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A METHOD FOR RECONSTRUCTION
OF ELECTROMAGNETIC SHOWER PARAMETERS
IN A CALORIMETER
WITH A RECTANGULAR CELLULAR STRUCTURE

[^0]
## 1. Introduction

To detect electromagnetic showers produced by high-energy gamaquanta, hodoscopic calorimeters with a cellular structure are used in some experimental facilities (e.g. see Refs /1-3/). The processing of the experimental data from these detectors consists in reconstruction of the released energy values and the ooordinates of the electromagnetic shower cores.

In this paper an algorithm is proposed for the processing of the data from an electromagnetic calorimeter with square cells of sufficiently large size (as compared with the transverse size of the shower). The method is based on fitting the given model of the shower energy distribution in the calorimeter cells to the real data. This is a computer programme that is part of the software for the HYPERON facility $/ 4,5 /$.

Here are general conditions defining the application range of the method proposed:

1. The calorimeter cells have a square section and are tightly joined together to make a "wall" (see Fig. 1).
2. The transverse dimension of the shower does not exoeed the size of the cell, so a ahower does not hit more than four adjacent cells (a block of 2x2) (see Fig. 2).
3. Let the group of the calorimeter cells where the energy release took place be called a cluster. Each cell of the cluster has at least one common side with any other cell of the oluster, and any two cells of the cluster can be connected by a chain of the cells of the same cluster, the latter cells joined with their sides. Let us suppose the probability of three or more-electromagnetic showers hitting one cluster to be negligible.
4. The model distribution of the energy release of a shower produced by a particle with the energy $a$ and ooordinates $x$, $y$ for the point of bitting the wall is as follows:
a) according to Item 2, the shower releases energies $e_{1}, \theta_{2}, \theta_{3}$, $e_{4}$ in the block of $2 x 2$ adjacent cella;
b) the energies $e_{i}$ are proportional to the energy $e$ of the fincident particle, i.e.

$e_{i}=e f_{i}(x, y)$
c) the quantities $f_{i}(x, y)$ from item $4 b$ are related to one another as

$$
\begin{equation*}
f_{1} \cdot f_{4}=f_{2} f_{3} \tag{2}
\end{equation*}
$$

(in accordance with the numeration in Fig. 2);


Fig. 1


Fig. 2
d) coordinates $x$, $y$ are unambiguously reconstructed by the ratios $f_{1}(x, y) / f_{j}(x, y), \quad 1 \leqslant i<j \leqslant 4$.

Of all these assumptions relation (2) from item 4 c seems to be least evident. Nevertheless, the model of the form

$$
\left\{\begin{array}{l}
f_{1}=R_{1}(x) R_{1}(y)  \tag{3}\\
f_{2}=R_{2}(x) R_{1}(y) \\
f_{3}=R_{1}(x) R_{2}(y) \\
f_{4}=R_{2}(x) R_{2}(y)
\end{array}\right.
$$

turned to be good for description of the results obtained in the test measurements at the HYPERON facility. The functions $R_{1}$ and $R_{2}$ were obtained by approximation of the experimental data $/ 5 \%$.

The electromagnetic. shower parameter reconstruction technique to be considered below has been developed for processing the data from the Shower Hodoscopic Detector (SHD) of HYPERON. It is mainly based on relation (2) from item 4 c , but it also contains several general principles and procedures.

## 2. General scheme of reconstruction of shower parameters

'According to assumption 2 of shower energy release, each shower releases energy in several adjacent cells. On the other hand, aocording to assumption 3, the maximum of two cell-groups can be combined to make a cluster. So it is convenient to divide all the calorimeter cells, where energy was released, into clusters. Thus every shower is in its cluster, and in one cluster there is no more than two showers.

One must ind out, how many showers are in a cluster (one or two), and to reconstruct the parameters of the showers. Division of the cells with the non-zero energy into clusters is a simple oombinatoric problem, so we omit its solution. Note, however, that this part of the programme covers up to $20-40 \%$ of the total processing time even if there is quite a low density of clusters per event (e.g. 2-5 clusters for 190 cells). Thus, its optimization may also be of importance.

Now we turn to the technique of reconstruction of shower parameters inside a cluster. If $C$ is the set of cells making up a cluster, the model distribution of the energy release is fitted to the really measured values of the energy $e_{i}(i \in C)$ by the least squares method:

$$
\begin{equation*}
X^{2}=\sum_{i \in C} \frac{\left(e_{i}-\hat{e}_{i}\right)^{2}}{\cdot d_{i}} \rightarrow i n f \tag{4}
\end{equation*}
$$

where $\hat{e}_{1}, L \in C$ are the "expected" energies, calculated by formula (1) for each cell of the cluster. Formula (4) Includes covariances of occasional errors $d_{i}$ at measurements of the energy $e_{1}$. We assume that the expressions of $d_{1}$ through $e_{i}$ are known (e.g. $d_{i}=c_{0}+$ $\left.c_{1} \cdot e_{i}\right)$.
If the one-shower-per-cluster hypothesis zields a satisfactory fit ( $\mathcal{X}^{2}<X^{2} \lim _{\text {im }}$ ), it is accepted. If not, the parameters of two showers are fitted.

Let us analyse the expression of $X^{2}$ in formula (4). Taking the hypothesis of one shower, one can find a block of $2 \times 2$ oelle (let It be denoted by $B$ ), where the shower released all its energy, for each hypothetical position of the hitting point $(x, y)$. Then

$$
\begin{equation*}
X^{2}=\sum_{i \in B} \frac{\left(e_{i}-\hat{e}_{i}\right)^{2}}{d_{i}}+\sum_{i \in C \backslash B} \frac{e_{i}^{2}}{d_{i}} \tag{5}
\end{equation*}
$$

Quantity (5) can be minimized by the following sckeme: a) to look through all blocks of $2 \times 2$ cells running across the given cluster;
b) to minimize only the first summand of (5) for each block B, since the second summend does not depend on the shower parameters (e, $x, y$ )
c) to choose the smallest value among all minimal values of the function $X^{2}$, obtained above; it will provide the best fit for the parameters of one shower in the given cluster.

The above scheme allows the one-shower-inside-a-cluster hypothesis to be reduced to a problem of minimization of the quantity

$$
\begin{equation*}
L(e, x, y)=\sum_{i=1}^{4} \frac{\left(e_{i}-\hat{e}_{i}\right)^{2}}{d_{i}} \tag{6}
\end{equation*}
$$

for four arbitrary figures $e_{1}, e_{2}, e_{3}, e_{4}$ interpreted as the energy releases in the block of $2 \times 2$ cells. This problem is solved in the maximum general form in section 3.

Checking the hypothesis of two showers, one can find two blocks of $2 \times 2$ cells (denoted by $B_{1}$ and $B_{2}$ ), where two showers released all their energy, for each pair of the hypothetical points ( $x^{(1)}, y^{(1)}$ ), ( $x^{(2)}, y^{(2)}$ ), where the primary particles hit the blocks. Then

$$
\begin{equation*}
\mathcal{X}^{2}=\sum_{i \in B_{1} \cup B_{2}} \frac{\left(e_{i}-\hat{e}_{i}\right)^{2}}{d_{i}}+\sum_{i \in C \backslash\left(B_{1} \cup B_{2}\right)} \frac{e_{i}^{2}}{d_{i}} \tag{7}
\end{equation*}
$$

Quantity (7) can be minimized by the following scheme:
a) to look through all pairs of the blocks of $2 \times 2$ cells running ecross the given cluster;
b) to minimize only the first summand in (7) for each pair of blocks $B_{1}$ and $B_{2}$, aince the second summand does not depend on the shower parameters;
c) to choose the smallest value among all minimal values of the function $X^{2}$, obtained above; it will provide the best fit for the parameters of two showers in the given cluster.

The form of the first summand in (7) largely depends. on the cutual position of blocks $B_{1}$ and $B_{2}$. Four variants are possible:

1) blocks $B_{1}$ and $B_{2}$ colncide;
2) blocks $B_{1}$ and $B_{2}$ heve two common cell;
3) blocks $B_{1}$ and $B_{2}$ have one common cell;
4) blocks $B_{1}$ and $B_{2}$ do not intersect.

In the fourth case the first summend in (7) becomes a sum of two summands of form (6), each depending only on the parameters of one shower. So each summand is minimized separately, uging twice the minimization algorithm of (6), desoribed below in section 3.

Cases 1-3 require independent solutions, they are described in sections 4-6 of the present paper.

## 3. Fitting the parameters of one shower inside a block of $2 x 2$ cells

According to (1), iunction (6) is re-written as

$$
\begin{equation*}
L(e, x, y)=\sum_{i=1}^{4} \frac{\left(e_{i}-e f_{i}(x, y)\right)^{2}}{\alpha_{i}} \tag{8}
\end{equation*}
$$

In the point of the minimum of function ( 8 ) $\partial L / \partial e=0$, which allows the unknown $e$ to be expressed through $x, y$ :

$$
e=\sum_{i=1}^{4} \frac{e_{i} f_{i}(x, y)}{d_{i}} / \sum_{i=1}^{4} \frac{f_{i}^{2}(x, y)}{d_{i}}
$$

Substituting it to ( 8 ) we reduce our problem to minimization of the quantity

$$
\begin{equation*}
L(x, y)=\sum_{i=i}^{4} \frac{f_{i}^{2}(x, y)}{d_{i}} /\left(\sum_{i=1}^{4} \frac{e_{i} f_{i}(x, y)}{d_{i}}\right)^{2} \tag{9}
\end{equation*}
$$

The vital procedure is the introduction of new variables

$$
\begin{equation*}
u_{k}=f_{k}(x, y) / \sum_{i=1}^{4} \frac{e_{i} f_{i}(x, y)}{d_{i}} \tag{10}
\end{equation*}
$$

$k=1,2,3,4$. Then (9) becomes of the form

$$
\begin{equation*}
L\left(u_{1}, u_{2}, u_{3}, u_{4}\right)=\sum_{i=1}^{4} \frac{u_{i}^{2}}{d_{i}} \tag{11}
\end{equation*}
$$

It follows from (2) that

$$
\begin{equation*}
u_{1} u_{4}=u_{2} u_{3} \tag{12}
\end{equation*}
$$

and from the definition of (10) it follows that

$$
\begin{equation*}
\sum_{i=1}^{4} \frac{u_{i} e_{i}}{d_{i}}=1 \tag{13}
\end{equation*}
$$

To stress the importance of introduoing the variables $u_{1}$, we note that they can be considered as the independent variables with restrictions. (12) and (13) imposed on them. Thus, minimization of the function of the general form ( 8 ) is reduced to minimization of a concrete aimple function (11) on the variables $u_{i}$ with restrictions (12) and (13). For the reconstruotion of coordinates $x, y$ by the known $u_{i}$ one can use assumption $4 d$ on the model dietribution.

It is convenient to reduce the number of variables to three by introducing a new one: $t=u_{3} / u_{1}$. Then $u_{3}=t u_{1}$ and, in virtue of (12), $u_{4}=t u_{2}$, so (11) is of the form

$$
\begin{equation*}
L\left(u_{1}, u_{2}, t\right)=u_{1}^{2}\left(\frac{1}{d_{1}}+\frac{t^{2}}{d_{3}}\right)+u_{2}^{2}\left(\frac{1}{d_{2}}+\frac{t^{2}}{d_{4}}\right) \tag{14}
\end{equation*}
$$

and restriction (13) becomes of the form

$$
\begin{equation*}
u_{1}\left(\frac{e_{1}}{d_{1}}+t \frac{e_{3}}{d_{3}}\right)+u_{2}\left(\frac{e_{2}}{d_{2}}+t \frac{e_{4}}{d_{4}}\right)=1 \tag{15}
\end{equation*}
$$

If $t$ is fixed, the minimum of (14) on the variables $u_{1}, u_{2}$ with restriction (15) is achieved at

$$
\begin{gathered}
u_{1}=\left(\frac{e_{1}}{d_{1}}+t \cdot \frac{e_{3}}{d_{3}}\right)\left(\frac{1}{d_{2}}+\frac{t^{2}}{d_{4}}\right) / D \\
u_{2}=\left(\frac{e_{2}}{d_{2}}+t \cdot \frac{e_{4}}{d_{4}}\right)\left(\frac{1}{d_{1}}+\frac{t^{2}}{d_{3}}\right) / D \\
D=\left(\frac{e_{1}}{d_{1}}+t \frac{e_{3}}{d_{3}}\right)^{2}\left(\frac{1}{d_{2}}+\frac{t^{2}}{d_{4}}\right)+\left(\frac{e_{2}}{d_{2}}+t \frac{e_{4}}{d_{4}}\right)^{2}\left(\frac{1}{d_{1}}+\frac{t^{2}}{d_{3}}\right)(17)
\end{gathered}
$$

Substituting these values to (14) we obtain

$$
\begin{equation*}
L(t)=\left(\frac{1}{d_{1}}+\frac{t^{2}}{d_{3}}\right)\left(\frac{1}{d_{2}}+\frac{t^{2}}{d_{4}}\right) / D \tag{18}
\end{equation*}
$$

Function (18) is a fractional-rational one with polynomials of the $4-$ th power in the numerator and the denominator. There is no much difficulty in minimizing it. Making the derivative $L^{\prime}(t)$ equal to zero, we obtain an equation of the 6th degree. We only need the roots in the region $L^{\prime \prime}(t) \geqslant 0$ (there are no more than three roots). The presence of the good initial approximation

$$
t_{0}=\frac{e_{3}+e_{4}}{e_{1}+e_{2}}
$$

facilitates essentially finding the roots. (In order "to see" this approximation, one should use assumptions 4 b and $4 \mathrm{c}: \quad t=u_{3} / u_{1}=$ $\left.u_{4} / u_{2} \approx e_{3} / e_{1} \approx e_{4} / e_{2}\right)$.

We would like to add that the above procedure cannot be used only in two quite rare cases: $e_{1}=e_{4}=0$ and $e_{2}=e_{3}=0$. In these cases function (18) achieves its maximum either at $t=0$ or at $t=\infty$, which turns its minimization into a simple task.

## 4. Checking the hypothesis of two showers for a block of $2 x 2$

Here we consider case 1 from section 2 with blocks $B_{1}$ and $B_{2}$ coincided. In this case $B_{1} \cup B_{2}$ is a block of $2 \times 2$, and the first
summand of (7) includes 4 experimentally measured energies, denoted by $e_{i}, \quad 1 \leqslant i \leqslant 4$, as in section 3 . At the same time the model distribution of two showers depends on six parameters $e^{(1)}, x^{(1)}, y^{(1)}$, $e^{(2)}, x^{(2)}, j^{(2)}$. Such an redundancy of parameters leads to a posm sibility of reducing the first summand of (7) exactly to zero, i.e. the equations $\hat{e}_{i}=e_{i}$ have an exact solution at $i \in B_{1} \cup B_{2}$. Moreover, this is not a single solution (a set of these solutions makes up a two-dimensional surface in the six-dimensional space of parameters of two showers).

Usually, the model does not allow one to choose "the best" of all solutions. So it is enough to show one of them. It can be easily obtained by employing a concrete form of the functions $f_{i}(x, y)$ from (1). In model (3), adopted for the SHD of HYPERON, it is enough to assume that the energies $e_{1}$ and $e_{2}$ are released by one shower, and $e_{3}$ and $e_{4}$ by the other. Then there is no difficulty in reconstructing the shower parameters.

## 5. Checking the hypothesis of two showers for a block of $2 \times 3$

Here we consider case 2 from section 2. In this case $B_{1} \cup B_{2}$ makes up a block of $2 \times 3$ cells. We numerate the cells as shown in Fig. 3 and denote the respective energies by $e_{1}, e_{2}, e_{3}, e_{4}, e_{5}, e_{6}$. The block of $2 \times 3$ can be positioned horizontally and the problem will have a similar solution.
The number of unknown parameters ( $e^{(1)}$, $\left.x^{(1)}, y^{(1)}, e^{(2)}, x^{(2)}, y^{(2)}\right)$ coincides W1th the number of measured energies ( $e_{1}-e_{6}$ ). It allows the assumption that in the general case the equation $\hat{e}_{i}=e_{i}, 1 \leqslant 1 \leqslant 6$, has a solution, and this is the only solution. To obtain it, we assume that block $\mathrm{B}_{1}$ consists of cells 1-4, and block $B_{2}$ consists of cells 3-6. Then, according to (1),

$$
\begin{aligned}
& \hat{e}_{1}=e^{(1)_{p}(1)} ; \hat{e}_{2}=e^{(1)_{p}(1)} \\
& \hat{e}_{3}=e^{(1)_{p}(1)}+e^{(2)_{p}(2)} \\
& \hat{e}_{4}=e^{(1)_{P}(1)}+e^{(2)_{p}(2)} \\
& \hat{e}_{5}=e^{(2)_{p}(2)} ; \hat{e}_{6}=e^{(2)_{P_{4}}(2)},
\end{aligned}
$$

where the functions $f_{i}^{(1)}$ and $f_{i}^{(2)}$ depend on $\left(x^{(1)}, y^{(1)}\right.$ ) and
( $x^{(2)}, y^{(2)}$ ) respectively. Setting $\widehat{e}_{i}$ equal to $e_{i}$ and solving eq. (19), we obtain

$$
\begin{array}{r}
\frac{f_{3}^{(1)}}{f_{4}^{(1)}}=\frac{f_{1}^{(1)}}{f_{2}^{(1)}}=\frac{e_{1}}{e_{2}} ; \frac{f_{3}^{(2)}}{f_{4}^{(2)}}=\frac{f_{1}^{(2)}}{f_{2}^{(2)}}=\frac{e_{5}}{e_{6}} ; \\
\frac{f_{3}^{(1)}}{f_{1}^{(1)}}=\frac{f_{4}^{(1)}}{f_{2}^{(1)}}=\frac{e_{3} e_{6}-e_{4} e_{5}}{e_{1} e_{6}-e_{2} e_{5}} ;  \tag{20}\\
\frac{f_{1}^{(2)}}{f_{3}^{(2)}}=\frac{f_{2}^{(2)}}{f_{4}^{(2)}}=\frac{e_{1} e_{4}-e_{2} e_{3}}{e_{1} e_{6}-e_{2} e_{5}}
\end{array}
$$

The ratios $f_{i}^{(1)} / f_{j}^{(1)}, f_{i}^{(2)} / f_{j}^{(2)}$ allow one to find respective coordinates $x^{(1)}, y^{(1)}$ and $x^{(2)}, y^{(2)}$ using assumption 4d. Using the coordinates, we can find the values of $f_{i}^{(1)}, f_{i}^{(2)}$ and the energies $e^{(1)}, e^{(2)}$ from eq. (19). Thus, the solution is found exactiy.
(1) However, the solution obtained will have a sense only if $e^{(1)} \geqslant 0$ and $e^{(2)} \geqslant 0$. It follows from (20) that in order to have this it is necessary and sufficient that three quantities

$$
d^{\prime}=e_{1} e_{6}^{-e_{2}} e_{5}, \quad d^{\prime \prime}=e_{3} e_{6}^{-e_{4}} e_{5}, \quad d^{\prime \prime}=e_{1} e_{4}^{-e_{2}} e_{3}
$$

are all negative or all positive at the same time.
If the hypothesis of two showers is in good agreement with the $e_{1}-e_{6}$ data, the above condition is satisfied and one cen find an exact solution by formulas (20).

If the hypothesis of two showers does not agree with the $e_{1}{ }^{-e_{6}}$ data well enough, but the discrepancy is not very large, the following "trick" is possible. As shown, the first summand in (7) reaches the absolute minimum (zero) in the point beyond the region of allowable values $f_{i}^{(1)} \geqslant 0, f_{i}^{(2)} \geqslant 0$. If the minimum of (7) lies in the close vicinity of the boundary of the region of allowable values, the minimum of (7) is achieved at the boundary of the region. This boundary consists of points, for which $f_{i}^{(1)}=0$ for some $1 \leqslant i \leqslant 4$, or $f_{i}^{(2)}=0$ for some $1 \leqslant i \leqslant 4$.

The latter conditions mean that one of the showers hits only two of the six cells. It is easy to show that checking two variants, $f_{3}^{(1)}=f_{4}^{(1)}=0$ and $f_{1}^{(2)}=f_{2}^{(2)}=0$, is enough. In both variants the first summand of (7) becomes a sum of two summands, each depending on the parameters of only one shower. Each of the summands is minimized by the method described in section 3.

Finally, let the hypothesis of two showers be in very poor agreement with the measured energies $e_{1} \mathbf{e}_{6}$, so that the above considerations cannot be applied. Then minimization of (7) would require some iteration schemes of the general form, and the above solution could only be used as the initial approximation. Usually, however, this work has no sense for a simple reason: if the hypothesis of two showers poorly agrees with the data, it should be rejected without specifying the shower parameters, because it is senseless to fit the hypothesis known to be inadequate to the real data.
6. Checking the hypothesis of two showers for a block of seven cells

Here we consider case 3 of section 4. In this case $B_{1} \cup B_{2}$ makes up a block of seven cells (Fig. 4a, 4b). We numerate the cells as


Fig. 4a
 -shown in Fig. 4a and denote the respective energies of $e_{1}-e_{7}$. If the block is placed as shown in Fig. 4b, the problem is solved in a similar way.

Let $B_{1}$ consist of cells 1-4 and $B_{2}$ consist of cells 4-7. Then $e_{4}=e_{4}^{\prime}+e_{4}^{1^{\prime}}$, where $e_{4}^{\prime}$ and $e_{4}^{\prime \prime}$ are the energies released in cell 4 by the first and second showers respectively. If the two-shower hypothesis describes the $e_{1}-e_{7}$ data well, then in virtue of (2)
$e_{4}^{\prime} \approx e_{2} \cdot e_{3} / e_{1}$ and $e_{4}^{\prime} \approx e_{5} \cdot e_{6} / e_{7}$.
These relations allow an approximate estimation of $e_{4}^{\prime}$ and $e_{4}^{\prime \prime}$. Taking into account the requirement that $e_{4}^{\prime}+e_{4}^{\prime \prime}=$ $e_{4}$, one can propose the following estimation:

$$
e_{4}^{\prime}=\frac{\frac{e_{2} e_{3}}{e_{1}} e_{4}}{\frac{e_{2} e_{3}}{e_{1}}+\frac{e_{5} e_{6}}{e_{7}}} ; \quad e_{4}^{\prime \prime}=\frac{\frac{e_{5} e_{6}}{e_{7}} e_{4}}{\frac{e_{2} e_{3}}{e_{1}}+\frac{e_{5} e_{6}}{e_{7}}}
$$

Then one can estimate the parameters of both showers by their energy release $e_{1}, e_{2}, e_{3}, e_{4}^{\prime}$ and $e_{4}^{\prime}, e_{5}, e_{6}, e_{7}$, respectively. To do this, one should twice apply the method described in section 3. If there is good agreement between the two-shower hypothesis and the experimental data, we shall obtain the minimum of the first summand of (7) wrth a bigh accuracy.

In the general case, however, the obtained estimations can be only considered as the initial approximation to the sought-for solution. In this case in our programme further minimization of the first summand in (7) went on by the iteration scheme of quite a general form. We only note the general principles of this scheme.

1. Elimination of the unknown $e^{(1)}, e^{(2)}$ (shower energies) by the method described in section 3 for one shower. After that only the method described in section 3 for one shower. After
four unknown quantities remain $\left(x^{(1)}, y^{(1)}, x^{(2)}, y^{(2)}\right)$.
2. Going to new independent arguments $u_{i}^{(k)}, k=1,2$, as in section 3 for one shower (the index $k$ of the variables $u_{i}^{(k)}$ is the number of the shower, they are determined as in section 3).
3. Going further to new independent arguments

$$
t^{(k)}=u_{3}^{(k)} / u_{1}^{(k)} ; g^{(k)}=u_{2}^{(k)} / u_{1}^{(k)}
$$

( $k$ is again the number of the shower), which actually generalizes the variable $t$ of section 3 of the case under consideration.
4. Application of the known method of the gradient descent with the variable step for minimization of the first summand of (7) by $t^{(1)}, s^{(1)}, t^{(2)}, s^{(2)}$.

Implementation of the above principles in the data processing programme allowed a relatively fast and accurate procedure of reconstruction of the shower parameters. Nevertheless, this procedure is quite slow as compared with the methods described in sections 3-5. It was not further optimized, because the clusters of this type (i.e: with the blocks like 4 a or 4 b ) are quite rarely encountered in practice.

## 7. Results of the test processing of the experimental data

The above algorithm was used to reconstruct the events in the experimental investigations of the $K^{+}$- meson decays at the HYPERON facility. To calibrate and check the algorithm, the decays $\mathrm{K}^{+} \rightarrow$ $\pi^{+} \mathbb{T}^{0}\left(\pi^{\circ} \rightarrow 2 \delta\right)$ were reconstructed. At first the energies and coordinates of gamma-quanta, reconstructed by two methods, were compared. The first method uses the programme with the above algorithm, the second one involves the standard package MINUIT/6/ for minimization of functional (4). Figs 5a and 5b show distributions of the differences of the electromagnetic shomer core coordinates reconstructed by the two methods. As seen, in $98 \%$ of the cases the difference of the coordinates is within $2 \sigma(\sigma=10 \mathrm{~mm}) / 4 /$. Fig. 6 shows distributions of the differences of the reconstructed energy values. They are also in good agreement within the measurement errors $/ 4 /$.


The main advantage of the proposed algorithm is its fast action. Fig. 7 shows the time distribution of the reconstructed two-cluster events $\left(K^{+} \rightarrow \pi^{+} \pi^{0}, \pi^{0} \rightarrow 2 \gamma\right)$. For these events the programme with the above algorithm reconstructs the energies and coordinates of the showers 8.1 times faster than MNUIT. It reduced the processing time almost by an order of magnitude (the comparison was carried out at an IBM/AT-type computer).

The proposed method also allowed a $10-12 \%$ increase in the number of the reconstructed decays of $\mathrm{K}^{+}$-mesons owing to a higher efficiency
of the algorithm in determination of the parameters of the overlapping showers (when more than 5 cells of the electromagnetic calorimeter are in operation).

Fig. 8 shows the effective
 mass of $\pi$ from the decays $K^{+} \rightarrow \pi^{+} \pi^{c}$ for 2028 reconstructed events. The mean value of the $\pi^{0}$ mass is in good agreement with the table value $(134.9 \mathrm{MeV})$, and the peak width ( 30 MeV at halfmaximum) corresponds to the one obtained in simulation and agrees with the experimental data $/ 7 /$ and $/ 8 /$.

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Метод восстановления параметров электромагнитных
ливней в калориметре с прямоугольной ячеистой струк турой

СОставной частью установки ГИПЕРОН /ЛЯП, ОИЯИ/ и мноГих других современных экспериментов является ливневый годоскопический детектор /ЛГД/-калориметр с ячейками прямоугольной формы. В работе рассмотрена модель распределения энерговыделений в ячейках ЛГД и предложено аналитическое решение задачи подгонки модельного распределения к реальным данным. Соответствующая программа была включена в систему математического обеспечения установки ГИПЕРОН и позволила ускорить обработку данных в 8 раз с повышением надежности на $10 \%$.

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A Method for Reconstruction of Electromagnetic
Shower Parameters in a Calorimeter with
a Rectangular Cellular Structure
The Shower Hodoscopic Detector (SHD) is an important part of the detector HYPERON (INP, JINR) as well as many other up-to-date detectors. It is a calorimeter with rectangular cells. In the present paper we consider a model of the distribution of energy release in the SHD cells and propose as analytical solution of the problem of fitting the model distribution to experimental data. The corresponding programme was included in the HYPERON software and allowed one to raise the rate of the data processing 8-9 times with about $10 \%$ reliability increase.

The investigation has been performed at the Laboratory of Computing Techniques and Automation, JINR.

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