$89-795$


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E14-89-795
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NEUTRON DIFFRACTION STUDY
OF THE MODULATED STRUCTURE OF $\mathrm{Bi}_{2}(\mathrm{Sr}, \mathrm{Ca})_{3} \mathrm{Cu}_{2} \mathrm{O}_{8+\gamma}$

Submitted to "Physica C"

Introduction
A simplified structural model of the high-temperature superconductor $\mathrm{Bi}_{2}(\mathrm{Sr}, \mathrm{Ca})_{3} \mathrm{Cu}_{2} \mathrm{O}_{\mathrm{B}}$ is of a high tetragonal symmetry $\mathrm{F} 4 / \mathrm{mmm}(a=5.4$ A, $c=30.7$ A). It is built of two alternating blocks, the oxygen - deficient perovskite (P) block and the triple-layer rock-salt block (RS) (See Fig.1). In the centre of the $P$ block there are two conducting $\mathrm{CuO}_{2}$ planes which sandwich the $C a$ layer. Because of the mentioned oxygen deficiency, calcium is eight-fold (cube) coordinated instead of the common dodecahedral coordination of large cations in perovskites. The coordination of cooper is square-pyramidal in which, however, the apical oxygen is largely displaced leaving copper effectively in the square-planar bonding. The Sr sites are located at the boundary of both blocks and their surroundings is the mixture of the dodecahedral and octahedral coordinations. It involves nine close oxygen atoms.

The Bi cations are in the centre of the rock-salt block and their coordination shown in Fig. 1 is octahedral. Such arrangement would be; however, unstable since it brings four oxygen neighbours within the Bi layer to a distance $a / 2=2.7$ A which is out of the region of possible $\mathrm{Bi}^{3+}-0$ bonds $(2.0-2.5$ A). In fact, the Bi coordination is largely distorted. That is the main reason for a decrease of the $\mathrm{Bi}_{2}(\mathrm{Sr}, \mathrm{Ca})_{3} \mathrm{Cu}_{2} \mathrm{O}_{\mathrm{B}}$ symmetry and appearance of a superstructure with period of approximately $5 a$.

As it is known from the early work of Subramanian et al.[1] and following single-crystal studies the fundamental structure can be described within the orthorhombic symmetry Amaa. There is much less confidence about the nature of the superstructure. The most complete information about the real arrangement of

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Fig. 1 - Scheme of the $\mathrm{Bi}_{z} \mathrm{Sr}_{z}$ Ca $\mathrm{Cu}_{z} \mathrm{O}_{\mathrm{a}}$ structure.
( P - the perovskite block, RS- the rock-salt block).
atoms comes of gao et al.[2] who analyzed own single-crystal $x$-ray data using the approach of incommensurate modulation of the displacive type. They determined the modulation of $\mathrm{Bi}, \mathrm{Sr}$ and $C u$ cations and average positions of other atoms. observed modulation displays components mainly in the $a, c$ plane and amplitudes are as large as $0.5 \AA$. Independently on their work we have undertaken a single-crystal neutron diffraction study and solved the problem of the superstructure using a different procedure. Here we present our results.

## Instrumentation and samples

Diffraction measurements were performed by the time-of-flight method on the neutron diffractometer $\mathrm{DN}-2$ which is equipped with
the linear position-sensitive detector. The diffractometer is placed at the mirror-guide tube of the pulsed reactor IBR-2 at the Joint Institute of Nuclear Research in Dubna. The great advantage of the apparatus is the scanning of the whole angular sector ( $\sim 10^{\circ}$ ) of the reciprocal plane at once and the nigh counting rate which is necessary for the investigation of extremely small crystals.

The integrated intensity of the Bragg reflection (intensity of a Lave spot) is given [3] by

$$
I_{o b s}=-\frac{F_{h k l}^{2} \lambda^{4}}{\sin ^{2} \vartheta} N(\lambda)
$$

where $N(\lambda)$ is the spectrum of the white neutron beam inciding the sample. With the use of the mirror guide the spectrum has a cut- off at $\lambda \sim 1 \AA$, maximum at $\lambda \sim 2 \AA$ and falls down in the long-wavelength side approximately as $\lambda^{-4}$. From that it follows that the experimental sensitivity to the structure factor $F_{h k l}^{2}$ is nearly uniform in the region $\lambda>2 \AA$ (practical limit is $8 \AA$ ), but it decreases quickly in the short-wavelength side. With the detector in positions $28=20^{\circ}-120^{\circ}$ the range $\lambda=2-8$ A corresponds (Bragg law $\lambda=2 d . \sin$ ) to the interplanar spacing $d=1.1-25 \AA$ which was the actual extent of our investigation.

Samples $\mathrm{Bi}_{2}(\mathrm{Sr}, \mathrm{Ca})_{3} \mathrm{Cu}_{2} \mathrm{O}_{8}$ used in our study were grown by a pseudo-flux method from melts with excess of copper [4]. The samples were of the plate or wedge shape with maximum face $\mathbf{2 \times 2}$ $\mathrm{mm}^{2}$ and width up to 0.8 mm . Some samples displayed facets apparently at right angles, giving the impression of a single crystal. However, the neutron diffraction has shown that each specimen contained several single-crystal blocks, sometimes slightly misoriented, sometimes disposed nearly perpendicularly. comparison with diffraction on very thin mica-like platelet revealed that even in bulk samples the width of blocks (the dimension along the c-axis) was microscopic.

In all investigated blocks the $\mathrm{Bi}_{2}(\mathrm{Sr}, \mathrm{Ca})_{3} \mathrm{Cu}_{2} \mathrm{O}_{\mathrm{B}}$ phase ( $\mathrm{C}=30.7$ A) was found to be interleaved with layers of the $\mathrm{Bi}_{2}(\mathrm{Sr}, \mathrm{Ca}) \mathrm{CuO}_{6}$ phase ( $\mathrm{c}=24.3$ A) the amount of which was estimated on the basis of diffracted intensity to $5 \%$. On the other hand, no signs of the $\mathrm{Bi}_{2}(\mathrm{Sr}, \mathrm{Ca})_{4} \mathrm{Cu}_{3} \mathrm{O}_{10}$ phase ( $\mathrm{c}-37 \mathrm{~A}$ ) were detected in our samples.

Extensive diffraction study was performed on a specimen which contained only two relatively large single-crystal blocks, quite misoriented. Investigation on one chosen block included measurements of four reciprocal planes hko, hol, okl, hhl and number of individual reflections associated mostly with the superstructure. Each measurement, which generally comprised detection of one or few reflections (sometimes with their higher orders), took 3 hours. Because of this long exposure the study was confined to one octant only and the $\pm \mathrm{h}, \pm \mathrm{k}, \pm \ell$ symmetry was checked on selected reflections.

Measurements by the time-of-flight method are generally strongly influenced by the secondary extinction because of long wavelengths used. To investigate its role, strong reflections were measured at different azimuthal angles, varying thus the mean diffraction path $\bar{T}$. Such experiments with the strongest reflection 220 allowed us to estimate the width of the investigated block from dimensions of its face (the $a, b$ plane) seen on the surface of the sample. The size of the block was established as $1.5 \times 1.0 \times 0.03 \mathrm{~mm}^{3}$. Thanks to the very small width, nearly all strong and medium reflections could be measured practically extinction free. Few exceptions were corrected (max. to 20\%) using the factor

$$
y=\left(1+k \underset{\sin 2 \theta}{-\frac{F_{k}^{2}}{} \lambda^{3}} \bar{T}\right)^{-1 / z}
$$

Results
Neutron diffraction experiments showed the same diffraction picture as the previous X-ray study of Gao et al. [2] -
fundamental reflections characteristic for the Amaa space group (observed lattice parameters $a=5.397(1), b=5.401$ (1), $c=30.716$ (3) A) and satellites of the first and second order in position given by the modulation vector $2^{n}[\tau, 0,1]$ with the observed value $\tau=0.213(3)$ (modulation period 4.69(7)a). In the investigated part of the reciprocal space the observable intensities were detected for nearly all fundamental reflections allowed by the Amaa symmetry and for about a half of satellites of the first order. Satellites of the second order were observed only in few cases.

Most data concerning the superstructure were obtained from the hol plane. There were several strong satellites $\tau 0 \ell$ which indicated large modulation of atomic layers along the c-axis. Remarkably strong were the satellites $2+\tau \quad 0 \quad l$ (the satellite reflection 2.2101 was very strong even among the fundamental reflections and reached $1 / 6$ intensity of the strongest reflection 220 ). Relatively strong were also some second-order satellites $4+2 \tau 0 \ell$ (especially 4.4200 ). on the other hand, satellites $2-0 \ell$ were weak. such observation indicated that some atoms in the $\mathrm{Bi}_{2}(\mathrm{Sr}, \mathrm{Ca})_{3} \mathrm{Cu}_{2} \mathrm{O}_{8}$ structure were arranged along the a-axis with spacing rather $a / 2.21-2.44 \mathrm{~A}$ than with $a / 2=2.7 \AA$ inherent in the true Amaa symmetry. We infered immediately that such property is associated probably wíth oxygen in the Bi layer and that the misfit is compensated by insertion of extra oxygen after each modulation period.

Search for the satellites was accomplished in the hko and ok $\ell$ planes. In the former plane and close to it we observed satellites $2+\pi \neq(2.2110,2.2121,2.2112,2.2132)$. All satellites of other types (i.e. $1^{\ddagger} \tau k 0,2-\tau k 0,3^{+} \tau k 0$ ) were unobservable. In the vicinity of the $0 k i$ plane we investigated satellites $\tau 1 \ell, \tau 2 \ell$ and $\tau 3 \ell$. As observable were found only some satellites $\tau 2 \ell$. Among them the weak satellite 0.2121 (disposed in the reciprocal space near the 010 line) evidenced
some b-axis modulation of the structure. Other $\tau 2 \ell$ satellites with larger $\ell$ index were associated rather with the c-axis modulation.

In total, we obtained for the structure refinement data on 114 fundamental reflections (including 14 unobservable), 72 satellites of the first order (28 unobservable) and 10 satellites of the second order (4 unobservable). The unobservable satellites included were those which carried a substantial information about the structure or were measured within a very small absolute uncertainty (concretely those with very large d-spacing). The gross of observable intensities displayed•st’atisťical uncertainty $10-20 \%$.
our structural model involved sinusoídial waving of atomic planes and a redistribution of atoms within the planes due to the insertion of extra oxygen into the Bi layer, both periodic along the a-axis. Longitudinal displacements associated with the redistribution were expressed by two harmonics except for oxygens in the Bi layer which were spaced out nearly equidistantly (including, of course, the extra oxygen). First refinements were carried out in the approximation of a supercell $5 \mathrm{a} \times \mathrm{b} \times \mathrm{c}$ (i.e. treating $\tau$ as equal to 0.2 ) within the space groups Pnnn and Pmnn. Both variants (See Fig. 2 a and b) yielded a satisfactory fit of the fundamental and satellite (properly speaking - superstructure) reflections and confirmed the expected excess of oxygen in the Bi layer. We note that the configuration of the Bio layer in the Pnnn model is the same as found recently in the $\mathrm{Bi}_{2} \mathrm{Sr}_{3} \mathrm{Fe}_{2} \mathrm{O}_{\mathrm{D}}, \gamma$ of the B 222 symmetry [5].

Final refinement was performed within a more realistic model shown in Fig. 2c. It corresponds to a supercell 19a $x \quad b \quad c$ possesses the pnaa symmetry and unites to some extent configurations in the previous Pnnn and Pmnn models. The pnaa model accounts for a modulation with the period 19a/4 (=4.75a) which agrees well with existing observations on
a)
Marys
Mrruns
$y^{C}$


##  <br>  <br> 

Fig. 2 - Bonding in the Bio plane in tentative models pmnn (a) and Pmnn (b) of the $5 a \times b \times c$ superstructure and the conclusive model pnaa of the $19 \mathrm{a} \times \mathrm{b} \times \mathrm{c}$ superstructure (c) (Bi cations shown by full dots: arrows mark the modulation periods, i.e. the places of the inserted oxygen.)
Two exceptional cases of the $B i(j)$ and $S r(j)$ coordination for $j=3$ (d) and 8 (f). (Labelling as in Figs. 2 c and 3a; expected shifts marked.)
$\mathrm{Bi}_{2}(\mathrm{Sr}, \mathrm{Ca})_{3} \mathrm{Cu}_{2} \mathrm{O}_{\mathrm{B}}$. (The most precise determination of the modulation period $[2,6]$ report a value $4.76(1) a$.$) The refined$ structural parameters are given in Tab.I and characteristic features of the superstructure are illustrated in Figs.2c-f,3 and 4. Some $x$ and $y$ coordinates in Tab.I were fixed on special values corresponding to the higher Amaa symmetry since our data were insensitive to small deviations from them (possible range $\pm 0.01$ ). For some atoms the modulation parameters $a_{1}, a_{2}$ were smaller than 0.01 and could not be determined with certainty for the same reason.

Finally, we should note that reflections $00 t$ appeared to be ~ 40\% enhanced with respect to other reflections. The excess of

| Atam | Mumber of positions |  |  | Present results |  |  |  | $\mathrm{B}_{\text {iso }}\left(\mathrm{A}^{2}\right)$ | Moculation amplitudes ${ }^{\text {a }}$ ( |  | ${ }_{\text {tudes }}{ }^{\text {d }}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ca,Sİ $\mathrm{j}=1,19)$ | $4 \times 19$ | 0 | . 5 | . 5 | 0 | . 5 | . 5 | 2.3(9) | - | - | -.0004(8) | . 0068 (22) | . 72 (9) $\mathrm{Ca}+$ |
| $\mathrm{Cu}(\mathrm{j}=1,19)$ | $8 \times 19$ | 0 | . 0002 | . 4467 | $\sim 0$ | -. 007 (3) | . 4474 (2) | $2.1(6)$ | - | - | -0093(4) | . 0062 (126) |  |
| $\mathbf{S r}(\mathrm{j}=1,19)$ | 8x19 | 0 | . 5037 | . 3909 | $\sim$ | . 494 (2) | . 3916 (4) | -0.1(6) | . 047 (4) | -.017(4) | -.00716) | . 0084 (10) | . 93 (3) |
| Bi (jew, 19) | $8 \times 19$ | 0 | . 0215 | . 3022 | - 0 | . 023 (3) | . $3018(2)$ | 2.0 | .070(4) | .058(5) | -.0078(6) | - | $\stackrel{1}{1}$ |
| O2 ( $\mathrm{j}=1,19)$ | $8 \times 19$ | . 25 | . 25 | . 445 | ~ 25 | -. 25 | .4488(4) | 0.9(3) | - | - | -.0086(3) | .0079(4) | 1 |
| $02(\mathrm{j}=1,19)$ | $8 \times 19$ | . 25 | . 75 | . 452 | ~. 25 | ~. 75 | . 4886 (4) | 0.9 | - | - | -.0086 | . 0079 | 1 |
| $03(\mathrm{j}=1,19)$ | $8 \times 19$ | 0 | -. 03 | . 372 | $\sim 0$ | -.033(3) | . 3668 (3) | 3.9(8) | . 098 (5) | . 051 (8) | -.0061(8) | . | 1 |
| $04(\mathrm{j}=1,21)$ | $8 \times 21$ | 0 | . 40 | . 303 | - | $\left..392(5)^{9}\right)$ | . 3097 (7) | 3.4 (11) | - | - | . 0008 (1) | ) 0015 (6) | 1 |

[^1]

Fig. 3 - (a) Bonding in the Sro plane in the Pnaa model(Sr cations shown by full dots) and (b) the $\mathrm{Sr}-\mathrm{O4}-\mathrm{Bi}-\mathrm{O} 3-\mathrm{Sr}$ links along the b-axis
intensity was related to tiny blocks (some of them evidenced by the diffraction) which were attached to the main block but were misoriented in the $\mathrm{a}, \mathrm{b}$ plane.

## Discussion

Our diffraction experiments have shown that the $\mathrm{Bi}_{2}(\mathrm{Sr}, \mathrm{Ca}), \mathrm{Cu}_{2} \mathrm{O}_{8}$ superconductor, grown by the single-crystal technology, formed lamellar structures consisting, of a stacking of microscopically thin blocks misoriented in the basal plane. The $\mathrm{Bi}_{\mathrm{z}}(\mathrm{Sr}, \mathrm{Ca})_{3} \mathrm{Cu}_{\mathrm{z}} \mathrm{O}_{\mathrm{g}}$ blocks were partially interleaved with layers of the related compound $\mathrm{Bi}_{2}(\mathrm{Sr}, \mathrm{Ca})_{2} \mathrm{CuO}_{6}$. Exceptionally, thicker blocks of several tens of microns were encountered making the single-crystal study possible. Despite of the pseudocubic metrics of the orthorhombic atomic structure all observed blocks were untwinned.

The essential feature of the modulated structure in $\mathrm{Bi}_{2}(\mathrm{Sr}, \mathrm{Ca})_{3} \mathrm{Cu}_{2} \mathrm{O}_{\mathrm{o}}, \gamma$ is the insertion of extra oxygen into the Bio


Fig. 4 - waving of atomic planes along the a-axis and the
longitudinal displacements observed.
(Cations shown by dots and circles, oxygen atoms by the dashed lines. Note the periodic expansions and contractions of the bismuth bilayers and their
opposite phases for $z=0.25$ and $z=0.75$. The arrows mark the location of additional oxygen.)
layers and associated displacive modulation of all layers with the period 4.75a. This gives rise to a superstructure of the 19a x b x c type and maximum symmetry pnaa. Structural refinement performed with the use of harmonic analysis resulted in a overall fit of observed and calculated intensities given by the R-factor of $13.2 \%$. Trial refinements going beyond the simplest harmonic analysis indicated, however, that the R -factor could be improved significantly still within the Pnaa space group.

Comparing the refined parameters given in Tab.I with results of previous diffraction studies we find that the cell parameters are smaller than in other single-crystal investigations and are close to the lower limit of values reported for powder samples. This may be a sign of the saturated oxygen content. The average atomic positions are in overall agreement with Ref[2]. A difference occurs for the Sr site which is slightly shifted along the b-axis, increasing thus the bond length to its 03 neighbour to $0.05 \AA$, as if our cation was larger. Similar shift, caused perhaps by the $\mathrm{Sr}^{2+}-\mathrm{Cu}^{2+}$ repulsion, is observed for the Cu site. The Cu cation thus occurs slightly off the centre of its square oxygen coordination. In contrary to previous data the average $z$-coordinates of the $O 1$ and 02 sites are found equal (their modulation is also the same within the e.s.d's). Largely different $z$-values in Ref [2] and in the powder neutron diffraction work [7] are likely a consequence of omission of the 01, 02 modulation. Extent and the course of the $a$ and $c$-axis modulation (See Fig.4) is similar to results on the related compound $\mathrm{Bi}_{2} \mathrm{Sr}_{3} \mathrm{Fe}_{2} \mathrm{O}_{9+\gamma}$ which exhibits a superstructure of the $5 \mathrm{a} \times \mathrm{b} \times \mathrm{c}$ type [5]. Separation of the Bio planes in the bilayer is quite large even in the narrowed place of the inserted oxygen. No additional atoms were detected between them. Total lack of oxygen in the ca layer was confirmed, as well.

Calculated interatomic distances are summarized in Tab.II. In spite of limitations associated with the harmonic approximation the coordination of cations is highly uniform. All bismuth cations display three nearly perpendicular bonds of 2.0 - 2.2 A length, two of them towards the 04 oxygens in the Bio plane, third to the 03 oxygen in the Sro plane. Other oxygen neighbours are displaced to $3 \AA$ or more. (Somewhat less advantageous configuration was obtained for Bi(8). Fig. 2 f shows a shift which would establish a better bonding.) Interconnection of bonds in the Bio plane forms the $B i_{n} O_{n+1}$ chains ( $n=9$ and

Tab.II Calculated metal-oxygen bonds and close oxygen-oxygenapproaches (<2.7 \&) in $\mathrm{Bi}_{2}(\mathrm{Sr}, \mathrm{Ca})_{3} \mathrm{Cu}_{2} \mathrm{O}_{\mathrm{B}, 21}$

| $\begin{gathered} \text { atoms } \\ (j=1,19) \end{gathered}$ | number <br> of bonds | range of distances | mean distance |
| :---: | :---: | :---: | :---: |
| $\mathrm{Bi}(\mathrm{j})-03$ | , 1 | 1.97-2.07 | 2.02 |
| $\mathrm{Bi}(\mathrm{j})=04^{\mathrm{ab}}$, | , 1 | 2.12-2.41 | 2.22 |
| $\mathrm{Bi}(\mathrm{j})-04^{\text {b }}$ | 1 | 2.06-2.19 | 2.12 |
| total Bi-O | 3 |  | 2.12 |
| Sr(j) - 01 | 2 | 2.50-2.71 | 2.58 |
| Sr(j) - $02{ }_{\text {e }}$, | , 2 | 2.53-2.74 | 2.63 |
| $\mathbf{S r}(\mathrm{j})-03^{\text {c }}$, | , 3 | 2.45-2.81 | 2.64 |
| $\operatorname{Sr}(\mathrm{j})-03^{\text {d }}$, | , | $2.66-2.70$ | 2.68 |
| Sr(j) - O4 ${ }^{\text {c }}$, | , | 2.52-2.80 | 2.65 |
| Sr(j) - O4 ${ }^{\text {c }}$, | 1-2 | 2.54-2.77 | 2.63 |
| total $\mathrm{Sr}-\mathrm{O}_{\text {d, }}$, | 8 |  | 2.62 |
| total $\mathrm{Sr}-\mathrm{O}^{\text {a }}$ | 6-7 |  | 2.62 |
| Ca(j) - 03 | 4 | 2.40-2.54 | 2.47 |
| $\mathrm{Ca}(\mathrm{j})$ - 02 | 4 | 2.41-2.55 | 2.48 |
| total ca-o | 8 |  | 2.48 |
| Cu(j) - 01 | 2 | 1.93-1.94 |  |
| Cu(j) - 02 | 2 | 1.88 |  |
| total $\mathrm{Cu}-\mathrm{O}$ | 4 |  | 1.91 |
| ( $\mathrm{Cu}(\mathrm{j})-03$ | 1 | 2.38-2.58) |  |
| O4 (3) - 04 (4) ${ }^{\text {a }}$ |  | 2.50 (< 04 (3) | - $\mathrm{Bi}(3)-04(4)=72^{\circ}$ ) |
| O4(4)-04(5) |  | 2.60 (< 04 (4) | $-\mathrm{Bi}(4)-\mathrm{O4}(5)=74^{\circ}$ ) |
| 04(14)-04(15) |  | 2.45 (< 04 (1 | $)-\mathrm{Bi}(3)-04(15)=71^{\circ}$ ) |

a) bonds directed approximately along the a-axis
b) bonds along the b-axis
c) data for atoms out of the region of the inserted 04 oxygen, i.e. except $j=3,4,12$ and 13
d) data for $j=3,4,12$ and 13
e) short $0-0$ distances and small $0-B i-0$ angles are likely artifacts of the sinusoidal approximation of the $z$-axis modulation (See text and Fig.2d)
10) along the a-axis (See Fig. 2c). The excess of oxygen and the configuration of bonds reminds the situation in $\mathrm{Bi}_{\mathbf{2}} \mathrm{Sr}_{\mathbf{3}} \mathrm{Fe}_{\mathbf{2}} \mathrm{O}_{\mathrm{o}+\boldsymbol{r}}$ [5]. In contrary to it we have found no indications for further segmentation of the $\mathrm{Bi}_{n} \mathrm{O}_{n+1}$ chains or for the formation of $\mathrm{Bi}_{2} \mathrm{O}_{2}$ dimers as described in Ref [8].

Strontium cations are bonded to eight oxygen atoms in maximum since one of four 03 neighbours in the Sro plane occurs always in a non-bonding distance larger than 2.9 A . The net of the sr-o bonds shown in Fig.3a displays the $\mathrm{Sr}_{\mathrm{n}} \mathrm{O}_{\mathrm{n}}$ chains ( $\mathrm{n}=9$ and 10) along the a-axis which are terminated in the vicinity of the inserted oxygen in the Bi layer. There is a link of the $\mathrm{Sr}_{\mathrm{n}} \mathrm{O}_{\mathrm{n}}$ and $B i_{n} O_{n+1}$ chains along the b-axis as shown in Fig. 3b. The mean sr-o bonding length amounts to 2.62 A and slightly exceeds the sum of ionic radii. This suggests that the decreased scattering length, observed in the Sr site, is rather due to a partial occupation (93\%) than by some calcium substitution. The most likely location of $S r$ vacancies are the unfavorably coordinated sites which terminate the $\mathrm{Sr}_{\mathrm{n}} \mathrm{O}_{\mathrm{n}}$ chains and are labelled 3, 4, 12 and 13 in Fig.3a. These sites (expected occupation -1/2) form zigzag chains along the b-direction. We note also that oxygen 03 (apical in the $\mathrm{CuO}_{5}$ pyramid) makes a closest approach to copper just at the mentioned sites. In principle the real location of vacancies could be revealed by diffraction. Our data appeared, however, quite insensitive.

Second alkali-ion site located between the $\mathrm{CuO}_{z}$ planes, is coordinated via $2.48 \AA$ bonds to eight oxygens in corners of an elongated cube. According to the observed scattering length, the site is occupied by $72 \% \mathrm{Ca}$ and $28 \% \mathrm{Sr}$. Total composition is thus given by the formulae $\mathrm{Bi}_{\mathrm{z}} \mathrm{Sr}_{\mathrm{z} .14} \mathrm{Ca}_{\mathrm{o} .72} \mathrm{Cu}_{\mathrm{z}} \mathrm{O}_{\mathrm{B} .21}$. This corresponds to the formal copper valence of 2.35 .

Calculated oxygen-oxygen distances involve a couple of approaches of $2.5 \AA$ only (occurring e.g. in the $\mathrm{Bi}(3)$ coordination shown in Fig.2d). These very short distances are artifacts of the harmonic analysis which is not able to describe discrete features of the modulation in places of the inserted oxygen. Trial refinements performed with the more symmetrical models within the $5 \mathrm{a} \times \mathrm{b} \times \mathrm{c}$ approximation did show that atoms 04, instead of lack of any c-axis modulation in Fig.4, in fact
follow to some extent the waving of the Bi layer, except for the inserted oxygens (e.g. O4(4)) which are shifted to a position intermediate between the 04 and 03 levels. The shift of $O 4(4)$ is accompanied with solitary shifts of $03(3)$ and $03(4)$ as marked in Fig.2d. In this way the oxygen-oxygen distance increases to -2.7 $\AA$ and the $0-B i-0$ angle becomes closer to $90^{\circ}$.

Besides the modulation given by the harmonical amplitudes $a_{1}, a_{2}$ and $c_{1}$, the structure involves other considerable displacements. They manifest themselves in the anisotropy of the temperature factor. Concretely, large displacements along the c-axis were evidenced for sites $04, \mathrm{Ol}+\mathrm{O} 2, \mathrm{Sr}, \mathrm{Ca}$ and Cu . (They were characterized in Tab. I within a split-atom model by the amplitude $\Delta c$.) On the other hand, the 03 site exhibited somewhat larger displacements in the basal plane. We concluded that the main contribution to the splitting amplitude $\Delta c$ comes from random displacements arising due to the dissimilar size of atoms in the mixed ( $\mathrm{Ca}, \mathrm{Sr}$ ) site and due to vacancies present in the Sr site. Other possibilities like the modulation with period 9.5 a (inherent in the pnaa model), the second and higher order harmonical c-axis modulation or a corrugation of atomic planes due to some cooperative ordering may apply only to some of the mentioned sites or can contribute in a limited extent.

Concluding remarks
The complexity of the $\mathrm{Bi}_{2}(\mathrm{Sr}, \mathrm{Ca})_{3} \mathrm{Cu}_{2} \mathrm{O}_{\mathrm{s}+\gamma}$ structure originates from the pecularities of the $\mathrm{Bi}^{3+}$ bonding. It is known that this cation has a lone pair which leads generally to a distorted coordination. Namely, in the direction of the lone pair the oxygen atoms are largely displaced whereas opposite to it short bonds occur. Such coordination cannot be realized within a simple tetragonal model. It is achieved by two mechanisms - by the ordering of long (non-bonding) and short (bonding) Bi-O distances along the b-axis and by formation of the $B i_{n} O_{n, 1}$
chains along the a-axis through the inserted oxygen. The former mechanism results in an orthorhombic distortion of the Amaa symmetry. The later one is responsible for waving of atomic layers along the a-axis and for considerable longitudinal modulation within some layers. Transversal modulation along the b-axis is certain only for oxygen in the Bio layer. In spite of the non-integer period of the modulations there are strong indications that the superstructure is commensurate with a cell 19 times enlarged in the a-direction. This supercell comprises four modulation periods of 4.75a. A direct proof of the commensurability would be e.g. an observation of a modulation with double period 9.5 a which might manifest itself by very weak superstructure reflections.

The $\mathrm{Bi}_{2}(\mathrm{Sr}, \mathrm{Ca})_{3} \mathrm{Cu}_{2} \mathrm{O}_{\mathrm{i}}+\gamma$ structure involves one rather theoretical aspect. The $\mathrm{Bi}_{2} \mathrm{O}_{2}$ bilayers are in the Pnaa symmetry formally polar. Realization of a polarized state would be e.g. possible if the cation vacancies present in the Sr layer were distributed in an ordered way over the sites suggested in the present study.

## Acknowledgement

The authors thank to Drs. S.Durčok and M.Nevł̌iva for the preparation of the single crystals.

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Бескровншй A.H. и AP.
E14-89-795
Нейтронографическое исследование модулироаянной
структури Bi $_{2}\left(\mathrm{Sr}, \mathrm{Ca}^{2}\right)_{3} \mathrm{Cu}_{2} \mathrm{O}_{8+\mathrm{Y}}$
Исследование 80 R сверппроподника $\mathrm{Bi}_{2}(\mathrm{Sr}, \mathrm{Ca}){ }_{3} \mathrm{Cu}_{2} \mathrm{O}_{8+\gamma}$ проводилось п широкой области обратного пространстеа с помощьо өремяпролетного нейтронного дифрактометра DН-2 с однокоординатным позицнонно-чупстаительным детектором. Модулацип структуры была уточнена по набору дифракционных рефлексов, полученных от шонодоменного бпока размерами $1,5 \times 1,0 \times 0,03$ ми $^{3}$. Модулпиия признана соизмеримой с периодом 4,75 a, что дает сперхрешетку 19 а $\times \mathrm{b} \times \mathrm{c} / \mathrm{a}$ $=5,397(1)$, b $=5,401(1)$, с = $30,716(3)$ А / и симшетрио Рпая. асновной чертой структуры является периодическое пнедрение дополнительных радов атомоө


 окрушение катионов в




Работа влполнена ${ }_{2}$ набораторин нейтронной физики оияи

Препринт Обзедмненного мнституте ядерних иссладованй. Ду6не 1989

Received by Publishing Department
on November 27, 1989.

## Beskrovnyl A.I, at al

Meutron DIffraction Study of the Modulated
Structure of $\mathrm{Bi}_{2}(\mathrm{Sr}, \mathrm{Ca})_{3} \mathrm{Cu}_{2} \mathrm{O}_{8+}$
The modulated structure of the 80 K superconductor $\mathrm{Bi}_{2}\left(\mathrm{Sr}, \mathrm{Ca}_{\mathbf{a}}\right)_{3} \mathrm{Cu}_{2} \mathrm{O}_{8+Y}$ is refined from the single-crystal neutron diffraction date on monodoma In block of dimenslons $1.5 \times 1.0 \times 0.03 \mathrm{~mm}^{3}$. The modulation is recognized as commensurate with perlod 4.75 a , resulting in the superceli ig a $x$ ox(a = $5.397(1), b=5.401(1), c=30.716(3)$ A and symmetry Pnea. sentlal feature of the structure
 to the bio and sro plane form characterlstic chains running along the aaxis. The coordinat lon of the $\mathrm{Bi}^{3+}$ cations is unlform and conslsts of three mutually nearly perpendicular bonds to oxygens of 2.0-2.2 $A$ lengths. The $\mathrm{Sr}^{2+}$ cat the Sr sltes, located in the vicinity of the inserted oxygen, are possibly vacent. The Ca site situated berween the $\mathrm{CuO}_{2}$ planes is substituted to $30 \%$ by serontium.
The Investlgation has been performed at the Laboratory of Neutron PhysICE, JINR.


[^0]:    1085
    s.

[^1]:    $\mathrm{r}_{\text {hkl }}^{2}=13.2$
    a) Ref. at $\begin{aligned} & \text { at } 1 / 4,1 / 4) \text {. } \\ & x_{j}^{0}=x_{1}^{0}+(j-1) \approx 0.5 \quad \text { (except for } 04 \text { ), }\end{aligned}$
    $x_{j}^{0}=(j-1)+19 / 42-4.75 / 42 \quad$ (for 04),
    $x_{j}^{0}=\left(0.25-x_{)}^{0}\right)(-1)^{j}+0.25 \quad$ (except for 04
     $\left.Y_{j}=0.25+\operatorname{l-1}\right)^{j} \sin \left[0.5 *\left(2 \pi x_{j}^{0} / 4.75-\pi / 2\right)+K \sin \left(2 \pi x_{j}^{0} / 4.75-\pi / 2\right)\right]$.
    where $A=0.168(7), k=1.14(35)$. e) Each site splitted along the c-axis to $\mathrm{z}_{\mathrm{j}} \pm \Delta \mathrm{C}$. e) Each site splitted along the c-axis to $2_{j} \pm \Delta \mathrm{c}$.
    f) Neutron scattering length used: $b_{\mathrm{Cu}}=4.900, \mathrm{~b}_{\mathrm{Sr}}=7.020$,
    $\mathrm{b}_{\mathrm{Ca}}=7.718, \mathrm{~b}_{\mathrm{BI}}=8.526, \quad \mathrm{~b}_{\mathrm{O}}=5.805\left[10^{-25_{\mathrm{m}}} \mathrm{m}\right.$.
    g) Average value over the b-axis modulation.

