

**ОБЪЕДИНЕННЫЙ  
ИНСТИТУТ  
ЯДЕРНЫХ  
ИССЛЕДОВАНИЙ  
ДУБНА**

**E2-86-383**

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**POLARIZATION PHENOMENA  
IN HARD HADRON SCATTERING  
AND STRONG INTERACTION  
AT LARGE DISTANCES**

Submitted to "ЯФ"

**1986**

Quantum chromodynamics (QCD) plays an important role in the modern theory of strong interaction. The hypotheses about colour quarks<sup>/1/</sup> and local gauge-invariance make the basis of QCD. The most important results in QCD are obtained for the processes where an approximate separation of long and short distances is achieved. However, there are some troubles in QCD for elastic hadron-hadron scattering and polarization phenomena. For example, QCD models lead to a zero value for the polarization parameter. This difficulty is essential. Really, the vector interaction in QCD leads to the scattering amplitude which obeys the  $\gamma_5$ -invariance<sup>/3/</sup> for the massless-quark limit. In this case the polarization is zero. When we take into account the quark masses, a small polarization  $\rho \sim m_q/\sqrt{E}$  is possible in contradiction with the experiment. Most models of hard scattering obey the  $\gamma_5$ -invariance at short distances. So, the polarization is zero in these models.

We want to emphasize that in high-energy large-angle scattering one must take into account soft rescatterings which occur at the same collision. The following physical picture of scattering is true for every hard scattering model. Soft rescatterings of particles take place before and after a hard scattering process<sup>/4/</sup>. These effects of long distances caused by particle interaction in initial and final states lead to a large polarization at finite energies<sup>/5/</sup> for every  $\gamma_5$ -invariant model.

In this paper, following ref.<sup>/5/</sup> we thoroughly investigate the spin effects in large-angle  $PP$ -scattering. As a result, we explain the behaviour of different spin correlation functions and obtain the information about the properties of hadron interaction at short distances.

Consider the elastic hadron scattering at large angles. The investigation of these processes is not possible in QCD in a model-independent way. In QCD diagrams describing the hard scattering are some nonplanar graphs with "pinch" singularities<sup>/6,7/</sup>. They have quark masses as dimensional parameters. If the contribution of these

diagrams to the scattering amplitude is sufficiently small, the dimensional parameters are unimportant in the asymptotic region. As a result, the scattering amplitude obeys the  $\gamma_5$ -invariance.

Below we shall use the following representation for the  $\gamma_5$ -invariant asymptotical amplitude of large-angle  $\rho\rho$ -scattering<sup>/4/</sup>:

$$T_{as}(s,t) = V(s,t) \gamma_\mu^{(1)} \gamma_\mu^{(2)} + A(s,t) (\gamma_5 \gamma_\mu)^{(1)} (\gamma_5 \gamma_\mu)^{(2)}, \quad (1)$$

where  $V(s,t)$  and  $A(s,t)$  are vector-vector and axial-axial parts of interaction, respectively. Other matrix structures in the  $NN$ -scattering amplitude<sup>/8/</sup> are not  $\gamma_5$ -invariant. They must be suppressed as a power of  $S$  with growing energy.

It is easily seen that amplitude (1) leads to the following asymptotic forms of the helicity proton-proton scattering amplitude:

$$\Phi_1(s,t) = \langle ++|++ \rangle = 2[V(s,t) + V(s,u) - A(s,t) - A(s,u)];$$

$$\Phi_3(s,t) = \langle +-|+- \rangle = (1 + \cos\theta)[V(s,t) + A(s,t)]; \quad (2)$$

$$\Phi_4(s,t) = \langle +-|-+ \rangle = -(1 - \cos\theta)[V(s,u) + A(s,u)];$$

$$\Phi_2(s,t) = \langle ++|-+ \rangle \equiv 0; \quad \Phi_5(s,t) = \langle ++|+- \rangle \equiv 0.$$

As a result of  $\gamma_5$ -invariance, at short distances the amplitude  $\Phi_5$  and polarization are zero.

A consistent calculation of long-distance contributions<sup>/4,5/</sup> to the hard scattering amplitude can be done on the basis of the Logunov-Tavkhelidze quasipotential method. It leads to the preasymptotic corrections of orders  $1/\rho$ ,  $1/\rho^2$  and so on where  $\rho$  is the c.m.s. momentum of colliding particles. For the helicity amplitudes we have

$$\Phi_i (i=1,3,4)(s,t) = \Phi_i^{(0)}(s,t) + \frac{1}{\rho} \Phi_i^{(1)}(s,t) + \frac{1}{\rho^2} \Phi_i^{(2)}(s,t) + \dots, \quad (3)$$

where  $\Phi_i^{(0)}$  is the asymptotic term (2)  $\Phi_i^{(1,2)}$  are first- and second-order corrections to the leading contribution. These corrections contain the contributions of long distances. They were calculated and summed up in<sup>/5/</sup>, where one may find their explicit form.

The correction terms contain the hadron masses and other dimensional parameters, which leads to the violation of  $\gamma_5$ -invariance of interaction at finite energies. It can be shown that this effect leads to the spin-flip amplitude of the order  $m_N/\rho$ <sup>/5/</sup>.

We shall consider a particular example with  $V(s,t)$  and  $A(s,t)$  in (1) that obey the dimensional quark-counting rule (9). They have a power behaviour in  $t$  and  $u$  variables:

$$V(s,t) = \frac{1}{s^5} \left( B_1 \left| \frac{s}{t-d} \right|^{n_1} + B_3 \left| \frac{s}{u-d} \right|^{n_3} \right), \quad (4)$$

$$A(s,t) = \frac{1}{s^5} \left( B_2 \left| \frac{s}{t-d} \right|^{n_2} + B_4 \left| \frac{s}{u-d} \right|^{n_4} \right).$$

In (4) an approximate consideration of higher-order corrections to the hard part of interaction is achieved by the parameter  $d$ . We obtain the following expression for the helicity-flip amplitude

$$\begin{aligned} \Phi_5(s,t) = & \frac{e^{2i\chi(\theta)}}{s^5} \sqrt{1-\cos^2\theta} \left\{ B_1 \left[ \left| \frac{s}{t-d} \right|^{n_1} - \left| \frac{s}{u-d} \right|^{n_1} \right] F(n_1) \right. \\ & + B_2 \left[ \left| \frac{s}{t-d} \right|^{n_2} - \left| \frac{s}{u-d} \right|^{n_2} \right] F(n_2) + B_3 \left[ \left| \frac{s}{t-d} \right|^{n_3} - \left| \frac{s}{u-d} \right|^{n_3} \right] \times \\ & \left. + F(n_3) + B_4 \left[ \left| \frac{s}{t-d} \right|^{n_4} - \left| \frac{s}{u-d} \right|^{n_4} \right] F(n_4) \right\}, \quad (5) \end{aligned}$$

where the function

$$F(n) = \frac{m_N}{2\rho} + \frac{2m_N}{i\rho^2} (n - \frac{1}{2}) a \quad (6)$$

contains the preasymptotic contributions. The coefficient  $a$  and the eikonal factor  $\exp(2i\chi(\theta))$  depend on the soft part of interaction. As a result, for the hadron interaction in initial and final states we obtain the helicity-flip amplitude  $\Phi_5$  of the order  $m_N/\rho$ . It can be shown that the polarization for different models of hard scattering at  $P_L \sim 10$  GeV is 10 - 40%<sup>/5/</sup> and decreases with energy as  $1/s$ .

The calculations show that the long-distance effects don't change the amplitude  $\Phi_2$  which is equal to zero as in the asymptotic limit (2).

The experimental information about  $\rho\rho$ -polarization at large angles at  $P_L = 28$  GeV<sup>/10/</sup> permits us to determine the form of hard part of the scattering amplitude. To solve this problem, we use experimental data for  $d\sigma/dt$  at  $\cos\theta \lesssim 0.7$  and  $P_L < 7$  GeV<sup>/11/</sup>,

for the polarization at  $P_L = 28$  GeV, for spin correlation parameters  $A_{LL}$  at  $P_L = 11.75$  GeV<sup>12/</sup> and  $A_{NN}(90^\circ)$  at  $P_L > 6$  GeV<sup>13/</sup>

Only the hard part of interaction was fitted when we analysed the experimental data. The soft part which determines the preasymptotic effects to the helicity amplitudes (3,5) was fixed on the basis of the small-angle scattering analysis. So, this does not lead to additional freedom in the scattering amplitude.

The best description of the experimental data was obtained for the following values of parameters in (3)

$$\begin{aligned} B_1 &= -[162,3 \pm 14] (\text{GeV}^2)^4 & n_1 &= 4 \\ B_2 &= [8235 \pm 94] (\text{GeV}^2)^4 & n_2 &= 1 \\ B_3 &= [1586 \pm 300] (\text{GeV}^2)^4 & n_3 &= 1 \\ B_4 &= [1938 \pm 260] (\text{GeV}^2)^4 & n_4 &= 2 \\ d &= (2,5 \pm 0,1) (\text{GeV}^2) \end{aligned}$$

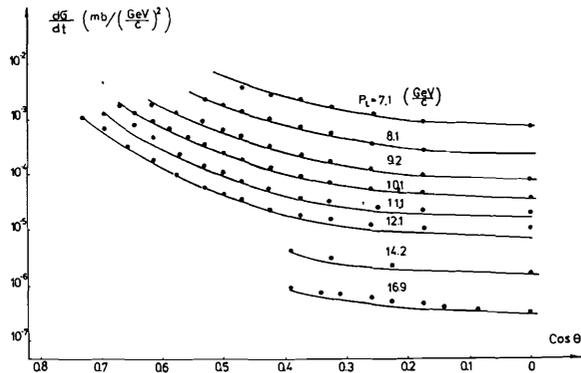


Fig. 1. Differential cross-section of  $PP$ -scattering.

Theoretical curves for differential  $PP$ -cross-sections at large angles are shown in fig. 1. The obtained results for polarization and  $A_{NN}(90^\circ)$  are presented in figs. 2,3. The polarization at  $P_L = 28$  GeV<sup>2</sup> and  $\theta_{cm} = 55^\circ$  is of order 35%.

We want to note that the preasymptotic terms of the scattering amplitudes are approximately equal to the main asymptotic term at  $P_L = 5$  GeV. As a result, they compensate leading contribution to  $\phi_3$  at  $P_L \sim 5$  GeV and  $\theta = 90^\circ$ . This leads to a dip at  $A_{NN}(90^\circ)$  in this energy region (fig.3). At lower energies the behaviour of  $A_{NN}(90^\circ)$  is determined by preasymptotic terms. It is interesting that the theory predictions are in accordance with experiment at very low energies  $P_L \sim 2$  GeV (fig. 3).

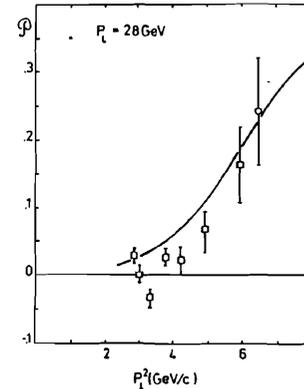


Fig. 2. Description of  $PP$ -polarization at  $P_L = 28$  GeV

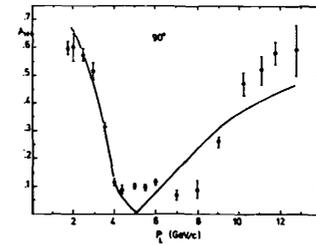


Fig. 3. Energy dependence of  $A_{NN}(90^\circ)$ .

In fig. 4 the ratio of cross sections with parallel and antiparallel spins is shown. The obtained angular and energy dependences of different spin-correlation parameters at  $P_L$  from 12 GeV to 100 GeV are plotted in fig.5. A rapid change of  $A_{SS}$ ,  $A_{LL}$ ,  $A_{NN}$  at  $\theta \sim 60^\circ$  is connected with the zero asymptotic amplitude  $\phi_3$ . The preasymptotic terms smooth this effect at low energies. Like the polarization, the parameter  $A_{SL}$  is determined by the preasymptotic effects and decreases with energy as  $1/\sqrt{s}$ .

So the dynamical mechanism which is connected with the long-distance effects discussed here leads to important conclusions about the energy dependence of spin-correlation functions. The functions  $A_{SS}$ ,  $A_{LL}$ ,  $A_{NN}$  must go to their nonzero asymptotic limits when  $s \rightarrow \infty$ . At the same time the polarization and  $A_{SL}$  must decrease with energy as

$$P \sim 1/s ; A_{SL} \sim 1/\sqrt{s}.$$

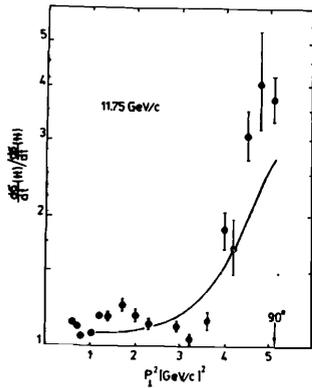


Fig. 4. The obtained ratio for cross-sections with parallel and antiparallel spins.

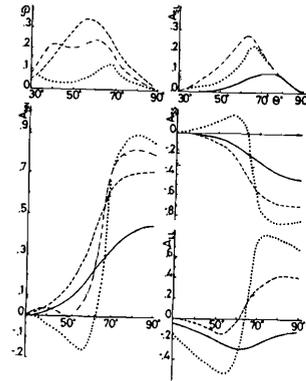


Fig. 5. Predictions for the energy dependence of spin correlation functions  $A_{SS}, A_{SL}, A_{LL}, A_{NN}$  and polarization at  $P_L = 12$  GeV;  $---$   $P_L = 28$  GeV;  $- \cdot -$   $P_L = 50$  GeV;  $\dots$   $P_L = 100$  GeV.

The large-angle polarization experiments in  $pp$ -scattering at sufficiently high energies are needed in order to check these predictions.

The information about the form of asymptotic terms of vector-vector and axial-axial parts of  $pp$  interaction at short distances can now be obtained; they are shown in fig.6. The vector-vector part of interaction is largest near  $\theta \sim 0^\circ$ . In this case the hard parts of helicity amplitudes  $\phi_1$  and  $\phi_3$  are approximately equal at  $\theta \sim 0^\circ$  to each other in accordance with experiment. This vector-vector part of interaction has zero at  $\theta \sim 60^\circ$ . This leads to zero of the helicity amplitude  $\phi_3$  that was discussed above.

The obtained hard part of interaction explains all physical effects in large angle  $pp$ -scattering with taken into account preasymptotic corrections caused by the soft rescattering of hadrons in initial and final states. So, such a behaviour of vector-vector and axial-axial parts of interaction shown in fig.6 should take place in all realistic  $\gamma_5$ -invariant models of hard hadron scattering including QCD.

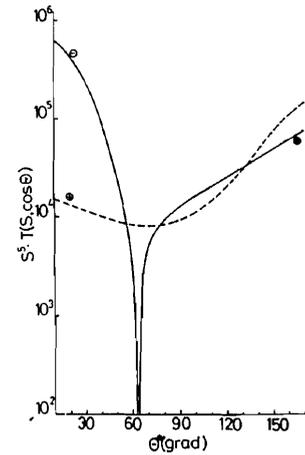


Fig. 6. Asymptotic angular dependences of hadron interaction at short distances:

— - vector-vector part at interaction,  
 --- - axial-axial part of interaction.

The authors express their deep gratitude to V.A. Matveev, V.A. Meshcheryakov, A.N. Tavkhelidze for interest in the work and useful remarks and to A.V. Koudinov for fruitful discussions.

#### References

1. Bogolubov N.N., Struminski B.V., Tavkhelidze A.N., JINR, D-1968, Dubna, 1965.
2. Logunov A.A., Meshcheryakov V.A., Tavkhelidze A.N. Doklady Akademii Nauk SSSR, 1962, v. 142, p. 317.
3. Brodsky S.J., Lepage G.P., Phys.Rev., 1981, v. 24, p. 2848.
4. Goloskokov S.V., Kuleshov S.P., Matveev V.A., Smondyrev M.A., Particles and Nucleus, 1977, v.8, p. 969.
5. Goloskokov S.V., Koudinov A.V., Kuleshov S.P., Particles and Nucleus, 1981, v. 12, p. 614.
6. Goloskokov S.V., Koudinov A.V., Matveev B.A., Teplyakov V.G., JINR, P2-81-420, Dubna 1981.
7. Mueller A.H. Phys.Rev. C, 1981, v.73, p. 237.
8. Goldberger M.L. et al. Phys.Rev. 1960, v. 120, p. 2250.

9. Matveev V.A., Muradyan R.M., Tavkhelidze A.N. Lett. Nuovo Cim., 1973, v. 7, p. 779.  
Brodsky S.J., Farrar G.R. Phys.Rev.Lett., 1973, v.30, p.1153.
10. Cameron P.R. et al. Preprint DM. HE-85-17, Michigan, 1985.
11. Benary O. et al. N.N. and ND Interactions. A Compilation. Preprint UCRL-20000, Berkeley, 1970.
12. Auer I.P. et al. Phys.Rev.Lett., 1984, v.52, p. 808.
13. Lin A. et al. Phys.Lett., 1978, v. 74B, p. 273.  
Crosbie E.A. et al. Phys.Rev., 1981, v. D23, p. 600.

Received by Publishing Department  
on June 16, 1986.

Голоскоков С.В., Кулешов С.П., Селюгин О.В. E2-86-383  
Роль взаимодействия на больших расстояниях  
в поляризационных эффектах в жестком рассеянии адронов

Показано, что учет в жестком рассеянии адронов эффектов больших расстояний позволяет количественно объяснить поведение поляризации и спиновых корреляционных параметров в pp-рассеянии на большие углы. Извлечена информация о свойствах вектор-векторной и аксиал-аксиальной частей взаимодействия протонов на малых расстояниях при высоких энергиях. Сделан вывод, что такие условия зависимости должны получаться во всех реалистических  $\gamma_5$ -инвариантных моделях жесткого столкновения адронов, в том числе и в КХД.

Работа выполнена в Лаборатории теоретической физики ОИЯИ

Препринт Объединенного института ядерных исследований. Дубна 1986

Goloskokov S.V., Kuleshov S.P., Seljugin O.V. E2-86-383  
Polarization Phenomena in Hard Hadron Scattering  
and Strong Interaction at Large Distances

It is shown that making allowance for the large-distance effects hard hadron scattering provides a quantitative description of the polarization behaviour and of spin-correlation parameters in large-angle pp-scattering. The information about vector-vector and axial-axial parts of proton-proton high-energy interaction at small distances is obtained. The conclusion has been drawn that such conditions of dependence could take place in all realistic  $\gamma_5$ -invariant models of hard hadron scattering including QCD.

The investigation has been performed at the Laboratory of Theoretical Physics, JINR.

Preprint of the Joint Institute for Nuclear Research. Dubna 1986