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# AN INSIGHT INTO THE PARITY <br> VIOLATION 

AT $\pi$ NN VERTEX

[^0]In this paper we consider the parity violating (PV) $\pi N N v e r-$ tex parametrized in the usual way

$$
\begin{equation*}
\left\langle\pi^{-} \mathrm{p}\right| \mathcal{H}^{\mathrm{PV}}|\mathrm{n}\rangle=\mathrm{iGm}_{\pi}^{2} \mathrm{~A}_{\pi} \phi_{\pi} \overline{\mathrm{u}}_{\mathrm{p}} \mathrm{u}_{\mathrm{n}}, \tag{1}
\end{equation*}
$$

where $\mathcal{H}^{P V}$ is the effective Hamiltonian of the PV hadron-hadron interactions. Interest in the constant $A_{\pi}$ stems from the fact that it determines the long-range ( $\mathrm{r} \sim 1.4 \mathrm{fm}$ ) part of the PVNN potential with $\Delta I=1$. These properties enable $A_{\pi}$ to be separated, for instance, from the experiments on observation of $P V$ in the electromagnetic nuclear transitions. Taking into account the theoretical uncertainties while extracting from experiments, the value of $A_{\pi}^{\exp }$ is in the interval (1.5, 2.5) $1 /$.

The theoretical evaluation of $A_{\pi}$ is difficult because the Hamiltonian $\mathcal{H}^{P V}$ is formulated in terms of the quark operators. For the local hamiltonian $\mathcal{H P V}^{\mathrm{PV}}$ the structure of the vertex (1) is shown in the figure. Two different methods are usually used to calculate $A_{\pi}$. The first one is based on the PCAC and $\operatorname{SU}(3)^{/ 2 /}$ and expresses a part of the amplitude (1), defined by the equal time commutator (ETC) in the standard technique of soft pions, $A_{\pi}^{E T C}$, through the ETC-parts of $s$-wave amplitudes of the decays $\Lambda^{\circ} \rightarrow \pi^{-} p$ and $\exists \exists^{-} \Lambda^{\circ}$ with $\Delta S=1$. However, this method can be applied just to the part $H_{\Delta \mathrm{PV}=0}^{\mathrm{PV}}$, which has the $\operatorname{SU}(3)$ partner in $H_{\Delta S=1}^{\mathrm{PV}}$. According to the estimates of ref. ${ }^{\prime 3 /} \mathrm{A}_{\pi}^{\mathrm{ETC}} \approx 1$.

The second method ${ }^{/ 4,3 /}$ allows one to calculate the part of the amplitude (1) which corresponds to the factorizing (F) diagrams (d) of the figure, $A_{\pi}^{F}$. The method assumes factorization $\cap f$


Quark structure of the $P V \pi N N$ vertex (1). The circle denotes the effective hamiltonian $\mathcal{H}^{P V}$; (a)-(c) are nonfactoriting (NF) and (d) factorizing (F) diagrams.

the amplitude (1) and applicability of free equations of motion to the quark fields. As a result, in $A_{\pi}^{F}$ there appears a factor $\mathrm{f}_{\pi} /\left(\mathrm{m}_{\mathrm{u}}+\mathrm{m}_{\mathrm{d}}\right)$ which amounts to $\sim 10$, if one uses the parameters of the chiral symmetry breaking $\mathrm{m}_{\mathrm{u}}+\mathrm{m}_{\mathrm{d}} \sim 10 \mathrm{MeV}^{15 /}$ as quark masses. The obtained value of $\mathbb{A}_{\pi}^{\mathrm{F}}$ is in the interval (1.5, $3.5)^{\prime 3 /}$ and may pretend to the explanation of $A_{\pi}^{\exp }$.

However, these methods of calculation of $A_{\pi}^{\pi}$ have the following unclear points:
i) interpretation of $A_{\pi}^{\text {ETC }}$ in terms of the diagrams of the figure; calculation of $A^{E T C}$ for the total hamiltonian $\mathcal{H}^{P V}$ in the standard electroweak model $\operatorname{SU}(2)_{\mathrm{L}} \otimes \mathrm{U}(1)$ (SEWM);
iii) dependence of the observable $A_{\pi}$ on the nonobservable points. parameters $\mathrm{m}_{\mathrm{v}}$ and $\mathrm{m}_{\mathrm{d}}$. We now proceed to consider these
I. Using PCAC, within the field-theoretical approach ${ }^{/ 6 /}$ one can show that the ETC--part of the amplitude (1) describes the nonfactorizing (NF) diagrams (a), (b) of the figure with $\mathrm{k}_{\pi} \rightarrow 0$, whereas the NF diagram (c) vanishes in this limit. Thus, $A_{\pi}^{\pi} * A_{\pi}^{N F}+A_{\pi}^{F}$, where $A^{N F} A^{E T C}$, The same can be referred to any amplitude $\left.<\pi \mathrm{B}^{\prime}\left|\mathcal{H}^{\mathrm{PV}}\right| \mathrm{B}\right\rangle$; in particular to $\mathrm{A}\left(\Lambda_{-}^{\circ}\right)$ and $\mathrm{A}\left(\Xi_{-}^{-}\right)$. This conclusion justifies the arguments of papers. 17,8 , and is proved in the Appendix.

$$
\text { II. From point } I \text { and ref:/2/ it follows that if the effec- }
$$ tive hamiltonian $\mathcal{H} \mathrm{PV}$ can be represented as

$$
\begin{equation*}
\mathcal{H}^{\mathrm{PV}}=c_{\Delta S=1} \mathcal{O}_{\Delta \mathrm{S}=1, \Delta \mathrm{I}=1 / 2^{+}}^{8} \quad{ }^{c} \Delta \mathrm{~S}=0=0 \mathcal{O}_{\Delta S=0, \Delta \mathrm{I}=1}^{8} \quad, \mathcal{O}_{\mathrm{k}}^{8} \in 8, \tag{2}
\end{equation*}
$$

then

$$
\begin{equation*}
A_{\pi}^{N F}=-\sqrt{\frac{2}{3}} c^{c}{ }^{c}{ }_{\Delta S=0}\left[2 A^{N F}\left(\Lambda^{\circ}\right)-A^{N F}\left(E_{-}\right)\right], \tag{3}
\end{equation*}
$$

where

$$
A^{N F}(H)=A^{e x p}(H)-A^{F}(H)
$$

Let us now show that owing to the penguin contributions/4/ to the effective hamiltonian $\mathcal{H}^{\mathrm{PV}}$ in the SEWM\&QCD, the matrix elements $\left.<\pi \mathrm{B}^{\prime}\left|\mathcal{H}^{\mathrm{PV}}\right| \mathrm{B}\right\rangle^{\mathrm{NF}}$ in the valence quark approximation satisfy condition (2). In the SEWM\&QCD in part of $\mathcal{H}^{P V}$ under consideration has the form $/ 4,3 /$

$$
\begin{equation*}
\mathcal{H}^{\mathrm{PV}}=\sqrt{2} \mathrm{G} \sum_{\mathrm{k}}\left(\mathrm{c}^{27} \mathcal{O}^{27}+\mathrm{c}^{\mathrm{S}} \mathcal{O}^{\mathrm{S}}+\mathrm{c}^{\mathrm{A}} \mathcal{O}^{\mathrm{A}}+\mathrm{c}^{6} \mathcal{O}^{6}+\ldots \mathrm{c}^{5} \mathcal{O}^{5}\right)_{k} . \tag{4}
\end{equation*}
$$

Here $k$ takes two values $k=(\Delta S=1)$ and $k=(\Delta S=0, \Delta I=1) ; c^{r}$ are the numerical coefficients, depending on the structure of weak and quark-gluon interactions; $\mathcal{O}^{r}$ are the local operators:
$\{\underline{27}\}: \quad \mathcal{O}_{\Delta s=1}^{27}=\bar{d} d \bar{d} s+\bar{s} s \bar{d} s+\bar{d} s \bar{d} d+\bar{d} s \bar{s} s-2(\bar{d} u \bar{u} s+\bar{d} s \bar{u} u+$ $+\bar{u} s \bar{d} u+\bar{u} u \bar{d} s)+h . c ., \quad ;$

$$
\begin{aligned}
& \Theta_{\Delta s=0,}^{27} \Delta_{I=1}= \frac{1}{2}(\bar{u} u \bar{u} u-\bar{d} d \bar{d} d-\bar{u} u \bar{s} s-\bar{s} s \bar{u} u+\bar{d} d \bar{s} s+\bar{s} s \bar{d} d)- \\
&-\bar{u} s \bar{s} u \\
&+\bar{d} s \bar{s} d+h . c .
\end{aligned}
$$

$\{8\}$

$$
\left[\begin{array}{l}
\mathcal{O}^{S} \\
\mathcal{O}^{A} \\
\mathcal{O}^{6} \\
\mathcal{O}^{5}
\end{array}\right]_{k}=\left[\begin{array}{cccc}
1 & 1 & 1 & 1 \\
-1 & 1 & -1 & 1 \\
1 & 0 & -1 & 0 \\
0 & 1 & 0 & -1
\end{array}\right]\left[\begin{array}{l}
\mathcal{O}\left(\Lambda_{k}, 1\right) \\
\mathcal{O}^{c}\left(\Lambda_{k}, 1\right) \\
\mathcal{O}\left(1, \Lambda_{k}\right) \\
\mathcal{O}^{c}\left(1, \Lambda_{k}\right)
\end{array}\right]
$$

where

$$
\begin{aligned}
& \bar{q}_{1} q_{2} \bar{q}_{3} q_{4}=: \bar{q}_{1 i} \gamma_{\mu} \gamma_{5} q_{2 i} \bar{q}_{3 j} \gamma^{\mu} q_{4 j}:, \quad \mathcal{O}(\mathrm{A}, \mathrm{~B})= \\
& =: \bar{q}_{i} \gamma_{\mu} \gamma_{5} A q_{i} \bar{q}_{j} \gamma^{\mu} B q_{j}: \quad \quad \mathcal{O}^{c}(\mathrm{~A}, \mathrm{~B})=: \bar{q}_{i} \gamma_{\mu} \gamma_{5} A q_{j} \bar{q}_{j} \gamma^{\mu} B q_{i}:,
\end{aligned}
$$

the summation is assumed over the colour indices $i$ and $; \Lambda_{k}=\lambda_{6}$ at $\mathrm{k}=(\Delta \mathrm{S}=1)$ and $\Lambda_{\mathrm{k}}=1 / 2 \lambda_{\mathrm{s}}$ at $\mathrm{k}=(\Delta \mathrm{S}=0, \Delta \mathrm{I}=1)$. The $\mathrm{SU}(3)$ properties of the operators are denoted in the braces. The typical values of the coefficients $c^{r}$ are given in the table. We should like to recall that without the penguin contributions $\mathrm{c} \delta_{s=1}=$ $=\mathrm{c}_{\Delta \mathrm{S}=\overline{\mathrm{F}}}^{\delta} 0$. Therefore, thanks to penguins each operator $\mathcal{O}_{\Delta \mathrm{S}=0, \Delta \mathrm{I}=1}$ in (4) acquires the $\operatorname{SU}(3)$ partner $\mathcal{O}_{\Delta \mathrm{s}=1}^{r}$ !

## Table

Numerical values of the coefficient functions $c^{r}$ a $\sin \theta_{\mathrm{C}}=0.23, \sin ^{2} \theta_{\mathrm{W}}=0.23, \alpha_{\mathrm{s}}\left(\mathrm{m}_{\mathrm{c}}\right) / a_{\mathrm{s}}\left(\mathrm{M}_{\mathrm{W}}\right)=2.45$, $a_{\mathrm{s}}\left(\mathrm{R}_{\mathrm{c}}^{-1}\right) / a_{\mathrm{s}}\left(\mathrm{m}_{\mathrm{c}}\right)=3.71^{19 \%}$.

| $\Delta \mathrm{S}$ | $\mathrm{c}^{27}$ | $\mathrm{c}^{\mathrm{S}}$ | $\mathrm{c}^{\mathrm{A}}$ | $\mathrm{c}^{6}$ | $\mathrm{c}^{5}$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| 1 | -0.014 | 0.0049 | 0.15 | 0.0020 | -0.012 |
| 0 | 0.029 | -0.027 | 0.46 | -0.029 | -0.081 |

In the valence quark approximation for the matrix elements $\left.<\pi \mathrm{B}^{\circ}\left|\mathcal{O}^{\mathrm{r}}\right| \mathrm{B}\right\rangle^{\mathrm{NF}}$ the following relations hold:

$$
\left\langle\pi \mathrm{B}^{\prime}\right| \mathcal{O}^{27 .}|\mathrm{B}\rangle^{N F}=\left\langle\pi \mathrm{B}^{\prime}\right| \mathcal{O}^{S}|\mathrm{~B}\rangle^{N F}=0, \text { and }\left\langle\pi \mathrm{B}^{\prime}\right| \mathcal{O}^{5}|\mathrm{~B}\rangle^{\mathrm{NF}}=-\left\langle\pi \mathrm{B}^{\prime}\right| \mathcal{O}^{6}|\mathrm{~B}\rangle^{\mathrm{NF}}
$$

owing to antisymmetry of the quark wave functions in baryons;
 rators, and consequently, $\mathcal{O}_{\Delta}^{A}=1$ does not contribute to the right-hand side of relation $(\overline{3})$.

Thus, we have shown that the sum rule (3) can be applied to the total effective hamiltonian (4) with

$$
\begin{equation*}
\frac{{ }^{c} \Delta S=0}{c_{\Delta S=1}}=\frac{\left(c^{6}-c^{5}\right) \Delta S=0}{\left(c^{6}-c^{5}\right) \Delta S=1} \tag{5}
\end{equation*}
$$

III. Finally, we consider the factorizing parts of the amplitudes

$$
\begin{aligned}
& A_{\pi}^{F}=-\frac{4}{3}\left(c^{6}+3 c^{5}\right) \Delta S=0 \frac{f_{\pi}}{m_{u}+m_{d}} \cdot \eta_{n},
\end{aligned}
$$

$$
\begin{align*}
& +\frac{4}{3}\left(\mathrm{c}^{6}+3 \mathrm{c}^{5}\right) \mathrm{Ds}=1^{\mathrm{f}_{\pi}} \mathrm{m}_{\mathrm{u}}+\mathrm{m}_{\mathrm{d}}\binom{\eta_{\Lambda}}{\eta_{\Xi}} . \tag{6}
\end{align*}
$$

Here, we choose the value $\eta_{\mathrm{n}}=\langle\mathrm{p}| \overline{\mathrm{u}} \mathrm{d}|\mathrm{n}\rangle \approx 0.5, \eta_{\Lambda}=\langle\mathrm{p}| \overline{\mathrm{u}} \mathrm{s}\left|\Lambda^{\circ}\right\rangle \approx 0.6$, $\eta_{\Xi}=\left\langle\Lambda^{\circ}\right| \mathrm{us} \mid \Xi^{-}>\approx 0.6$ (that is in agreement within the factor 2 with other estimates $/ 4,3 /$ ), and concentrate our attention on the factor $\mathrm{f}_{\pi} /\left(\mathrm{m}_{\mathrm{u}}+\mathrm{m}_{\mathrm{d}}\right)$. This factor appears in the calculation of the matrix element $\left\langle\pi^{-}\right| \overline{\mathrm{d}} \gamma_{5} \mathbf{u}|0\rangle$. using the free equations of motion $\left(i \gamma^{\mu} \partial_{\mu}-m_{q}\right) \mathbf{q}=0, \quad \mathbf{q}=\mathbf{u}, \mathrm{d}$ and the assumption that the form of these equations does not change in the presence of strong interactions ${ }^{\prime 4 /}$. There arises a question: "What meaning should be attributed to the masses $m_{q}$ ?"

If the quarks were really free, the use of current masses $\mathrm{m}_{\mathrm{q}}^{\circ} \sim 5 \mathrm{MeV}$ would be justified. The situation is different when the quarks are confined. In this case the role of $m_{q}$ is played by the effective mass $\mathrm{m}_{\mathrm{q}}^{*}$, which bears the information on the quark confinement ${ }^{111 /}$. The mass $\mathrm{m}_{\mathrm{q}}^{*}$ is not a universal characteristic of the quark $q$ and depends on the problem under consideration. At that $\mathrm{m}_{\mathrm{q}}^{*} \sim \mathrm{R}_{\mathrm{c}}^{-1}$, where $\mathrm{R}_{\mathrm{c}}$ is the radius of confinement, which is characteristic of this problem. Here are two examples of calculation of $\mathrm{m}_{\mathrm{q}}^{*}$ in the simplest version of the MIT bag with $\mathrm{m}_{\mathrm{q}}^{\circ}=0^{112 /}$

$$
\begin{aligned}
& \mathrm{m}_{\mathrm{q}}^{*}=-\frac{\mathrm{i}}{2} \partial^{\mu}\left\langle\pi^{-}\right| \mathrm{d} \gamma_{\mu} \gamma_{5} \mathrm{u}\left|0>/<\pi^{-}\right| \mathrm{d} \gamma_{5} \mathrm{u}|0\rangle=\frac{2 \omega}{3(\omega-1)} \cdot \mathrm{R}_{\pi}^{-1}, \\
& \left.\underset{\mathrm{q}}{\mathrm{~m}_{=}-\frac{\dot{1}}{2}} \dot{\partial}^{\mu}\langle\mathrm{p}| \overline{\mathrm{u}}^{\prime} \gamma_{\mu} \gamma_{5} \mathrm{~d}|\dot{\mathrm{n}}>/<\mathrm{p}| \overline{\mathrm{u}}_{\gamma_{5}} \mathrm{~d} \right\rvert\, \dot{\mathrm{n}}>=\frac{2 \omega^{2}}{4 \omega-3}-\mathrm{R}_{\mathrm{N}}^{-1},
\end{aligned}
$$

where $\omega=2.04$. : We note that in both the cases the coefficients at $R_{c}^{-1}$ do not differ strongly from unity. Hence, it follows that for the calculation of $A^{F}$, in (6) it is reasonable to choose $\mathrm{m}_{\mathrm{d}}^{*}=\mathrm{m}_{\mathrm{d}}^{*} \approx 200 \mathrm{MeV}$ that corresponds to $\mathrm{R}_{\mathrm{c}}=1 \mathrm{fm}$. In this case $f_{\pi} /\left(m_{u}+m_{d}\right)=1 / 2 f_{\pi} R_{c}=0.23$ and $A_{\pi}^{F}$ practically vanishes.

Now we can calculate the amplitude $A_{\pi}$ : Substituting the values of $\mathrm{c}^{\mathrm{r}}$ from the table into formulae (6), (5) and (3), we get

$$
\mathrm{A}_{\pi}=\mathrm{A}_{\pi}^{\mathrm{NF}}+\mathrm{A}_{\pi}^{\mathrm{F}} \approx \mathrm{~A}_{\pi}^{\mathrm{NF}} \approx 3.5
$$

The obtained $A_{\pi}$ is $1.5-2$ times as large as the average value of $A_{\pi}^{\text {exp }} / 88 /$, that is, in our opinion, due to the approximations $/ \cdot 4,9 /$ which have been adopted in the calculation of the coefficient functions $\mathrm{c}^{\mathrm{r}}$ of the effective hamiltonian $\mathcal{H}^{\mathrm{PV}}$. The coefficients $c \delta_{S=1}$ and $c \Delta S=1$, which are determined by the behaviour of the $Q C D$ running constant $a_{s}(\mu)$ at $\mu \leqslant m_{c}\left(m_{c}\right.$ is the mass of c -quark), are especially sensitive to such approximations. Thus, the amplitude $A_{\pi}$ may serve as a "touchstone" for the study of the quark-gluon interactions at large distances.

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## APPENDIX

Here we give the field-theoretical description of the amplitude $<{ }_{\pi} B^{\prime} \mid \mathcal{H}^{P} Y_{B}>$ (part A) and show that the ETC-part of this amplitude corresponds to the diagrams (a) and (b) of the figure with $k_{\pi} \rightarrow 0$ (part B).
A. We write down the effective hamiltonian $\mathcal{H}^{P V}$ in the form

$$
\mathcal{H}^{\mathrm{rm}}=\sqrt{2} \bar{G}_{\mathrm{M}, \mathrm{~N}} \mathrm{c}^{\mathrm{MN}} \mathcal{O}^{\mathrm{MN}},
$$

where $\mathcal{O}^{M N}=: \bar{q} M q \bar{q} N q:, M$ and $N$ are the matrices in the (spinor) $\otimes$ (flavour) $\otimes$ (colour) space, and consider the matrix elements $\left.\mathbb{Q}=\ll n^{\prime} \cdot\left|\mathcal{O}^{\mathrm{MN}}\right| \mathrm{B}\right\rangle$ : Using the reduction formula and PCAC, we get

$$
\begin{align*}
& \left.\mathbb{Q}=\frac{i\left(-k_{\pi}^{2}+m_{\pi}^{2}\right)}{f_{\pi} m_{\pi}^{2}} \int \mathrm{~d}^{4} x e^{i k^{x}}<B^{\prime} \right\rvert\, \dot{\partial}^{\mu} T\left(: \bar{q}(x) P_{\mu} q(x):, \otimes \mathcal{O}^{M N}(0)\right)- \\
& -\delta\left(x^{\circ}\right)\left[: \bar{q}(x) P_{0} q(x):, \mathcal{O}^{M N}(0)\right]|B\rangle, \tag{A1}
\end{align*}
$$

where $\mathrm{P}_{\mu}=y_{\mu} \gamma_{5} \frac{\lambda}{2}, \lambda$ is the matrix defining the pion isotopic properties.

Expand the T -product and commutator in (AI) according to the Wick theorem

$$
\begin{align*}
& \partial^{\mu_{\mathrm{T}}\left(: \overline{\mathrm{q}}(\mathrm{x}) \mathrm{P}_{\mu} \mathrm{q}(\mathrm{x}):, \mathcal{O}^{\mathrm{MN}}(0)\right)=\mathrm{T}_{9}(\mathrm{x})+\mathrm{T}_{6}(\mathrm{x})+\mathrm{T}_{6}^{\prime}(\mathrm{x})+\mathrm{T}_{3}(\mathrm{x}),}  \tag{A2}\\
& T_{9}(x)=1: \bar{q}(x) P q(x) \bar{q}(0) M q(0) \bar{q}(0) N q(0):,  \tag{a}\\
& \mathrm{T}_{6}^{\prime}(\mathrm{x})=:\left[\overline{\mathrm{q}}(0) M S^{\mathrm{c}}(-\mathrm{x}) \mathrm{Pq}(\mathrm{x})+\overline{\mathrm{q}}(\mathrm{x}) \mathrm{PS}^{\mathrm{c}}(\mathrm{x}) \mathrm{Mq}(0)\right] \bar{q}(0) \mathrm{Nq}(0):+\{\mathrm{M} \leftrightarrow N\},  \tag{b}\\
& \left.\mathrm{T}_{\mathrm{G}}^{\prime}(\mathrm{x})=-\delta^{4}(\mathrm{x}):\left[\overline{\mathrm{q}}(0) \mathrm{M} \gamma_{0} \mathrm{P}_{0} \mathrm{q}(\mathrm{x})+\overline{\mathrm{q}}(\mathrm{x}) \gamma_{0} \mathrm{P}_{0} \mathrm{Mq}(0)\right] \overline{\mathrm{q}}(0) \mathrm{Nq}(0):+\{\mathrm{M}\lrcorner \mathrm{N}\right\},  \tag{c}\\
& \left.\mathrm{T}_{3}(\mathrm{x})=\mathrm{J}^{\mu}\left[\mathrm{Sp}_{\mathrm{p}} \mathrm{~S}^{\mathrm{c}}(-\mathrm{x}) \mathrm{P}_{\mu} \mathrm{S}^{\mathrm{c}}(\mathrm{x}) \mathrm{M}\right): \overline{\mathrm{q}}(0) \mathrm{Nq}(0):-: \overline{\mathrm{q}}(0) \mathrm{MS}^{\mathrm{c}}(-\mathrm{x}) \mathrm{P}_{\mu} \mathrm{S}^{\mathrm{c}}(\mathrm{x}) \mathrm{Nq}(0): \mathrm{f}_{+} \mathrm{d}\right)
\end{align*}
$$

$+\left\{\mathrm{M}_{\mapsto} \mathrm{N}\right\}$;

$$
\begin{equation*}
\left[:-\bar{q}(x) P_{0} q(x):, \mathcal{O}^{M N}(0)\right]=C_{6}(x)+C_{3}(x) \tag{A3}
\end{equation*}
$$

$$
C_{6}(x)=-i:\left[\bar{q}(x) P_{0} S(x) \cdot M q(0)-q(0) M S(-x) P_{0} q(x)\right] \bar{q}(0) N q(0):+\{M \leftrightarrow N\} \text {. }(a)
$$

$$
\begin{equation*}
\mathrm{C}_{3}(\mathrm{x})=\left[\mathrm{Sp}_{\mathrm{S}}\left(\mathrm{~S}^{+}(\mathrm{x}) \mathrm{MS}^{-}(-\mathrm{x}) \mathrm{P}_{0}\right)-\mathrm{Sp}\left(\mathrm{~S}^{+}(-\mathrm{x}) \mathrm{P}_{0} \mathrm{~S}^{-}(\mathrm{x}) \mathrm{M}\right)\right]: \overline{\mathrm{q}}(0) \mathrm{Nq}(0):+ \tag{b}
\end{equation*}
$$

$$
+: \bar{q}(0)\left[M S^{+}(-x) P_{0} S^{-}(x) N-M S^{-}(-x) P_{0} S^{+}(x) N\right] q(0):+\{M \rightarrow N\}
$$

where the following notation is used: $P=y_{5}\left\{\mathrm{~m}_{\mathrm{q}}^{*}, \frac{\lambda}{2}\right\} ; \mathrm{S}^{\mathrm{c}}(\mathrm{x})=$ $=\mathrm{i}<0|\mathrm{~T}(\mathrm{q}(\mathrm{x}), \overline{\mathrm{q}}(0))| 0\rangle ; \mathrm{S}_{\beta a}^{+}(\mathrm{x})=\mathrm{i}<0 \mid \overline{\mathrm{q}}_{a}^{-}(0) \mathrm{q} \beta^{(\mathrm{x}) \mid 0>,} \quad \mathrm{S}_{a \beta}^{-}(\mathrm{x}) \mathrm{x}$. $=\mathrm{i}\langle 0| \mathrm{q}_{a}(\mathrm{x}) \overline{\mathrm{q}}_{\beta^{\prime}}(0)|0\rangle, \quad \mathrm{S}(\mathrm{x})=\mathrm{S}^{+}(\mathrm{x})+\mathrm{S}^{-1}(\mathrm{x})$.
The subscripts of the operators $T(x)$ and $C(x)$ denote their operator dimensions.

We introduce the matrices $Q$ and $R$ through the Fierz transformation

$$
M_{A B} \otimes N_{C D}=Q_{A D} \otimes \dot{R}_{C B}
$$

Then from (Al), (A2d), (A3b) and relations

$$
\langle 0| T\left(: \bar{q}(x) P_{\mu} q(x):,: \bar{q}(0) L q(0):\right)|0\rangle=\operatorname{Sp}\left(S^{c}(-x) P_{\mu} S^{c}(x) L\right),
$$

$$
\begin{gathered}
<0\left|\left[: \bar{q}(x) P_{0} q(x):,: \bar{q}(0) L q(0):\right]\right| 0>=S p\left(S^{+}(x) L S^{-}(-x) P_{0}\right)- \\
\quad-S p\left(S^{+}(-x) P_{0} S^{-}(x) L\right), \quad L=M, N, Q, R
\end{gathered}
$$

we find

$$
\begin{aligned}
& \frac{\mathrm{i}\left(-\mathrm{k}_{\pi}^{2}+\mathrm{m}_{\pi}^{2}\right)}{\mathrm{f}_{\pi} \mathrm{m}_{\pi}^{2}} \int \mathrm{~d}^{4} \mathrm{e}^{i \mathrm{k}_{\pi^{x}}}\left\langle\mathrm{~B}^{\prime}\right| \mathrm{T}_{3}(\mathrm{x})-\delta\left(\mathrm{x}^{\circ}\right) \mathrm{C}_{3}(\mathrm{x})|\mathrm{B}\rangle= \\
& =\langle\pi|: \overline{\mathrm{q}}(0) \mathrm{Mq}(0):|0\rangle ;\left\langle\mathrm{B}^{\prime}\right|: \overline{\mathrm{q}}(0) \mathrm{Nq}(0):|\mathrm{B}\rangle-\langle\pi|: \ddot{\mathrm{q}}(0) Q \mathrm{q}(0):|0\rangle\left\langle\mathrm{B}^{\circ}\right|: \overline{\mathrm{q}}(0) \mathrm{Rq}(0):|\mathrm{B}\rangle+
\end{aligned}
$$

$$
\begin{equation*}
+\{M \leftrightarrow N, Q \leftrightarrow R\} . \tag{A4}
\end{equation*}
$$

Noting now that from $\left.S(x)\right|_{x^{\circ}=0}=1 y^{\circ} \delta^{3}(x)$ it follows

$$
\begin{equation*}
\left.\int \mathrm{d}^{4} \mathrm{x} \mathrm{e}^{\mathrm{ik} k^{x}}<\mathrm{B}^{\prime}\left|\mathrm{T}_{6}^{\prime}(\mathrm{x})-\delta\left(\mathrm{x}^{\circ}\right) \mathrm{C}_{6}(\mathrm{x})\right| \mathrm{B}\right\rangle=0 \tag{A5}
\end{equation*}
$$

we get the final expression

$$
\begin{align*}
& \left.\mathbb{Q}=\frac{i\left(-k_{\pi}^{2}+m_{\pi}^{2}\right)}{f_{\pi} m_{\pi}^{2}} \int d^{4} e^{i k_{\pi} \mathbf{x}}<B^{\prime}\left|T_{9}(x)+T_{6}(x)\right| B\right\rangle+Q^{F},  \tag{A6}\\
& \text { ere the factorizing part of the amplitude } Q, Q^{F}
\end{align*}
$$

where the factorizing part of the amplitude $\mathbb{Q}, \mathbb{Q}^{\mathrm{F}}$ is defined by expression (A4).

The comparison of (A2a, b) and (A6) with the diagrams of the figure shows that the matrix element of the operator $T_{9}$ corresponds to the diagram (c), and the matrix element of ${ }^{9} \mathrm{~T}_{6}$ to the diagrams (a) and (b). As is seen from (A2a), the matrix element of the operator $T_{9}$ vanishes at $k_{\pi} \rightarrow 0$, and consequently, the diagrams (a) and (b) dominate in the nonfactorizing part of the amplitude $\mathbb{A}, \mathbb{Q}^{N F}$.
B. By definition $\mathbb{Q}^{\mathrm{ETC}}=\lim _{\operatorname{kim}_{\boldsymbol{m}} \mathbb{Q}} \mathbb{Q}$.

According to the canonical current algebra

$$
\begin{equation*}
\mathfrak{Q}^{\mathrm{ETC}}=-\frac{\mathrm{i}\left(-\mathrm{k}_{\pi}^{2}+\mathrm{m}_{\pi}^{2}\right)}{\mathrm{f}_{\pi} \mathrm{m} \frac{2}{2}} \cdot \int \mathrm{~d}^{4} \mathrm{xe}^{\mathrm{ik} \mathrm{k}^{\mathrm{x}}} \delta\left(\mathrm{x}^{\mathrm{D}}\right)<\mathrm{B}^{\prime}\left|\mathrm{C}_{6}(\mathrm{x})\right| \mathrm{B}>\left.\right|_{\mathrm{k}_{\pi} \rightarrow 0} \tag{A7}
\end{equation*}
$$

It should be mentioned now that as $k_{\pi} \rightarrow 0$
$\int d^{4} x e^{i k^{x}} \pi^{x}<B^{\prime}\left|T_{6}(x)+T_{6}^{\prime}(x)\right| B>\rightarrow 0$.
Hence and from relations (A7) and (A5), we get immediately $Q^{\text {ETC }}=\frac{i\left(-k_{\pi}^{2}+\mathrm{m}_{\pi}^{2}\right)}{\mathrm{f}_{\pi} \mathrm{m}_{\pi}^{2}}: \int \mathrm{d}^{4} \mathrm{x} \mathrm{e}^{\mathrm{i} k_{\pi^{\mathrm{x}}}}<\mathrm{B}^{\prime}\left|\mathrm{T}_{6}(\mathrm{x})\right| \mathrm{B}>\left.\right|_{\mathrm{k}_{\pi} \rightarrow 0}$,
i.e., $\mathbb{Q}^{\mathrm{ETC}}$ corresponds to the diagrams (a) and (b) with $\mathrm{k}_{\pi} \overrightarrow{\mathrm{F}}_{\mathrm{N}} 0$,
and since the diagram (b) in this limit valishes, $\mathbb{Q}^{\mathrm{ETC}}=\mathbb{Q}_{k_{\pi} \rightarrow 0}$

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Дубовик В.М., Зенкин С.В.
Новый взгляд на несохранение четности в $\pi$ NN вершине
Рассмотрена нарушающая четность амплитуда $A_{\pi}=A\left(n \rightarrow \pi^{-} p\right)$. B рамках теоретико-полевого подхода показано, что каноническая ETC-часть $\mathrm{A}_{\pi}$ соответствует нефакторизационным (NF) диаграммам. $A_{T}^{N F}$ может быть выиислена для полного эффективного гамильтониана теории $\operatorname{SU}(2)_{L} \otimes \mathrm{U}(1)$ \& $\operatorname{SU}(3)$ с с помощью SU(3) правила сумм и оказывается очень чувствительной к поведени бегущей константы QCD $\alpha_{s}(\mu)$ при $\mu \leq \mathrm{m}_{\mathrm{c}} / \mathrm{m}_{\mathrm{c}}$ - масса с-кварка/. Приведены аргументы, согласно которым вклад факторизационных диаграмм в $A_{\pi}$ пренебрежимо мал.

Работа выполнена в Лаборатории теоретической физики оияи,

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Ansight into the Parity Violation at $\pi$ NN Vertex
$\mathrm{A}_{\pi}=\mathrm{A}\left(\mathrm{n} \rightarrow \pi^{-} \mathrm{p}\right) \quad$ parity-violating amplitude is considered. Within the ield-theoretical approach it is shown that canonical ETC-part of $A$ corresponds to nonfactorizing (NF) diagrams. ANF may be calculated for the total effective Hamiltonian in $\operatorname{SU}(2) \oplus(1) \otimes \operatorname{SU}(3)$, $\oplus$, $\operatorname{SU}(3)$ sum rule and is very sensitive to the behaviour of running OCD stant $\cdot_{a_{s}}(\mu)$ at $u \leq m_{c}$ ( $m_{c}$ is mass of $c$-quark). it is argued that in con ribution of factorizing diagrams into $A_{n}$ is negligible.

The investigation has been performed at the Laboratory of Theoretical Physics, JINR


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