c\}/c$$

(1/C) \ N	5	6	7	8	9
.20	13.17771	16.04441	19.14886	22.57716	26.34551
.19	12.95551	15.67733	18.63222	21.88661	25.47338
.18	12.73390	15.31386	18.11774	21.20333	24.60448
.17	12.52291	14.96225	17.60997	20.52335	23.73994
.16	12.32558	14.61115	17.10004	19.84771	22.87448
.15	12.14293	14.26553	16.59885	19.17445	22.11446
.14	11.97000	13.92662	16.10116	18.51662	21.35881
.13	11.80578	13.59333	15.61000	17.84226	20.60557
.12	11.64836	13.26666	15.12447	17.18433	19.84500
.11	11.49155	12.94661	14.64559	16.53520	18.61558
.10	11.25553	12.63556	14.17444	15.88664	17.77996
.09	11.02023	12.33333	13.71009	15.24883	16.95004
.08	10.79562	12.03333	13.25561	14.61886	16.12991
.07	10.58168	11.73444	12.81005	13.99882	15.31669
.06	10.36837	11.43773	12.37990	13.39881	14.51550
.05	10.56667	11.20003	11.95002	12.78894	13.72447
.04	10.43554	10.99444	11.53665	12.20331	12.94755
.03	10.31194	10.80993	11.13444	11.63002	12.18500
.02	10.19884	10.64555	10.74442	11.07115	11.43886
.01	10.10221	10.52241	10.36666	10.52880	10.70998
.00	10.00000	10.00000	10.00000	10.00000	10.00000

Table 6a. Eigenvalues of the separation constant  $\Lambda_0(n, n-2, p) + p$

p \ n	2	3	4	5	6
.00	0.60000	2.00000	6.00000	12.00000	20.00000
.20	0.62914	1.82933	5.87339	11.91755	19.92448
.40	0.63555	1.63433	5.74711	11.80771	19.84443
.60	0.63555	1.41337	5.63310	11.66981	19.75811
.80	0.63555	1.16221	5.43668	11.57995	19.66555
1.00	0.60000	0.87633	5.25554	11.45022	19.56660
1.20	0.55559	0.58233	5.05338	11.30889	19.45889
1.40	0.51523	0.29550	4.82997	11.15544	19.34334
1.60	0.47833	-0.20551	4.58008	10.98853	19.21886
1.80	0.44419	-0.64447	4.33449	10.80000	19.08338
2.00	0.41233	-1.12331	4.00000	10.59669	18.93777
2.20	0.38337	-1.63733	3.66444	10.37422	18.77955
2.40	0.35337	-2.18661	3.23669	10.13044	18.60779
2.60	0.32614	-2.76551	2.89969	9.86337	18.42217
2.80	0.30000	-3.37337	2.46444	9.57225	18.21955
3.00	0.27444	-4.00000	2.00000	9.25554	18.00000
3.20	0.24999	-4.64333	1.55044	8.91114	17.76119
3.40	0.22555	-5.31733	1.11988	8.53966	17.50337
3.60	0.20111	-6.00000	0.71422	8.13966	17.22443
3.80	0.17666	-6.69555	0.31466	7.71114	16.92223
4.00	0.15444	-7.40000	0.00000	7.25554	16.59669
4.20	0.13222	-8.12333	-0.31466	6.77225	16.24779
4.40	0.11000	-8.86666	-0.64333	6.26337	15.87723
4.60	0.08777	-9.63333	-1.00000	5.73044	15.48723
4.80	0.06555	-10.43333	-1.39555	5.17444	15.07470
5.00	0.04333	-11.26666	-1.83333	4.59669	14.63969

Table 6b. Eigenvalues of the separation constant  $\Lambda_2(n, n-2, p) + p$

p \ n	2	3	4	5	6
.00	0.00000	12.00000	20.00000	30.00000	42.00000
.20	0.49114	11.37337	19.32000	29.33225	41.25552
.40	0.63555	10.76555	18.65555	28.65929	40.55557
.60	0.83333	10.18111	18.00000	27.99119	39.84449
.80	1.09114	9.63773	17.36332	27.32205	39.13445
1.00	1.40000	9.12331	16.74446	26.65498	38.43440
1.20	1.75999	8.63447	16.14666	25.99911	37.74441
1.40	2.15555	8.16951	15.58000	25.35456	37.05556
1.60	2.59555	7.73457	15.03999	24.72147	36.36884
1.80	3.07444	7.32887	14.52446	24.09930	35.68442
2.00	3.59669	6.95111	14.03333	23.48731	35.00223
2.20	4.15999	6.60227	13.56555	22.88558	34.32225
2.40	4.76333	6.28333	13.12333	22.29336	33.64441
2.60	5.40666	6.00000	12.70333	21.71111	32.96883
2.80	6.08000	5.74446	12.30555	21.13929	32.29557
3.00	6.78333	5.51111	11.93000	20.57777	31.62441
3.20	7.51666	5.29999	11.57555	20.02666	30.95556
3.40	8.28000	5.10777	11.24111	19.48555	30.28886
3.60	9.07333	4.93333	10.92666	18.95444	29.62441
3.80	9.89666	4.77555	10.63000	18.43333	28.96111
4.00	10.75000	4.63333	10.35000	17.92222	28.29999
4.20	11.63333	4.50000	10.08555	17.42111	27.64111
4.40	12.54666	4.37555	9.83555	16.92999	26.98444
4.60	13.49000	4.26000	9.60000	16.44888	26.32888
4.80	14.46333	4.15333	9.37555	15.97777	25.67444
5.00	15.46666	4.05555	9.16000	15.51666	25.02111

$$\{ \Lambda_0(n, n-2, p) + p \} / p$$

(1/p) \ n	2	3	4	5	6
.20	0.28668	0.21225	0.80000	0.31934	0.91334
.19	0.31881	0.23333	0.83333	0.29335	0.85338
.18	0.34999	0.25555	0.86666	0.26889	0.79333
.17	0.38221	0.27777	0.90000	0.24555	0.73333
.16	0.41448	0.29999	0.93333	0.22222	0.67333
.15	0.44800	0.32222	0.96666	0.20000	0.61333
.14	0.48177	0.34444	1.00000	0.17889	0.55333
.13	0.51588	0.36666	1.03333	0.15889	0.49333
.12	0.55044	0.38888	1.06666	0.13966	0.43333
.11	0.58554	0.41111	1.10000	0.12111	0.37333
.10	0.62099	0.43333	1.13333	0.10333	0.31333
.09	0.65669	0.45555	1.16666	0.08666	0.25333
.08	0.69333	0.47777	1.20000	0.07111	0.19333
.07	0.73011	0.49999	1.23333	0.05666	0.13333
.06	0.76774	0.52222	1.26666	0.04333	0.07333
.05	0.80551	0.54444	1.30000	0.03111	0.01333
.04	0.84333	0.56666	1.33333	0.02000	0.00000
.03	0.88116	0.58888	1.36666	0.01000	0.00000
.02	0.92008	0.61111	1.40000	0.00000	0.00000
.01	0.95888	0.63333	1.43333	0.00000	0.00000
.00	1.00000	0.65555	1.46666	0.00000	0.00000

$$\{ \Lambda_2(n, n-2, p) + p \} / p$$

(1/p) \ n	2	3	4	5	6
.20	0.48668	1.01225	2.00000	3.48006	5.48006
.19	0.45881	0.94994	1.87333	3.36665	5.12662
.18	0.42999	0.88773	1.74999	3.25338	4.78002
.17	0.40221	0.82773	1.62333	3.14111	4.44334
.16	0.37448	0.76922	1.51333	3.02888	4.11665
.15	0.34880	0.71222	1.40888	2.91666	3.80000
.14	0.32417	0.65665	1.29999	2.80444	3.49333
.13	0.29958	0.60111	1.19227	2.69222	3.18666
.12	0.27504	0.54666	1.08555	2.58000	2.88000
.11	0.25054	0.49333	0.97777	2.46777	2.57333
.10	0.22609	0.44000	0.87000	2.35555	2.26666
.09	0.20169	0.38773	0.76222	2.24333	1.96000
.08	0.17734	0.33555	0.65444	2.13111	1.65333
.07	0.15301	0.28333	0.54666	2.01888	1.34666
.06	0.12874	0.23111	0.43888	1.90666	1.04000
.05	0.10511	0.17888	0.33111	1.79444	0.73333
.04	0.08133	0.12666	0.22333	1.68222	0.42666
.03	0.05755	0.07444	0.11555	1.57000	0.12000
.02	0.03377	0.02222	0.00777	1.45777	0.00000
.01	0.01000	0.00000	0.00000	1.34555	0.00000
.00	0.00000	0.00000	0.00000	1.23333	0.00000

Table 6c. Eigenvalues of the separation constant  $\Lambda_1(n, n-3, p) + p$

$p \setminus n$	3	4	5	6	7
.00	2.00000	6.60000	12.00000	20.00000	30.00000
.20	1.16449	5.52453	11.03253	19.33760	29.41089
.40	-1.18088	4.46883	10.63422	18.73988	28.81277
.60	-1.77033	3.66633	9.92559	18.09280	28.20448
.80	-1.74662	2.84559	9.20000	17.42889	27.58669
1.00	-2.74466	2.00000	8.45660	16.75300	26.95884
1.20	-3.76332	1.13133	7.69335	16.06229	26.32189
1.40	-4.80000	0.24148	6.91244	15.35881	25.67680
1.60	-5.85229	-0.66911	6.11244	14.63381	25.02552
1.80	-6.92011	-1.60000	5.29335	13.90225	24.37300
2.00	-8.00000	-2.54333	4.45660	13.15111	23.71822
2.20	-9.09111	-3.51175	3.63300	12.38337	23.06145
2.40	-10.19211	-4.50133	2.72559	11.60000	22.40268
2.60	-11.30119	-5.50419	1.83422	10.80000	21.74186
2.80	-12.41195	-6.51622	0.92553	9.98337	21.07564
3.00	-13.54440	-7.54440	0.00060	9.15111	20.40000
3.20	-14.67477	-8.58811	-0.94111	8.30225	19.72291
3.40	-15.81019	-9.63555	-1.89973	7.44881	19.04437
3.60	-16.95220	-10.68778	-2.86678	6.59331	18.36437
3.80	-18.09975	-11.74667	-3.85119	5.73629	17.68291
4.00	-19.24700	-12.81489	-4.84889	4.87530	17.00000
4.20	-20.39000	-13.89371	-5.85778	3.98889	16.31564
4.40	-21.53563	-14.98226	-6.87881	3.09190	15.62866
4.60	-22.68155	-16.07956	-7.90990	2.19318	14.94268
4.80	-23.82773	-17.18416	-8.94339	1.29760	14.25812
5.00	-25.04166	-18.29578	-10.00000	0.00000	13.57422

$$\{\Lambda_1(n, n-3, p) + p\} / p$$

$(1/p) \setminus n$	3	4	5	6	7
.20	-5.00083	-3.67116	-2.00000	-0.63330	2.32884
.19	-5.00496	-3.76911	-2.16550	-0.72473	1.98335
.18	-5.01916	-3.86633	-2.33229	-0.81886	1.63339
.17	-5.03343	-3.96633	-2.50339	-0.91541	1.27932
.16	-5.04776	-4.06331	-2.67880	-1.01342	0.91888
.15	-5.06221	-4.17133	-2.85556	-1.11294	0.55220
.14	-5.07672	-4.27977	-3.03668	-1.21399	0.17833
.13	-5.09132	-4.38856	-3.22216	-1.31660	-0.20333
.12	-5.10600	-4.49778	-3.41104	-1.42082	-0.59332
.11	-5.12077	-4.60743	-3.60331	-1.52667	-0.99111
.10	-5.13564	-4.72254	-3.80330	-1.63416	-1.40000
.09	-5.15060	-4.83322	-4.01111	-1.74333	-1.81779
.08	-5.16566	-4.94844	-4.22664	-1.85411	-2.24557
.07	-5.18082	-5.06804	-4.44160	-1.96669	-2.68335
.06	-5.19609	-5.19203	-4.66299	-2.08138	-3.13133
.05	-5.21146	-5.32335	-4.88436	-2.20673	-3.58885
.04	-5.22694	-5.45955	-5.10704	-2.34322	-4.05449
.03	-5.24253	-5.59933	-5.33269	-2.49132	-4.52999
.02	-5.25824	-5.74233	-5.56274	-2.65111	-5.01229
.01	-5.27406	-5.88883	-5.79618	-2.82225	-5.50331
.00	-5.00000	-6.00000	-6.00000	-6.00000	-6.00000

Table 6d. Eigenvalues of the separation constant  $\Lambda_3(n, n-3, p) + p$

$p \setminus n$	3	4	5	6	7
.00	12.00000	20.00000	30.00000	42.00000	56.00000
.20	11.29551	19.15441	28.80747	41.02440	54.98911
.40	10.61922	18.33111	28.16558	40.06682	53.98733
.60	9.97033	17.53111	27.27411	39.11090	52.99522
.80	9.34662	16.75441	26.43310	38.17111	52.01331
1.00	8.74446	16.00000	25.54440	37.24770	51.04166
1.20	8.16332	15.28889	24.73365	36.33771	50.08111
1.40	7.60000	14.58889	23.88876	35.44419	49.13200
1.60	7.05220	13.88889	23.00076	34.56619	48.19448
1.80	6.52011	13.20000	22.30065	33.69975	47.27000
2.00	6.00000	12.54433	21.54440	32.84889	46.35778
2.20	5.49911	11.91445	20.80000	32.01663	45.45888
2.40	4.99221	11.30133	20.07771	31.20000	44.57332
2.60	4.50119	10.70119	19.36558	30.40000	43.71144
2.80	4.01955	10.11162	18.67447	29.61663	42.84336
3.00	3.54440	9.54441	18.00000	28.84889	42.00000
3.20	3.07477	8.98441	17.34111	28.09975	41.17009
3.40	2.61009	8.43555	16.69733	27.36619	40.35663
3.60	2.15226	7.89773	16.06676	26.64619	39.55663
3.80	1.69975	7.36887	15.45119	25.93771	38.77009
4.00	1.24776	6.84333	14.84489	25.24770	38.00000
4.20	0.80000	6.33111	14.23778	24.57111	37.24336
4.40	0.35663	5.83226	13.67881	23.90000	36.50144
4.60	-0.08445	5.33555	13.10996	23.23263	35.77332
4.80	-0.52227	4.84445	12.54339	22.62440	35.05888
5.00	-0.95884	4.35773	12.00000	22.00000	34.35778

$$\{\Lambda_3(n, n-3, p) + p\} / p$$

$(1/p) \setminus n$	3	4	5	6	7
.20	-1.49177	0.87116	2.40000	4.40000	6.87116
.19	-1.29044	0.70811	2.14550	4.02773	6.35665
.18	-1.38844	0.54533	1.83229	3.65886	5.84661
.17	-1.48557	0.38633	1.64339	3.29441	5.34008
.16	-1.58222	0.22331	1.39880	2.93442	4.84412
.15	-1.67779	0.07111	1.15556	2.57334	4.34889
.14	-1.77228	-0.08233	0.91668	2.22229	3.86113
.13	-1.86668	-0.23444	0.68116	1.88669	3.38333
.12	-1.96000	-0.38444	0.45000	1.55482	2.91332
.11	-2.05223	-0.53221	0.22331	1.21667	2.45119
.10	-2.14336	-0.67775	0.00000	0.89116	2.00000
.09	-2.23440	-0.82233	-0.21669	0.57333	1.55779
.08	-2.32443	-0.96111	-0.43336	0.26117	1.12335
.07	-2.41118	-1.10000	-0.64440	0.04411	0.70335
.06	-2.49991	-1.23555	-0.85331	-0.17412	0.29113
.05	-2.58554	-1.36999	-1.05220	-0.33277	-1.11115
.04	-2.67006	-1.50226	-1.24936	-0.49178	-1.50511
.03	-2.75447	-1.63223	-1.44331	-0.65178	-1.89001
.02	-2.83776	-1.75999	-1.63336	-0.81336	-2.26771
.01	-2.91994	-1.88889	-1.81662	-1.07375	-2.63669
.00	-2.00000	-2.00000	-2.00000	-2.00000	-2.00000

Table 6e. Eigenvalues of the separation constant  $\Lambda_0(n, n-4, p) + p$

$p \setminus n$	4	5	6	7	8
0.00	0.00000	2.00000	6.00000	12.00000	20.00000
0.20	0.30399	1.65438	5.75699	11.80135	19.84899
0.40	-1.36077	1.29333	5.48159	11.58800	19.68999
0.60	-2.7226	0.74933	5.16769	11.33005	19.5074
0.80	-3.3221	0.16333	4.8087	11.1277	19.3139
1.00	-4.4821	-0.5031	4.3970	10.8458	19.1026
1.20	-5.7254	-1.2995	3.9248	10.5303	18.8710
1.40	-7.0308	-2.1726	3.3845	10.1763	18.6165
1.60	-8.3826	-3.1476	2.7696	9.7785	18.3360
1.80	-9.7695	-4.2043	2.0758	9.3312	18.0261
2.00	-11.1838	-5.3311	1.3019	8.8289	17.6831
2.20	-12.6199	-6.5160	0.4493	8.2668	17.3026
2.40	-14.0737	-7.7493	-0.4774	7.6406	16.8810
2.60	-15.5421	-9.0227	-1.4720	6.9481	16.4135
2.80	-17.0229	-10.3296	-2.5275	6.1883	15.8960
3.00	-18.5140	-11.6646	-3.6365	5.3625	15.3252
3.20	-20.0143	-13.0236	-4.7922	4.4732	14.6980
3.40	-21.5224	-14.4031	-5.9883	3.5523	14.0129
3.60	-23.0374	-15.8054	-7.2196	2.6246	13.2691
3.80	-24.5585	-17.2112	-8.4815	1.6884	12.4674
4.00	-26.0850	-18.6396	-9.7730	0.7309	11.6095
4.20	-27.6164	-20.0781	-11.0820	-0.2562	10.6981
4.40	-29.1523	-21.5275	-12.4147	-1.3488	9.7367
4.60	-30.6920	-22.9865	-13.7657	-2.4128	8.7289
4.80	-32.2354	-24.4544	-15.1332	-3.5478	7.6786
5.00	-33.7821	-25.9301	-16.5153	-4.7319	6.5896

Table 6f. Eigenvalues of the separation constant  $\Lambda_2(n, n-4, p) + p$

$p \setminus n$	4	5	6	7	8
0.00	0.00000	12.00000	20.00000	30.00000	42.00000
0.20	0.10488	11.80135	19.84899	29.84899	41.80513
0.40	0.33557	11.58800	19.68999	29.68999	41.60513
0.60	0.69449	11.33005	19.5074	29.5074	41.40390
0.80	1.1647	11.1277	19.3139	29.3139	41.2039
1.00	2.7173	10.8458	19.1026	29.1026	41.0039
1.20	3.2500	10.5303	18.8710	28.8710	40.8039
1.40	1.9653	10.1763	18.6165	28.6165	40.6039
1.60	1.6214	9.7785	18.3360	28.3360	40.4039
1.80	1.2809	9.3312	18.0261	28.0261	40.2039
2.00	0.9343	8.8289	17.6831	27.6831	40.0039
2.20	0.5749	8.2668	17.3026	27.3026	39.8039
2.40	0.1971	7.6406	16.8810	26.8810	39.6039
2.60	-0.2031	6.9481	16.4135	26.4135	39.4039
2.80	-0.6284	6.1883	15.8960	25.8960	39.2039
3.00	-1.0808	5.3625	15.3252	25.3252	39.0039
3.20	-1.5613	4.4732	14.6980	24.6980	38.8039
3.40	-2.0699	3.5523	14.0129	24.0129	38.6039
3.60	-2.6059	2.6246	13.2691	23.2691	38.4039
3.80	-3.1683	1.6884	12.4674	22.4674	38.2039
4.00	-3.7553	0.7309	11.6095	21.6095	38.0039
4.20	-4.3650	-0.2562	10.6981	20.6981	37.8039
4.40	-4.9956	-1.3488	9.7367	19.7367	37.6039
4.60	-5.6449	-2.4128	8.7289	18.7289	37.4039
4.80	-6.3109	-3.5478	7.6786	17.6786	37.2039
5.00	-6.9919	-4.7319	6.5896	16.5896	37.0039

$\{\Lambda_0(n, n-4, p) + p\}/p$

$(1/p) \setminus n$	4	5	6	7	8
0.20	-6.7564	-5.1863	-3.3031	-1.1264	1.3179
0.19	-6.8061	-5.2977	-3.4873	-1.3908	0.9697
0.18	-6.8568	-5.4113	-3.6758	-1.6623	0.6103
0.17	-6.9085	-5.5232	-3.8686	-1.9410	0.2396
0.16	-6.9612	-5.6422	-4.0660	-2.2271	-0.1427
0.15	-7.0151	-5.7633	-4.2681	-2.5207	-0.5355
0.14	-7.0701	-5.8893	-4.4750	-2.8220	-0.9422
0.13	-7.1264	-6.0224	-4.6869	-3.1312	-1.3597
0.12	-7.1839	-6.1626	-4.9041	-3.4487	-1.7893
0.11	-7.2427	-6.3094	-5.1268	-3.7746	-2.2314
0.10	-7.3030	-6.4629	-5.3552	-4.1194	-2.6862
0.09	-7.3647	-6.6233	-5.5895	-4.4733	-3.1542
0.08	-7.4279	-6.7904	-5.8299	-4.8366	-3.6357
0.07	-7.4928	-6.9643	-6.0768	-5.2097	-4.1312
0.06	-7.5594	-7.1453	-6.3303	-5.5929	-4.6411
0.05	-7.6278	-7.3319	-6.5907	-5.9764	-5.1654
0.04	-7.6981	-7.5233	-6.8581	-6.3604	-5.7043
0.03	-7.7703	-7.7197	-7.1327	-6.7448	-6.2577
0.02	-7.8447	-7.9214	-7.4149	-7.1297	-6.8251
0.01	-7.9212	-8.1284	-7.7036	-7.5151	-7.4061
0.00	-8.0000	-8.0000	-8.0000	-8.0000	-8.0000

$\{\Lambda_2(n, n-4, p) + p\}/p$

$(1/p) \setminus n$	4	5	6	7	8
0.20	-1.3984	-0.3213	0.9904	2.5945	4.5847
0.19	-1.5025	-0.4504	0.8276	2.3637	4.2553
0.18	-1.6106	-0.5823	0.6574	2.1339	3.9291
0.17	-1.7228	-0.7173	0.4781	1.9062	3.6045
0.16	-1.8388	-0.8555	0.2880	1.6848	3.2790
0.15	-1.9584	-1.0463	0.0856	1.4127	2.9495
0.14	-2.0814	-1.2942	-0.1305	1.1464	2.6118
0.13	-2.2076	-1.5931	-0.3606	0.8623	2.2686
0.12	-2.3366	-1.9366	-0.6344	0.5378	1.8894
0.11	-2.4683	-2.3263	-0.9610	0.2316	1.4921
0.10	-2.6022	-2.7611	-1.3287	-0.1454	1.0644
0.09	-2.7381	-3.2333	-1.7305	-0.4805	0.6060
0.08	-2.8756	-3.7431	-2.1689	-0.8538	0.1219
0.07	-3.0144	-4.2901	-2.6444	-1.2643	-0.3639
0.06	-3.1544	-4.8713	-3.1544	-1.7045	-0.8607
0.05	-3.2956	-5.4869	-3.7078	-2.1746	-1.4237
0.04	-3.4381	-6.1383	-4.3033	-2.6741	-2.0477
0.03	-3.5817	-6.8276	-4.9414	-3.2025	-2.7292
0.02	-3.7267	-7.5559	-5.6147	-3.7593	-3.4692
0.01	-3.8736	-8.3243	-6.3236	-4.3447	-4.2659
0.00	-4.0000	-4.0000	-4.0000	-4.0000	-4.0000

Table 6g. Eigenvalues of the separation constant  $\Lambda_4(n, n-4, p) + p$

$p \setminus n$	4	5	6	7	8
0.00	20.00000	30.00000	42.00000	56.00000	72.00000
.20	19.06991	29.06991	40.06991	54.06991	70.06991
.40	18.13982	28.13982	39.13982	53.13982	69.13982
.60	17.20973	27.20973	38.20973	52.20973	68.20973
.80	16.27964	26.27964	37.27964	51.27964	67.27964
1.00	15.34955	25.34955	36.34955	50.34955	66.34955
1.20	14.41946	24.41946	35.41946	49.41946	65.41946
1.40	13.48937	23.48937	34.48937	48.48937	64.48937
1.60	12.55928	22.55928	33.55928	47.55928	63.55928
1.80	11.62919	21.62919	32.62919	46.62919	62.62919
2.00	10.70000	20.70000	31.70000	45.70000	61.70000
2.20	10.76991	20.76991	31.76991	45.76991	61.76991
2.40	10.83982	20.83982	31.83982	45.83982	61.83982
2.60	10.90973	20.90973	31.90973	45.90973	61.90973
2.80	10.97964	20.97964	31.97964	45.97964	61.97964
3.00	10.00000	19.00000	30.00000	44.00000	60.00000
3.20	9.06991	18.06991	29.06991	43.06991	59.06991
3.40	8.13982	17.13982	28.13982	42.13982	58.13982
3.60	7.20973	16.20973	27.20973	41.20973	57.20973
3.80	6.27964	15.27964	26.27964	40.27964	56.27964
4.00	5.34955	14.34955	25.34955	39.34955	55.34955
4.20	4.41946	13.41946	24.41946	38.41946	54.41946
4.40	3.48937	12.48937	23.48937	37.48937	53.48937
4.60	2.55928	11.55928	22.55928	36.55928	52.55928
4.80	1.62919	10.62919	21.62919	35.62919	51.62919
5.00	0.70000	9.70000	20.70000	34.70000	50.70000

Table 6h. Eigenvalues of the separation constant  $\Lambda_1(n, n-5, p) + p$

$p \setminus n$	5	6	7	8	9
0.00	2.00000	6.00000	12.00000	20.00000	31.00000
.20	1.86991	5.86991	11.86991	19.86991	30.86991
.40	1.73982	5.73982	11.73982	19.73982	30.73982
.60	1.60973	5.60973	11.60973	19.60973	30.60973
.80	1.47964	5.47964	11.47964	19.47964	30.47964
1.00	1.34955	5.34955	11.34955	19.34955	30.34955
1.20	1.21946	5.21946	11.21946	19.21946	30.21946
1.40	1.08937	5.08937	11.08937	19.08937	30.08937
1.60	0.95928	4.95928	10.95928	18.95928	29.95928
1.80	0.82919	4.82919	10.82919	18.82919	29.82919
2.00	0.70000	4.70000	10.70000	18.70000	29.70000
2.20	0.56991	4.56991	10.56991	18.56991	29.56991
2.40	0.43982	4.43982	10.43982	18.43982	29.43982
2.60	0.30973	4.30973	10.30973	18.30973	29.30973
2.80	0.17964	4.17964	10.17964	18.17964	29.17964
3.00	0.00000	4.00000	10.00000	18.00000	29.00000
3.20	-0.13989	3.86991	9.86991	17.86991	28.86991
3.40	-0.27970	3.73982	9.73982	17.73982	28.73982
3.60	-0.41951	3.60973	9.60973	17.60973	28.60973
3.80	-0.55932	3.47964	9.47964	17.47964	28.47964
4.00	-0.70000	3.34955	9.34955	17.34955	28.34955
4.20	-0.84000	3.21946	9.21946	17.21946	28.21946
4.40	-0.98000	3.08937	9.08937	17.08937	28.08937
4.60	-1.12000	2.95928	8.95928	16.95928	27.95928
4.80	-1.26000	2.82919	8.82919	16.82919	27.82919
5.00	-1.40000	2.70000	8.70000	16.70000	27.70000

$\{\Lambda_4(n, n-4, p) + p\}/p$

$(1/p) \setminus n$	4	5	6	7	8
.20	1.3548	2.3073	3.9126	6.1319	8.8974
.19	1.2486	2.1081	3.5797	5.6423	8.2350
.18	1.1474	1.9191	3.2583	5.1823	7.5805
.17	1.0513	1.7405	2.9505	4.7448	6.9350
.16	0.9600	1.5727	2.6580	4.3222	6.3037
.15	0.8735	1.4157	2.3825	3.9180	5.6871
.14	0.7915	1.2695	2.1255	3.5356	5.0903
.13	0.7140	1.1335	1.8875	3.1809	4.5191
.12	0.6405	1.0073	1.6686	2.8609	4.0799
.11	0.5710	0.8903	1.4678	2.5730	3.7493
.10	0.5052	0.7815	1.2839	2.3248	3.4218
.09	0.4427	0.6804	1.1148	2.1078	3.1082
.08	0.3835	0.5880	0.9589	1.9164	2.8047
.07	0.3273	0.4995	0.8141	1.7483	2.5199
.06	0.2738	0.4146	0.6788	1.5975	2.2416
.05	0.2228	0.3363	0.5516	1.4630	1.9791
.04	0.1748	0.2628	0.4312	1.3416	1.7206
.03	0.1298	0.1925	0.3167	1.2316	1.4659
.02	0.0834	0.1255	0.2070	1.1320	1.2150
.01	0.0408	0.0615	0.1017	1.0421	0.9676
.00	0.0000	0.0000	0.0000	1.0000	0.0000

$\{\Lambda_1(n, n-5, p) + p\}/p$

$(1/p) \setminus n$	5	6	7	8	9
.20	-0.52236	-6.7334	-4.6624	-5.6255	-4.4139
.19	-0.58009	-6.8851	-4.8142	-5.7773	-4.5657
.18	-0.63991	-7.0368	-4.9660	-5.9291	-4.7175
.17	-0.69973	-7.1885	-5.1178	-6.0809	-4.8693
.16	-0.76000	-7.3402	-5.2696	-6.2327	-5.0211
.15	-0.82000	-7.4919	-5.4214	-6.3845	-5.1729
.14	-0.88000	-7.6436	-5.5732	-6.5363	-5.3247
.13	-0.94000	-7.7953	-5.7250	-6.6881	-5.4765
.12	-0.99999	-7.9470	-5.8768	-6.8399	-5.6283
.11	-1.06000	-8.0987	-6.0286	-6.9917	-5.7801
.10	-1.12000	-8.2504	-6.1804	-7.1435	-5.9319
.09	-1.18000	-8.4021	-6.3322	-7.2953	-6.0837
.08	-1.24000	-8.5538	-6.4840	-7.4471	-6.2355
.07	-1.30000	-8.7055	-6.6358	-7.5989	-6.3873
.06	-1.36000	-8.8572	-6.7876	-7.7507	-6.5391
.05	-1.42000	-9.0089	-6.9394	-7.9025	-6.6909
.04	-1.48000	-9.1606	-7.0912	-8.0543	-6.8427
.03	-1.54000	-9.3123	-7.2430	-8.2061	-6.9945
.02	-1.60000	-9.4640	-7.3948	-8.3579	-7.1463
.01	-1.66000	-9.6157	-7.5466	-8.5097	-7.2981
.00	-10.0000	-10.0000	-10.0000	-10.0000	-10.0000

Table 6i. Eigenvalues of the separation constant  $\Lambda_3(n, n-5, p) + p$

$p \setminus n$	5	6	7	8	9
0.00	12.00000	22.60000	38.00000	42.30000	56.00000
0.20	10.89771	18.77433	28.72744	35.42991	49.70119
0.40	9.84155	17.53328	26.47452	33.42991	47.41119
0.60	8.82554	16.42235	25.24442	32.24442	45.21885
0.80	7.84008	15.33513	24.03652	30.91117	42.8552
1.00	6.87977	14.26677	23.85228	35.67664	49.59221
1.20	5.93551	13.14413	22.89356	34.4582	48.3405
1.40	5.00111	12.18333	21.95858	33.2581	47.1011
1.60	4.07225	11.26666	21.04473	32.0768	45.8751
1.80	3.14552	10.38889	19.35990	30.9148	44.6632
2.00	2.21599	9.13477	18.2921	29.7723	43.4663
2.20	1.28200	8.13333	17.2448	28.6492	42.2849
2.40	0.34144	7.16977	16.2151	27.5451	41.1195
2.60	-0.6074	6.21166	15.2008	26.4594	39.9785
2.80	-1.5655	5.2554	14.1997	25.3910	38.8379
3.00	-2.5335	4.3015	13.2395	24.3389	37.7216
3.20	-3.5121	3.3491	12.2280	23.3016	36.6214
3.40	-4.5013	2.3853	11.2529	22.2777	35.5367
3.60	-5.5013	1.4213	10.2824	21.2657	34.4669
3.80	-6.5120	0.4513	9.3144	20.2638	33.4111
4.00	-7.5330	-0.5253	8.3475	19.2704	32.3684
4.20	-8.5641	-1.5592	7.3793	18.2839	31.3377
4.40	-9.6055	-2.5911	6.4105	17.3026	30.3178
4.60	-10.6551	-3.6213	5.4413	16.3262	29.3074
4.80	-11.7141	-4.6505	4.4613	15.3550	28.3052
5.00	-12.7814	-5.6264	3.4797	14.3761	27.3101

$\{\Lambda_3(n, n-5, p) + p\}/p$

$(1/p) \setminus n$	5	6	7	8	9
0.20	-2.55563	-1.11553	0.6959	2.8752	5.4623
0.19	-2.6976	-1.3067	0.4141	4.4879	4.9417
0.18	-2.8416	-1.5112	-0.1300	6.0999	4.4229
0.17	-2.9884	-1.7191	-0.1572	7.7107	3.9051
0.16	-3.1383	-1.9311	-0.4480	9.3193	3.3876
0.15	-3.2913	-2.1472	-0.7433	10.9247	2.8693
0.14	-3.4478	-2.3683	-1.0441	12.5256	2.3489
0.13	-3.6078	-2.5931	-1.3511	14.1205	1.8247
0.12	-3.7714	-2.8213	-1.6654	15.7092	1.2944
0.11	-3.9388	-3.0533	-1.9876	17.2911	0.7553
0.10	-4.1099	-3.2903	-2.3183	18.8668	0.2047
0.09	-4.2848	-3.5323	-2.6580	20.4364	-0.3600
0.08	-4.4634	-3.7791	-2.9971	22.0001	-0.9410
0.07	-4.6455	-4.0303	-3.3353	23.5582	-1.5389
0.06	-4.8311	-4.2861	-3.6728	25.1111	-2.1530
0.05	-5.0199	-4.5463	-4.0099	26.6588	-2.7810
0.04	-5.2116	-4.8111	-4.3472	28.2011	-3.4194
0.03	-5.4055	-5.0803	-4.6847	29.7388	-4.0641
0.02	-5.6009	-5.3533	-5.0211	31.2711	-4.7113
0.01	-5.8005	-5.6264	-5.3575	32.8011	-5.3575
0.00	-6.0000	-6.0000	-6.0000	-6.0000	-6.0000

Table 6j. Eigenvalues of the separation constant  $\Lambda_5(n, n-5, p) + p$

$p \setminus n$	5	6	7	8	9
0.00	36.00000	42.00000	56.00000	72.00000	91.00000
0.20	29.9014	36.73333	49.20000	63.47744	83.47744
0.40	27.8279	34.99556	46.28333	60.3636	80.3636
0.60	26.7793	33.82222	44.28333	58.28333	78.28333
0.80	25.7556	33.04333	42.84333	56.84333	76.84333
1.00	24.7566	35.91333	49.3107	64.3727	82.5278
1.20	23.7828	34.77111	48.04333	63.4381	81.1759
1.40	22.8334	33.64333	46.73666	62.4411	79.6411
1.60	21.9085	32.54333	45.55333	60.8413	78.2256
1.80	21.0078	31.46666	44.33666	59.4405	76.8157
2.00	20.1310	30.40333	43.14333	58.1773	75.4266
2.20	19.2776	29.37556	41.96666	56.9325	74.0535
2.40	18.4471	28.38333	40.81333	55.7262	72.6966
2.60	17.6391	27.42889	39.68111	54.5585	71.3562
2.80	16.8527	26.51222	38.57111	53.4293	70.0324
3.00	16.0873	25.63333	37.48000	52.3411	68.7254
3.20	15.3421	24.79111	36.41111	51.2946	67.4355
3.40	14.6162	23.98333	35.36666	50.2933	66.1528
3.60	13.9089	23.21111	34.34333	49.3337	64.8756
3.80	13.2191	22.47333	33.33333	48.4144	63.6098
4.00	12.5459	21.76666	32.34333	47.5316	62.4498
4.20	11.8886	21.09333	31.37333	46.6839	61.3916
4.40	11.2461	20.45111	30.42666	45.8711	60.4336
4.60	10.6175	19.83999	29.50000	45.0919	59.5749
4.80	10.0023	19.25333	28.59333	44.3437	58.8199
5.00	9.3994	17.1971	27.7324	43.6131	56.6205

$\{\Lambda_5(n, n-5, p) + p\}/p$

$(1/p) \setminus n$	5	6	7	8	9
0.20	1.8799	3.4393	5.5465	8.1826	11.3241
0.19	1.6385	3.0813	4.9533	7.5295	10.4809
0.18	1.4009	2.7433	4.5833	7.0795	9.6444
0.17	1.1675	2.4299	4.0933	6.5336	8.9118
0.16	0.9384	2.0664	3.6211	6.0113	8.2957
0.15	0.7139	1.7425	3.1618	5.4799	7.4887
0.14	0.4943	1.4237	2.7135	4.9374	6.5941
0.13	0.2797	1.1133	2.2774	4.3773	5.6155
0.12	0.0704	0.8133	1.8548	3.8011	4.8560
0.11	-0.1334	0.5237	1.4469	3.2043	4.1189
0.10	-0.3316	0.2473	1.0547	2.6176	3.4051
0.09	-0.5246	-0.0257	0.6788	2.0447	2.7271
0.08	-0.7107	-0.2846	0.3198	1.4363	2.0789
0.07	-0.8915	-0.5333	-0.0223	0.8429	1.4653
0.06	-1.0666	-0.7739	-0.3476	0.2341	0.8862
0.05	-1.2356	-0.9933	-0.6573	-0.2112	0.3405
0.04	-1.3994	-1.2165	-0.9517	-0.6345	-0.1748
0.03	-1.5575	-1.4251	-1.2320	-0.9780	-0.6630
0.02	-1.7101	-1.6243	-1.4994	-1.3337	-1.1277
0.01	-1.8576	-1.8163	-1.7550	-1.6737	-1.5724
0.00	-2.0000	-2.0000	-2.0000	-2.0000	-2.0000

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Кульчицкий Ю.А. и др.  
Таблицы и графики сфероидальных  
функций осциллятора

E2-86-432

В работе подытожены - в виде таблиц и графиков - результаты вычислений на ЭВМ угловых и радиальных функций изотропного осциллятора в вытянутых и в сплюснутых сфероидальных координатах. Установлена зависимость сфероидальных констант разделения от дополнительного параметра входящего в определение сфероидальных координат.

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Kulchitsky Yu.A. et al.  
Tables and Graphs of  
Oscillator Spheroidal Functions

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In the paper, we summarize, in the form of tables and graphs, the results of calculations at computer and radial functions of an oscillator in prolate and oblate spheroidal coordinates. The dependence is established for separation spheroidal constants on an extra parameter defining the spheroidal coordinates.

The investigation has been performed at the Laboratory of Theoretical Physics, JINR.

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