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DIFFICULTIES OF THE THERMODYNAMICAL MODEL APPROACH TO PION PRODUCTION IN RELATIVISTIC ION COLLISIONS



Thermodynamic models based on various assumptions concerning the geometry and thermodynamics of collisions are widely used in describing data from relativistic ion collisions ^{/1/}. The models reproduce reasonably the shapes of the spectra of produced particles, but essential problems arise when the total number of produced pions is considered. Thermodynamic models predict about twice as many pions in comparison with experimental data.

In the present paper we concentrate on reproducing, in thermodynamic models, the average multiplicity of negative pions, $\langle n \rangle^{inel}$, produced in inelastic collisions of ⁴He and¹²C with various nuclear targets (Li,...,Pb) at a 4.5 GeV/e momentum per incident nucleon. We compare results of model calculations with experimental average transverse momenta, $\langle p_T \rangle$, of i^- mesons and average rapidities $\langle y \rangle$.

Two thermodynamic models, firestreak $^{2,3/}$ and firetube $^{4/}$, have been tested. The models differ only in geometrical assumptions concerning the dynamics of collisions. Because the firestreak model is widely described in the literature $^{/1-3/}$ we briefly present geometrical assumptions of the firetube model only. Diffuse surface density distributions are used in this model as in the firestreak one. Interactions between collinear tubes of nucleons (with geometrical cross sections $\sigma = \sigma_{\rm NN}^{\rm tot}$) are assumed to occur independently. The probability of finding n nucleons in a projectile or target tube centered at \overline{b} in the plane perpendicular to the collision axis z is

$$P_{p,t}^{n}(b) = \left(\frac{A_{p,t}}{n}\right) \left(\frac{\sigma T_{p,t}(b)}{A_{p,t}}\right)^{n} \left(1 - \frac{\sigma T_{p,t}(b)}{A_{p,t}}\right)^{A_{p,t}-n}$$

where $A_{p,t}$ is the projectile (target) mass number and the "thickness function", $T_{p,t}$, is $^{/5/}$

$$T_{p,t}(b) = \int_{-\infty}^{+\infty} \rho_{p,t}(b, z) dz$$
.

The cross section for projectile-target interaction is

$$\sigma_{A_{p},A_{t}} = \int d^{2}B P^{in1}(B),$$

where

$$P^{int}(B) = 1 - \exp \left[\int \frac{d^2 b}{\sigma} \ln P^0(\bar{b}, \bar{B}) \right],$$

$$P^0(\bar{b}, \bar{B}) = P^0_p(\bar{b}) + P^0_t(\bar{B} - \bar{b}) - P^0_p(\bar{b}) P^0_t(\bar{B} - \bar{b}).$$

A geometrical part of the firetube model imitates the one of the collective tube model^{/6/}. An advantage of this geometrical approach is that the absolute values of cross sections are determined without additional assumption (as opposed to the firestreak model). We have found a reasonable agreement (differences less than 15%) of calculated and experimental^{/7/} total inelastic cross sections. So, in the remaining part of our paper we shall concentrate on the firetube model. However, if the experimental values of the cross sections are used for normalization in the firestreak model, results of this model for <n>inel become close to those of the firetube model. Other results of the firetube to those to those to those to those to those model.

In the two tested models the nuclear thermodynamics of Ref.3 has been used, where, besides pions and deltas, light nuclei and resonances have been considered. We took a sharp Δ mass and, instead of $\eta_{\min,\max}(\eta = a_p/(a_p + a_1))$ with $a_{p,t}$ the number of nucleons from the projectile (target) tube), we used a cutoff for 939 MeV mass per baryon of fireobject, see Ref.4. We fixed the ratio of the charge to the baryon number equal to that of the whole system. When thermal equilibrium is assumed to be achieved, the systems decay at some critical density, ρ_c . The parameters of particle distributions (temperatures and chemical potentials) are fixed on the assumption of chemical equilibrium, charge, baryon number and energy densities conservation.

Colliding objects (streaks or tubes) are usually assumed to stop in their CM system, i.e., they lose their momenta complletely and the total kinetic energy undergoes thermalization (full thermalization case). In Fig.1 are presented average multiplicities of π^{-1} mesons produced in collisions of ⁴He and 12 C nuclei with various nuclear targets from 6 Li to 207 Pb $^{/7-9/}$. The dash-dotted lines correspond to the assumption of full thermalization. Results of the model differ from experimental values of $\langle n \rangle^{inel}$ by a factor of about 2 and exhibit a too steep rise with target mass number. Let us discuss the sensitivity of this result to the assumptions of the model. In our calculations we have used the value of critical density ρ_c = = 0.12 fm⁻³ as in Ref.3. The increase of ρ_c slightly decreases the number of produced pions as discussed in Ref.10. The number of pions obtained from the calculations is sensitive to the choice of particles and resonances taken into account in the thermalization process. Taking into account nucleon resonances affects the number of pions only insignificantly $\frac{10}{}$. Some decrease of < n > inel values can be obtained if one takes into account strange particle production. This leads to the change of the results by less than 10% in the collisions studied.

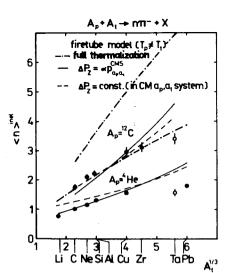


Fig.1. The average multiplicities, <n> inel, of π^- mesons (normalized to σ^{inel}) versus the target mass number, $A^{1/3}$. Experimental points (•) from Ref.7 and (o) from Ref.9.

Trying to explain the anisotropy of angular distributions of particles produced in ¹²C-¹²C central collisions,Das Gupta has assumed ^{/11}/ that nuclear matter is partly transparent, i.e., the colliding objects do not stop completely but lose only some fraction of their longitudinal momenta. The colliding parts of projectile

and target independently undergo thermalization and finally decay separately. The temperatures of colliding fireobjects from projectile and target are, of course, different $(T_n \neq T_i)$.

Following Das Gupta idea, we introduce the transparency to describe pion multiplicity.

The momentum loss of the colliding objects in thermodynamic models can take the form:

$$\Delta P_z = f(a_p, a_t, P^{CMS})$$

 P^{CMS} is the center of mass incident momentum. If the interaction of the objects is assumed to be coherent, it would be appropriate to study the momentum loss in the CM of the objects. If, on the other hand, the momentum loss is assumed to occur in separate nucleon-nucleon interactions, it is better to study the momentum loss in the nucleon-nucleon CM system.

We have considered five one-free-parameter forms of the function $f(a_p, a_t, P^{CMS})$ (a is a free parameter).

i) The nucleons undergo multiple scattering losing in each interaction a constant amount $_{\alpha}P_{NN}^{CMS}$ of their momenta^{/4/},

 $\Delta P_{z} = \alpha P_{NN}^{CMS} a_{p} a_{t}^{t}.$

ii) The nucleons undergo multiple scattering losing in each interaction a constant fraction α of their momenta,

$$\Delta \mathbf{P}_{\mathbf{z}} = \mathbf{P}_{\mathbf{a}_{\mathbf{p}}\mathbf{a}_{\mathbf{t}}}^{\mathbf{CMS}} [1 - \exp(-a(\mathbf{a}_{\mathbf{p}} + \mathbf{a}_{\mathbf{t}}))].$$

iii) The nucleons from target and projectile tubes interact coherently. During the collision the tubes lose a con-

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stant amount of their momenta (dashed lines in Fig.1)

 $\Delta P_z = \text{const} (\text{in CM} a_p, a_t \text{ system}).$

iv) The tubes interact coherently and lose a constant fraction of their momenta (solid lines in Fig.1),

$$\Delta P_{z} = \alpha P_{a_{b}a_{t}}^{CMS}$$

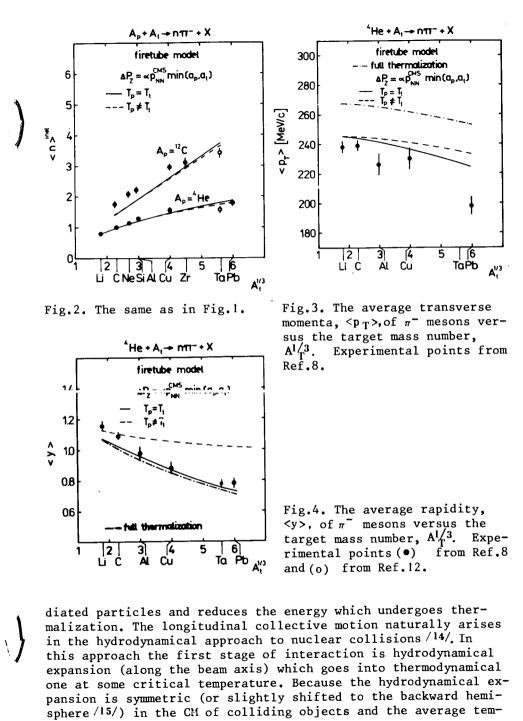
 v) The nucleon passing through a nucleus can interact only once with one of the nucleons of the target nucleus (dashed lines in Fig.2),

$$\Delta P_{z} = \alpha P_{NN}^{CMS} \cdot \min(a_{p}, a_{t})$$

In cases i) and ii) (not presented in figures) we have obtained the reduction of the value of $\langle n \rangle^{inel}$ by fitting parameter a. However, the increase of multiplicity with target mass number is as strong as for the full thermalization case. A weaker dependence on A_{T} has been found for cases iii) and iv), but the agreement with experimental data is not satisfactory (see Fig.1), We have found a reasonable description of multiplicity only for v)case(a = 0.47, Fig. 2, $T_p \neq T_t$), where the momentum loss $(\Delta P,)$ is roughly independent of the target mass number. In figs.3 and 4 we compare results of calculations, performed with such a momentum loss function (dashed lines, $T_p \neq T_1$), with data $^{/8,12/}$ concerning $< p_T >$ and < y > of negative pions.A significant disagreement has been found in the rapidity case. This discrepancy can be removed on the unphysical assumption that, despite the existence of transparency, the temperatures of the projectile and target fireobjects are equal $(T_p = T_t)$. On such an unphysical assumption a good agreement with <y> values has been found, whereas the model predictions concerning $\langle n \rangle^{inel}$ and $\langle p_{\tau} \rangle$ have been slightly changed (solid lines in Fig.2,3 and 4).

We have also found an agreement of the experimental values of $\langle y \rangle$ with those calculated under the assumption of full thermalization (see Fig.4). This means that the effective center of mass of produced pions is equal to the center of mass of colliding objects. So, if we assume that pions are emitted by two sources, the temperatures of the sources have to be equal/13/. Because the transparency leads to different temperatures of the fireobjects from target and projectile (independently of the form of the function ΔP_z), this idea is in <u>contradiction</u> with data concerning $\langle y \rangle$ of pions.

What is really needed for a description of various experimental data in the frame of thermodynamical models is the longitudinal collective motion of excited nuclear matter in the own center of mass. Such a motion introduces the anisotropy of ra-



peratures of parts of matter expanding forward and backward are equal, the average rapidity of produced pions should be zero in the CM of colliding objects. So, an agreement with the experimental data has to be obtained.

We conclude as follows:

1. The idea of transparency of nuclear matter is in disagreement with data.

2. The difficulties which arise at the thermodynamical description of pion production without transparency (too weak anisotropy of produced particles, overestimation of pion multiplicities and too high transverse momenta) can be overcome if the first stage of nuclear collisions at high energy is assumed to be governed by hydrodynamics.

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- 5. In our calculations we have used the following density distribution function

$$\rho(\mathbf{r}) = \rho_0 \begin{cases} [1 - (1 + R/a) \frac{\operatorname{sh} (\mathbf{r}/a)}{\mathbf{r}/a} \exp(-R/a)]; & \mathbf{r} \leq R \\ \\ [[R/a \operatorname{ch} (R/a) - \operatorname{sh}(R/a)] \frac{\exp(-\mathbf{r}/a)}{\mathbf{r}/a}]; & \mathbf{r} \geq R \end{cases},$$

where R = 1.18 A^{1/3} fm, $\rho_0 = 0.145$ fm⁻³ and $a = \sqrt{1/2}$. 6. Afek Y. et al. Nuovo Cim., 1978, A43, p.485. 7. Aksinenko C.D. et al. Nucl.Phys., 1980, A348, p.518. 8. Abdurakhimov A.Kh. et al. Nucl.Phys., 1981, A362, p.379. 9. Abdurakhmanov E.O. et al. Z.Phys., 1980, C56, p.1.

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13. The number of pions emitted from the source is a function of its temperature, f(T), and is proportional to mass, M, of the source. So, the average rapidity of pions radiated from two sources can be described by the formula:

$$\langle y \rangle = \frac{f(T_1)M_1y_1 + f(T_2)M_2y_2}{f(T_1)M_1 + f(T_2)M_2}$$

where y_i is the rapidity of an *i*-th source. If we require $\langle y \rangle = 0$ in the CM of the sources, where $M_1 y_1 = M_2 y_2$ (good approximation for $|M_1 - M_2|$ or $|y_1| + |y_2|$ not too high), we get $f(T_1) = f(T_2)$. So, $T_1 = T_2$.

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Васкотрены термодинанические модели с разными вариантами прозрат дериого вещества. Показано, что введение прозрачности хотя и заметно улучшает согласие с данными по множественности и поперечным импульсам ракоменных пионов, приводит к существенному расхождению с экспериментал ными данными по средней быстроте пионов. Приводятся существование по динамического расширения на первой стадии столкновения ядер. Paбота выполнена в Лаборатории высоких энергий ОИЯИ. Cooбщение Объединенного института ядерных исследований. Дубна 1983 Gaździcki M., Mrøwczyński S. E2-83-548 Difficulties of the Thermodynamical Model Approach to Pion Production in Relativistic Ion Collisions E2-83-548 Thermodynamical models with various forms of partial transparency nuclear matter are considered. It is shown that the introduction of tra parency, however, significantly improves agreement with pion data come ning multiplicities and transverse momenta, leads to a serious discreg vith average rapidity of pions. Qualitative arguments are given that of fuculties of the thermodynamical approach can be overcome If one assur- nydrodynamical expansion in the first stage of nuclear interactions. The Investigation has been performed at the Laboratory of High tergies, JINR.	Газдзицки М., Мрувчински С. Проблемы термодинамического подх в столкновениях релятивистских и	
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