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ДУБНА



G-22

20/1-75

E2 - 8223

136/2-75

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ON RELATIVISTIC FORM FACTORS
OF MANY-BODY SYSTEMS

1974

ЛАБОРАТОРИЯ
ТЕОРЕТИЧЕСКОЙ ФИЗИКИ

E2 - 8223

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Submitted to TMΦ



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E2 - 8223

О релятивистских формфакторах многочастичных систем

Получены выражения для релятивистских формфакторов многочастичных систем в рамках квазипотенциального подхода в переменных "светового фронта".

Препринт Объединенного института ядерных исследований.

Дубна, 1974

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E2 - 8223

On Relativistic Form Factors of Many-Body Systems

The "light-front" form of the quasipotential approach in quantum field theory is applied for constructing the relativistic form factors of many-body composite systems.

Preprint. Joint Institute for Nuclear Research.
Dubna, 1974

1. Introduction

In refs. /¹⁻⁵/ a problem of constructing form factors of composite particles has been considered. The consideration was based on the Logunov-Tavkhelidze quasipotential approach in quantum field theory /⁶. Expressions for the form factors in the case of two constituents have been obtained in terms of the relativistically covariant quasipotential quantities /⁷. In ref. /⁵/ the two-particle quasipotential formalism has been developed in terms of the "light-front" variables /⁸/ and a method for calculating form factors has been outlined.

In the present paper following methods of refs. /¹⁻⁵/ we consider the case of many-body systems.

Let us recall some aspects of the method of refs. /¹⁻⁵/ for completeness. Wave functions, in terms of which the form factors of composite particles are expressed, depend on values of the Bethe-Salpeter amplitudes $x_{P,a}(x_\mu)$ on definite hyperplanes. In the case of the "light-front" variables quasipotential wave functions $\Phi_{P,a}(x, \vec{p}_\perp)$ /⁵/ depend on values of the Bethe-Salpeter amplitude on the hyperplane

$$x_0 + x_3 = 0 \quad (1.1)$$

and obey the following equation:

$$[P^2 - \frac{(\vec{p}_\perp + (1/2-x)\vec{P}_\perp)^2 + m_1^2}{x} - \frac{(\vec{p}_\perp + (1/2-x)\vec{P}_\perp)^2 + m_2^2}{1-x}] \Phi_{P,a}(x, \vec{p}_\perp) = \\ = \int_0^1 \frac{dx'}{x'(1-x')} \int d\vec{p}'_\perp V(P; x, \vec{p}_\perp; x', \vec{p}'_\perp) \Phi_{P,a}(x', \vec{p}'_\perp). \quad (1.2)$$

Here

$$\Phi_{P,a}(x, \vec{p}_\perp) = P_+ x (1-x) \Psi_{P,a}(p_+, \vec{p}_\perp) \quad (1.3a)$$

$$\Psi_{P,a}(p_+, \vec{p}_\perp) = \frac{1}{(2\pi)^3} \int d^4x \delta(x_+) e^{i(p_+ x - \vec{p}_\perp \cdot \vec{x}_\perp)} X_{P,a}(x_\mu) \quad (1.3b)$$

P and p are total and relative momentum of the two-body system, respectively. The variable x is introduced in the following way:

$$x = \frac{1}{2} + \frac{p_+}{P_+} = \frac{1}{2} + \frac{p_0 + p_3}{p_0 + p_3}. \quad (1.4)$$

2. Equation of the Quasipotential Type for N Interacting Particles

We define the Fourier transform of the N -particle Bethe-Salpeter amplitude as

$$\delta^{(4)}(P - \sum_{i=1}^N p^{(i)}) X_{P,a}([p^{(i)}]) = \\ = \int \prod_{i=1}^N d^4x^{(i)} e^{i \sum_{i=1}^N (p^{(i)} \cdot x^{(i)})} X_{P,a}([x_\mu^{(i)}]). \quad (2.1)$$

Here

$$[p^{(i)}] = p^{(1)}, \dots, p^{(N)}; [x_\mu^{(i)}] = x_\mu^{(1)}, \dots, x_\mu^{(N)}. \quad (2.2)$$

Introducing the "light-front" variables

$$P_\pm = P_0 \pm P_3; p_\pm^{(i)} = p_0^{(i)} \pm p_3^{(i)}; x_\pm^{(i)} = \frac{x_0^{(i)} + x_3^{(i)}}{2} \quad (2.3)$$

and integrating (2.1) over $\prod_{i=1}^N dp_\pm^{(i)}$ we obtain

$$2\delta(P_+ - \sum_{i=1}^N p_+^{(i)}) \delta^{(2)}(\vec{P}_\perp - \sum_{i=1}^N \vec{p}_\perp^{(i)}) \Psi_{P,a}([p_+^{(i)}, \vec{p}_\perp^{(i)}]) = \quad (2.4) \\ = (2\pi)^N \int \prod_{i=1}^N d^4x^{(i)} \delta(x_+^{(i)}) e^{i \sum_{i=1}^N (p_+^{(i)} x_\perp^{(i)} - \vec{p}_\perp^{(i)} \cdot \vec{x}_\perp^{(i)})} X_{P,a}([x_\mu^{(i)}]).$$

The function $\Psi_{P,a}([p_+^{(i)}, \vec{p}_\perp^{(i)}])$ is related to the Bethe-Salpeter amplitude in the following manner:

$$\Psi_{P,a}([p_+^{(i)}, \vec{p}_\perp^{(i)}]) = \int_{-\infty}^{\infty} \prod_{i=1}^N dp_-^{(i)} \delta(P_- - \sum_{i=1}^N p_-^{(i)}) X_{P,a}([p_-^{(i)}]). \quad (2.5)$$

Let us introduce the Fourier transform of the "two-time" Green function

$$\bar{G}(P; [p_+^{(i)}, \vec{p}_\perp^{(i)}], [p_+^{(i)'}, \vec{p}_\perp^{(i)'}]) = \\ = \int_{-\infty}^{\infty} \prod_{i=1}^N dp_-^{(i)} dp_-^{(i)'} \delta(P_- - \sum_{i=1}^N p_-^{(i)}) G(P; [p_-^{(i)}], [p_-^{(i)'}])$$

$G(P; [p_-^{(i)}], [p_-^{(i)'}])$ is defined by the relation

$$G([x_\mu^{(i)}], [x_\mu^{(i)'}]) = \langle 0 | T(\phi_1(x_\mu^{(1)}), \dots, \phi_N(x_\mu^{(N)}), \phi_1(x_\mu^{(1)'}) \dots \\ \phi_N(x_\mu^{(N)'})) | 0 \rangle =$$

$$= \frac{1}{(2\pi)^{4N}} \int \prod_{i=1}^N d^4 p_i^{(i)} d^4 p_i^{(i)'} e^{-i \sum_{i=1}^N (p_i^{(i)} - p_i^{(i)'}) \cdot x^{(i)}} \times \\ \times G(P; [p_i^{(i)}], [p_i^{(i)'}]). \quad (2.7)$$

For the case of free particles we have

$$G^{(0)}(P; [p_i^{(i)}], [p_i^{(i)'}]) = \frac{i^N \prod_{i=1}^N \delta^{(4)}(p_i^{(i)} - p_i^{(i)'})}{\prod_{i=1}^N (p_i^{(i)2} - m_i^{(i)2} + i\epsilon)}. \quad (2.8)$$

Integrating both sides of eq. (2.8) according to the definition (2.6), we get

$$\tilde{G}^{(0)}(P; [p_+^{(i)}, \vec{p}_\perp^{(i)}], [p_+^{(i)'}, \vec{p}_\perp^{(i)'}]) = \quad (2.9)$$

$$= \prod_{i=1}^N \theta(x^{(i)}) \theta(1-x^{(i)}) \tilde{G}^{(0)}(P; [p_+^{(i)}, \vec{p}_\perp^{(i)}], [p_+^{(i)'}, \vec{p}_\perp^{(i)'}]),$$

where

$$\begin{aligned} \tilde{G}^{(0)}(P; [p_+^{(i)}, \vec{p}_\perp^{(i)}], [p_+^{(i)'}, \vec{p}_\perp^{(i)'}]) &= \\ &= \frac{(2i)^N (2\pi i)^{N-1} \prod_{i=1}^N \delta(p_+^{(i)} - p_+^{(i)'}) \delta^{(2)}(\vec{p}_\perp^{(i)} - \vec{p}_\perp^{(i)'})}{p_+^{N-1} \prod_{i=1}^N x^{(i)} [P^2 - \sum_{i=1}^N \frac{(\vec{p}_\perp^{(i)} - x^{(i)} \vec{p}_\perp^{(i)})^2 + m_i^{(i)2}}{x^{(i)}}]} \equiv \\ &\equiv \tilde{G}^{(0)}(P; [p_+^{(i)}, \vec{p}_\perp^{(i)}]) \prod_{i=1}^N \delta(p_+^{(i)} - p_+^{(i)'}) \delta^{(2)}(\vec{p}_\perp^{(i)} - \vec{p}_\perp^{(i)'}). \end{aligned} \quad (2.10)$$

The variables $x^{(i)}$ are defined by the following formula

$$x^{(i)} = \frac{p_+^{(i)}}{P_+}. \quad (2.11)$$

Thus, the function $\tilde{G}^{(0)}(P; [p_+^{(i)}, \vec{p}_\perp^{(i)}])$ is defined under the conditions

$$\sum_{i=1}^N x^{(i)} = 1; \quad 0 < x^{(i)} < 1; \quad \sum_{i=1}^N \vec{p}_\perp^{(i)} = \vec{P}_\perp. \quad (2.12)$$

Let us introduce now the inverse operator \tilde{G}^{-1} by means of the relation

$$\begin{aligned} &\int_0^P \prod_{i=1}^N d p_+^{(i)''} \int \prod_{i=1}^N d \vec{p}_\perp^{(i)''} \tilde{G}^{-1}(P; [p_+^{(i)}, \vec{p}_\perp^{(i)}], [p_+^{(i)''}, \vec{p}_\perp^{(i)''}]) \times \\ &\times \tilde{G}(P; [p_+^{(i)''}, \vec{p}_\perp^{(i)''}], [p_+^{(i)'}, \vec{p}_\perp^{(i)'})] = \prod_{i=1}^N \delta(p_+^{(i)} - p_+^{(i)'}) \times \\ &\times \delta^{(2)}(\vec{p}_\perp^{(i)} - \vec{p}_\perp^{(i)'}) \end{aligned} \quad (2.13)$$

and define the quasipotential V :

$$\begin{aligned} \tilde{G}^{-1}(P; [p_+^{(i)}, \vec{p}_\perp^{(i)}], [p_+^{(i)'}, \vec{p}_\perp^{(i)'})] &= \\ &= \tilde{G}^{(0)-1}(P; [p_+^{(i)}, \vec{p}_\perp^{(i)}], [p_+^{(i)'}, \vec{p}_\perp^{(i)'})] - \\ &- \frac{\delta(P_+ - \sum_{i=1}^N p_+^{(i)}) \delta^{(2)}(\vec{p}_\perp - \sum_{i=1}^N \vec{p}_\perp^{(i)})}{(2i)^N (2\pi i)^{N-1}} V(P; [p_+^{(i)}, \vec{p}_\perp^{(i)}], [p_+^{(i)'}, \vec{p}_\perp^{(i)'})]. \end{aligned} \quad (2.14)$$

The equation for the wave function

$$\Phi_{P,a}([x^{(i)}, \vec{p}_\perp^{(i)}]) = P_+^{N-1} \prod_{i=1}^N x^{(i)} \Psi_{P,a}([p_+^{(i)}, \vec{p}_\perp^{(i)}]) \quad (2.15)$$

looks as follows

$$[P^2 - \sum_{i=1}^N \frac{(\vec{p}_\perp^{(i)} - x^{(i)} \vec{p}_\perp^{(i)})^2 + m_i^{(i)2}}{x^{(i)}}] \Phi_{P,a}([x^{(i)}, \vec{p}_\perp^{(i)}]) =$$

$$= \int_0^{\infty} \frac{\prod_{i=1}^N dx^{(i)'} \delta(1 - \sum_{i=1}^N x^{(i)'})}{\prod_{i=1}^N x^{(i)'}} \int \prod_{i=1}^N dp_{\perp}^{(i)'} \delta^{(2)}(\vec{p}_{\perp} - \sum_{i=1}^N \vec{p}_{\perp}^{(i)'}) \times \\ \times V(P; [x^{(i)}, \vec{p}_{\perp}^{(i)}], [x^{(i)'}, \vec{p}_{\perp}^{(i)'})] \Phi_{P,\alpha}([x^{(i)'}, \vec{p}_{\perp}^{(i)'})]. \quad (2.16)$$

In the next section a formalism developed here is applied for constructing the relativistic form factors of many-body systems. An analysis of the equation obtained and some of its applications will be given elsewhere.

3. Form Factors of Composite Particles

In the present section we develop a method for constructing relativistic form factors of composite particles in terms of the quasipotential wave functions (2.5), (2.15).

Consider the quantity R , which is defined by the vacuum expectation value of the chronologically ordered product of the Heisenberg field operators $\phi_i(x_\mu^{(i)})$ and a local current $J(x)$

$$R([x_\mu^{(i)}], [y_\mu^{(i)}]) = \langle 0 | T(\phi_1(x_\mu^{(1)}) \dots \phi_N(x_\mu^{(N)}) J(0) \times \\ \times \phi_1^+(y_\mu^{(1)}) \dots \phi_N^+(y_\mu^{(N)})) | 0 \rangle = \\ = \frac{1}{(2\pi)^{4N}} \int \prod_{i=1}^N d^4 p^{(i)} d^4 q^{(i)} e^{-i \sum_{i=1}^N p^{(i)} x^{(i)} - i \sum_{i=1}^N q^{(i)} y^{(i)}} \times \\ \times R([p^{(i)}], [q^{(i)}]). \quad (3.1)$$

The quantity R can be presented in the form ^{/9/}

$$R = G \Gamma G, \quad (3.2)$$

where G is the Green function of the fields $\phi_i(x_\mu^{(i)})$

$$G([x_\mu^{(i)}], [y_\mu^{(i)}]) = \langle 0 | T(\phi_1(x_\mu^{(1)}) \dots \phi_N(x_\mu^{(N)}) \times \\ \times \phi_1^+(y_\mu^{(1)}) \dots \phi_N^+(y_\mu^{(N)})) | 0 \rangle \quad (3.3)$$

and the vertex function Γ is defined by the sum of the irreducible diagrams for the $(2N+1)$ -point function (3.1) (Fig. 1)

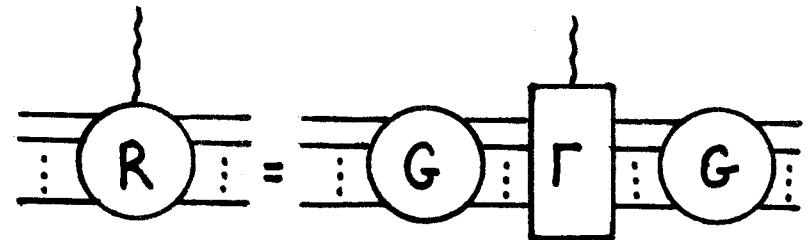


Fig. 1

Proceedings now to the quasipotential description we introduce the quantity $\tilde{R}([p_{\perp}^{(i)}, \vec{p}_{\perp}^{(i)}], [q_{\perp}^{(i)}, \vec{q}_{\perp}^{(i)}])$ by the relation

$$\tilde{R}([p_{\perp}^{(i)}, \vec{p}_{\perp}^{(i)}], [q_{\perp}^{(i)}, \vec{q}_{\perp}^{(i)}]) = \\ = \int_{-\infty}^{\infty} \prod_{i=1}^N d p_{\perp}^{(i)} d q_{\perp}^{(i)} \delta(p_{\perp} - \sum_{i=1}^N p_{\perp}^{(i)}) \delta(q_{\perp} - \sum_{i=1}^N q_{\perp}^{(i)}) \times \quad (3.4) \\ \times R([p^{(i)}], [q^{(i)}])$$

and write it in the form

$$\tilde{R} = \tilde{G} \tilde{\Gamma} \tilde{G}. \quad (3.5)$$

Multiplication in formula (3.5) has to be understood in the operator sense:

$$\begin{aligned} \tilde{A} \tilde{B} &= \int \prod_{i=1}^N dq_+^{(i)}' dq_\perp^{(i)}' \delta(Q_+ - \sum_{i=1}^N q_+^{(i)}') \delta^{(2)}(\vec{Q}_\perp - \sum_{i=1}^N \vec{q}_\perp^{(i)}') \times \\ &\times \tilde{A}([p_+^{(i)}, \vec{p}_\perp^{(i)}], [q_+^{(i)}', \vec{q}_\perp^{(i)}']) \tilde{B}([q_+^{(i)}', \vec{q}_\perp^{(i)}'], [q_+^{(i)}, \vec{q}_\perp^{(i)}]). \end{aligned} \quad (3.6)$$

From the spectral properties of the function R it follows that \tilde{R} possesses the double pole singularities

$$\begin{aligned} \tilde{R}([p_+^{(i)}, \vec{p}_\perp^{(i)}], [q_+^{(i)}, \vec{q}_\perp^{(i)}]) &\approx \\ P^2 \rightarrow M_\alpha^2, Q^2 \rightarrow M_\beta^2 \end{aligned} \quad (3.7)$$

$$\approx [i(2\pi)^4]^2 \frac{\Psi_{P,\alpha}([p_+^{(i)}, \vec{p}_\perp^{(i)}]) \langle P, \alpha | J(0) | Q, \beta \rangle \Psi_{Q,\beta}^+([q_+^{(i)}, \vec{q}_\perp^{(i)}])}{(P^2 - M_\alpha^2)(Q^2 - M_\beta^2)}$$

in the vicinity of the points, where N -particle system forms bound states with masses M_α and M_β and a set of other quantum numbers α and β , respectively.

On the other hand knowing the pole singularities of the Green function

$$\begin{aligned} \tilde{G}([p_+^{(i)}, \vec{p}_\perp^{(i)}], [q_+^{(i)}, \vec{q}_\perp^{(i)}]) &\approx \\ i(2\pi)^4 \frac{\Psi_{P,\alpha}([p_+^{(i)}, \vec{p}_\perp^{(i)}]) \Psi_{P,\alpha}^+([q_+^{(i)}, \vec{q}_\perp^{(i)}])}{P^2 - M_\alpha^2} \end{aligned} \quad (3.8)$$

one can cast formula (3.5) into the form

$$\begin{aligned} \tilde{R}([p_+^{(i)}, \vec{p}_\perp^{(i)}], [q_+^{(i)}, \vec{q}_\perp^{(i)}]) &\approx \\ \approx [i(2\pi)^4]^2 \frac{\Psi_{P,\alpha}([p_+^{(i)}, \vec{p}_\perp^{(i)}]) \Psi_{Q,\beta}^+([q_+^{(i)}, \vec{q}_\perp^{(i)}])}{(P^2 - M_\alpha^2)(Q^2 - M_\beta^2)} \times \\ \times \int \prod_{i=1}^N dp_+^{(i)} dp_\perp^{(i)} \delta(P_+ - \sum_{i=1}^N p_+^{(i)}) \delta^{(2)}(\vec{P}_\perp - \sum_{i=1}^N \vec{p}_\perp^{(i)}) \times \\ \times \int \prod_{i=1}^N dq_+^{(i)} dq_\perp^{(i)} \delta(Q_+ - \sum_{i=1}^N q_+^{(i)}) \delta^{(2)}(\vec{Q}_\perp - \sum_{i=1}^N \vec{q}_\perp^{(i)}) \times \\ \times \Psi_{P,\alpha}^+([p_+^{(i)}, \vec{p}_\perp^{(i)}]) \tilde{\Gamma}_{\alpha\beta}([p_+^{(i)}, \vec{p}_\perp^{(i)}], [q_+^{(i)}, \vec{q}_\perp^{(i)}]) \times \\ \times \Psi_{Q,\beta}^+([q_+^{(i)}, \vec{q}_\perp^{(i)}]). \end{aligned} \quad (3.9)$$

Here

$$\begin{aligned} \tilde{\Gamma}_{\alpha\beta}([p_+^{(i)}, \vec{p}_\perp^{(i)}], [q_+^{(i)}, \vec{q}_\perp^{(i)}]) &= \\ = \lim_{P^2 \rightarrow M_\alpha^2, Q^2 \rightarrow M_\beta^2} \int \prod_{i=1}^N dp_+^{(i)} dp_\perp^{(i)} \delta(P_+ - \sum_{i=1}^N p_+^{(i)}) \delta^{(2)}(\vec{P}_\perp - \sum_{i=1}^N \vec{p}_\perp^{(i)}) \times \\ \times \prod_{i=1}^N dp_+^{(i)\prime\prime} dp_\perp^{(i)\prime\prime} \delta(Q_+ - \sum_{i=1}^N p_+^{(i)\prime\prime}) \delta^{(2)}(\vec{Q}_\perp - \sum_{i=1}^N \vec{p}_\perp^{(i)\prime\prime}) \times \\ \times \tilde{G}^{-1}([p_+^{(i)}, \vec{p}_\perp^{(i)}], [p_+^{(i)\prime\prime}, \vec{p}_\perp^{(i)\prime\prime}]) \times \\ \times G \Gamma G([p_+^{(i)\prime\prime}, \vec{p}_\perp^{(i)\prime\prime}], [p_+^{(i)\prime\prime}, \vec{p}_\perp^{(i)\prime\prime}]) \times \\ \times \tilde{G}^{-1}([p_+^{(i)\prime\prime}, \vec{p}_\perp^{(i)\prime\prime}], [q_+^{(i)}, \vec{q}_\perp^{(i)}]). \end{aligned} \quad (3.10)$$

Comparing (3.7) with the (3.9) we arrive at the following expression for the matrix element of the bound state current:

$$\begin{aligned} \langle \mathbf{P}, \alpha | \mathbf{J}(0) | \mathbf{Q}, \beta \rangle &= \int \prod_{i=1}^N d\mathbf{p}_+^{(i)} d\vec{\mathbf{p}}_+^{(i)} \delta(\mathbf{P}_+ - \sum_{i=1}^N \mathbf{p}_+^{(i)}) \times \\ &\times \delta^{(2)}(\vec{\mathbf{p}}_\perp - \sum_{i=1}^N \vec{\mathbf{p}}_+^{(i)}) \times \\ &\times \prod_{i=1}^N d\mathbf{q}_+^{(i)} d\vec{\mathbf{q}}_\perp^{(i)} \delta(\mathbf{Q}_+ - \sum_{i=1}^N \mathbf{q}_+^{(i)}) \delta^{(2)}(\vec{\mathbf{Q}}_\perp - \sum_{i=1}^N \vec{\mathbf{q}}_\perp^{(i)}) \times \\ &\times \Psi_{\mathbf{P}, \alpha}^+([\mathbf{p}_+^{(i)}, \vec{\mathbf{p}}_\perp^{(i)}]) \tilde{\Gamma}_{\alpha\beta}([\mathbf{p}_+^{(i)}, \vec{\mathbf{p}}_\perp^{(i)}], [\mathbf{q}_+^{(i)}, \vec{\mathbf{q}}_\perp^{(i)}]) \times \\ &\times \Psi_{\mathbf{Q}, \beta}([\mathbf{q}_+^{(i)}, \vec{\mathbf{q}}_\perp^{(i)}]). \end{aligned} \quad (3.11)$$

The vertex operator $\tilde{\Gamma}_{\alpha\beta}$ can be constructed, using, for instance, perturbation theory methods of quantum field theory. Here we consider the so-called "impulse approximation" (Fig. 2)

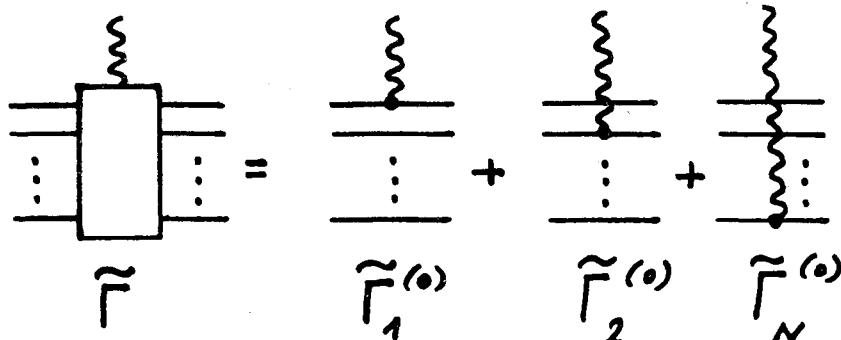


Fig. 2

In this case

$$\tilde{\Gamma}_\mu = \sum_{k=1}^N (\tilde{\Gamma}_\mu^{(0)})_k \quad (3.12a)$$

$$(\tilde{\Gamma}_\mu^{(0)})_k = [\tilde{G}^{(0)}]^{-1} [G^{(0)}(\Gamma_\mu^{(0)})_k G^{(0)}] [\tilde{G}^{(0)}]^{-1} \quad (3.12b)$$

Here

$$\begin{aligned} (\tilde{\Gamma}_\mu^{(0)})_k &= (2\pi)^4 Z_k (p^{(k)} + q^{(k)}) \prod_{j=1}^N \delta(p_j^{(j)} - q_j^{(j)}) \times \\ &\times [G^{(0)}(q^{(j)})]^{-1} \end{aligned} \quad (3.13a)$$

$$G^{(0)}([p^{(i)}]) = i \prod_{i=1}^N (p_i^{(i)2} - m_i^{(i)2} + i\epsilon)^{-1} \quad (3.13b)$$

$$G^{(0)}([q^{(i)}]) = i \prod_{i=1}^N (q_i^{(i)2} - m_i^{(i)2} + i\epsilon)^{-1} \quad (3.13c)$$

Z_k is the charge of k -th particle.

Performing integration in formula (3.12b) according to the definition (3.4), proceeding to the reference frame, where

$$\mathbf{P}_+ = \mathbf{Q}_+, \quad \vec{\mathbf{Q}}_+ = 0, \quad (\mathbf{P}_+ - \mathbf{Q}_+)^2 = \Delta^2 = -\vec{\Delta}_+^2 \quad (3.14)$$

and using the transformation properties of wave functions

$$\Psi_{\mathbf{P}, \alpha}^+([\mathbf{x}^{(i)}, \vec{\mathbf{p}}_\perp^{(i)}]) = \Psi_{\vec{\mathbf{p}}_+ = 0, \alpha}^+([\mathbf{x}^{(i)}, \vec{\mathbf{p}}_\perp^{(i)} - \mathbf{x}^{(i)} \vec{\mathbf{p}}_\perp]) \quad (3.15)$$

we obtain

$$\langle \mathbf{P}, \alpha | \mathbf{J}_\mu(0) | \mathbf{Q}, \beta \rangle = \sum_{k=1}^N \langle \mathbf{P}, \alpha | \mathbf{J}_\mu(0) | \mathbf{Q}, \beta \rangle_k, \quad (3.16)$$

where, for instance

$$\begin{aligned} \langle \mathbf{P}, \alpha | \mathbf{J}_\mu(0) | \mathbf{Q}, \beta \rangle_k &= (\mathbf{P}_+ + \mathbf{Q}_+) F_k(-\vec{\Delta}_+^2) = \\ &= \frac{-(2\pi)^4 Z_k (\mathbf{P}_+ + \mathbf{Q}_+)}{(2\pi i)^{N+1} (2\pi i)^{N-1}} \int_0^1 \frac{\prod_{i=1}^N dx_i^{(i)} \delta(1 - \sum_{i=1}^N x_i^{(i)})}{\prod_{i=1}^N x_i^{(i)}} \times \end{aligned}$$

$$\begin{aligned} & \times \int \prod_{i=1}^N d\vec{p}_+^{(i)} \delta^{(2)} \left(\sum_{i=1}^N \vec{p}_+^{(i)} \right) \times \\ & \times \Phi_{\vec{P}_+ = 0, \alpha}^+ ([x^{(i)}, \vec{p}_+^{(i)}] - x^{(i)} \vec{\Delta}_+)_{i \neq k}, x_k, \vec{p}_+^{(k)} + \\ & + (1-x) \vec{\Delta}_+) \Phi_{\vec{P}_+ = 0, \beta}^+ ([x^{(i)}, \vec{p}_+^{(i)}]). \end{aligned} \quad (3.17)$$

The wave functions $\Phi_{\vec{P}_+ = 0, \alpha}^+ ([x^{(i)}, \vec{p}_+^{(i)}])$ are defined by the formula (2.15).

Taking into account the normalization condition for the wave functions

$$\begin{aligned} & i(2\pi)^4 \int \prod_{i=1}^N d\vec{p}_+^{(i)} d\vec{p}_+^{(i)} \delta(P_+ - \sum_{i=1}^N \vec{p}_+^{(i)}) \delta^{(2)}(\vec{P}_+ - \sum_{i=1}^N \vec{p}_+^{(i)}) \times \\ & \times \prod_{i=1}^N dq_+^{(i)} d\vec{q}_+^{(i)} \delta(Q_+ - \sum_{i=1}^N q_+^{(i)}) \delta^{(2)}(\vec{Q}_+ - \sum_{i=1}^N \vec{q}_+^{(i)}) \times \\ & \times \Psi_{P, \alpha}^+ ([p_+^{(i)}, \vec{p}_+^{(i)}]) \frac{\partial \tilde{G}^{-1}(P; [p_+^{(i)}, \vec{p}_+^{(i)}], [q_+^{(i)}, \vec{q}_+^{(i)}])}{\partial P^2} \times \\ & \times \Psi_{Q, \beta}^+ ([q_+^{(i)}, \vec{q}_+^{(i)}]) = 1 \end{aligned} \quad (3.18)$$

for $\vec{\Delta}_+ = 0$ we get

$$F(\Delta^2 = 0) = \frac{1}{2} \sum_{k=1}^N Z_k. \quad (3.19)$$

Thus formulas (3.16); (3.17) define the form factors of a many-body system in terms of the quasipotential wave functions

$$\Phi_{\vec{P}_+ = 0, \alpha}^+ ([x^{(i)}, \vec{p}_+^{(i)}]).$$

The authors express their gratitude to N.N.Bogolubov, A.A.Logunov, A.N.Tavkhelidze for stimulating discussions and valuable remarks, to R.N.Faustov, V.G.Kadyshevsky, A.A.Khelashvili, S.P.Kuleshov, A.N.Kvinikhidze, M.D.Mateev, R.M.Mir-Kasimov, R.M.Muradyan, A.N.Sissakian, L.A.Slepchenko for fruitful discussions.

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Received by Publishing Department
on August 23, 1974.