объединенный
институт
ядерных
исследований
дубна

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A HIGH STATISTICS MEASUREMENT OF THE PROTON STRUCTURE FUNCTIONS $F_2(x,Q^2)$ AND R FROM DEEP INELASTIC MUON SCATTERING AT HIGH Q^2

BCDMS Collaboration

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We present results on the structure functions of the proton measured with high statistics in deep inelastic scattering of muons on a hydrogen target. In the one-photon exchange approximation, the deep inelastic muon-proton cross section can be written as

$$\frac{d^2\sigma}{dQ^2dx} = \frac{4\pi\alpha^2}{Q^4 x}\left[1 - y - \frac{Q^2}{4E^2} + \frac{y^2E^2 + Q^2}{2E^2(R(x,Q^2)+1)}\right]\cdot F_2(x,Q^2) \quad (1)$$

where E is the energy of the incident beam, Q^2 the squared four-momentum transfer between the muon and the proton, and x and y are the Bjorken scaling variables. This cross section depends on two structure functions F_2 and R, where $R = \sigma_L/\sigma_T$ is the ratio of absorption cross sections for virtual photons of longitudinal and transverse polarization. R is related to F_2 and to the longitudinal structure function F_L by

$$R(x,Q^2) = \frac{F_L(x,Q^2)}{(1+4M^2x^2/Q^2)\cdot F_2(x,Q^2) - F_L(x,Q^2)}, \quad (2)$$

where M is the mass of the proton.

The data were collected at the CERN SPS muon beam with a high-luminosity spectrometer which is described in more detail elsewhere[1]. It consists of a 40 m long segmented toroidal iron magnet which is magnetized close to saturation and surrounds a 30 m long "internal" liquid hydrogen target. The iron absorbs the hadronic shower after a few meters and the surviving scattered muon is focused towards the spectrometer axis. The toroids are instrumented with scintillation trigger counters and multiwire proportional chambers. A 10 m long "external" target in front of the spectrometer magnet extends the acceptance of the apparatus to smaller angles, i.e. to smaller values of x and Q^2 than are accessible

According to equation (1) the measured cross section depends on the two functions $R = \sigma_L/\sigma_T$ and F_2. Both functions can be separated by comparing cross sections at the same value of x and Q^2, measured at different beam energies. In this analysis we have chosen to compare the values of four test F_2's, called $F_2^*(R)$, obtained at the four beam energies assuming trial values for R. The experimental value of R was then obtained together with the parameters of a common phenomenological parametrization of F_2 by minimizing the χ^2 of the four $F_2^*(R)$ with respect to this parametrization. This was done separately in each bin of x under the assumption that R (eq.2) is independent of Q^2 in our kinematic range, as suggested by QCD calculations which predict only a weak (logarithmic) variation of the longitudinal structure function F_L with Q^2 /10/

$$F_L(x,Q^2) = \alpha_s(Q^2)/2\pi \cdot x^2 \int_x^1 \left[\frac{8}{3} F_2(z,Q^2) + \frac{40}{9}\left(1-\frac{x}{z}\right) z G(z,Q^2) \right] \frac{dz}{z^3}, \qquad (3)$$

where $\alpha_s(Q^2)$ is the running coupling constant of QCD. The theoretical prediction R_{QCD} was computed from equations (2) and (3) assuming a gluon momentum distribution $xG(x,Q_0^2) = 4.5 \cdot (1-x)^8$ at $Q_0^2 = 5$ GeV and a QCD mass scale parameter $\Lambda = 220$ MeV /9/. In the kinematic range of our experiment, this prediction does not depend strongly on the gluon distribution assumed. Equation (3) does not account for effects of the charm quark mass and for target mass corrections which were included following Refs. /11/ and /12/, respectively. The experimental results for R are given in Table 2 and are compared to the QCD prediction in Fig.1 together with earlier hydrogen data in a similar kinematical range by the European Muon Collaboration (EMC) /13/. At $x > 0.20$, the measured values are compatible with zero in agreement with our carbon target measurement /2/. At smaller x, the data show a rise which is consistent with the QCD prediction.

R_{QCD} was used to compute the final structure functions at the different beam energies which are given in Tables 3-6 and are shown[1)] in Fig.2.

1) A version of this paper containing detailed tables of $F_2(x,Q^2)$ with statistical and systematic errors is available /3/.

Table 2. Results for $R = \sigma_L/\sigma_T$ as a function of x. R is assumed to be independent of Q^2 in each bin of x.

x	< Q² > (GeV²)	R	statistical error	systematic error
0.07	15	0.167	0.134	0.074
0.10	20	0.122	0.078	0.062
0.14	20	0.163	0.055	0.040
0.18	25	0.121	0.051	0.031
0.225	30	0.046	0.032	0.028
0.275	35	0.025	0.027	0.022
0.35	40	0.023	0.025	0.022
0.45	45	−0.011	0.035	0.027
0.55	50	0.005	0.056	0.039
0.65	50	−0.057	0.092	0.071

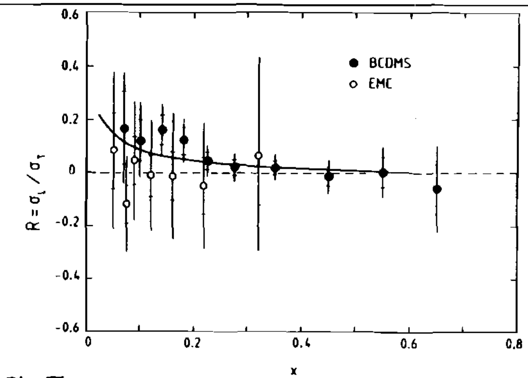

Fig.1. $R = \sigma_L/\sigma_T$ measured in this experiment (BCDMS) as a function of x. Also shown is the measurement by the EMC on a hydrogen target /13/. Inner error bars are statistical only, outer error bars are statistical and systematic errors combined linearly. The solid line is the next-to-leading order QCD prediction using $\Lambda_{\overline{MS}} = 220$ MeV and a gluon distribution $xG(x,Q_0^2) = 4.5(1-x)^8$ at $Q_0^2 = 5\,GeV^2$.

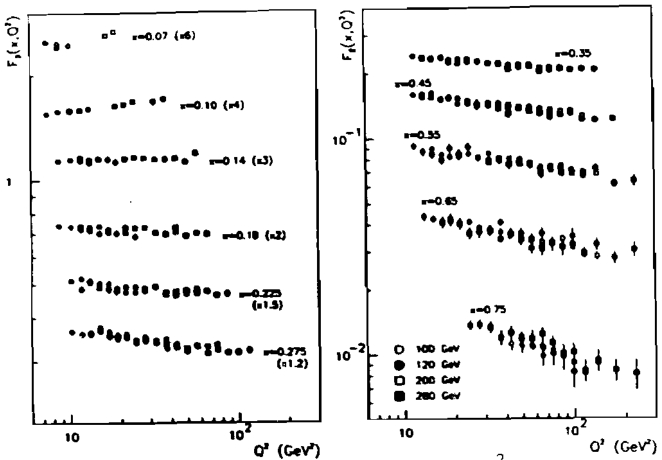

Fig.2. The proton structure function $F_2(x,Q^2)$ measured at the four beam energies 100, 120, 200 and 280 GeV, using $R=R_{QCD}$. At x<0.275, $F_2(x,Q^2)$ has been multiplied by the factors shown in the figure. Only statistical errors are shown.

The agreement between the different data sets in the region of large x allows to set stringent limits on most of the systematic errors as is discussed in more detail in Ref.[2]. The final $F_2(X,Q^2)$ from the combined data sets is shown in Fig.3.

The scaling violations which are observed in these data are compared to predictions from perturbative QCD in a separate paper [9].

Also shown in Fig.3 are the earlier EMC data from muon-hydrogen scattering[13] and the SLAC-MIT results from electron-hydrogen scattering at lower Q^2 [14]. The x dependence of F_2 from this experiment is compared to the EMC result in Fig.4 where the data are averaged over the Q^2 range common to both measurements. The agreement is poor, especially at small x where F_2 measured in the present experiment is larger by up to 15%. In the lowest bin of x, about 4% of this difference is due to the fact that the EMC result was obtained using R = 0. A similar behaviour

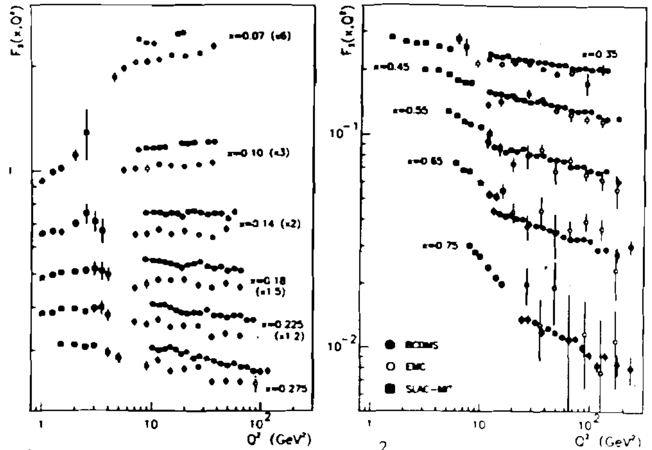

Fig.3. The structure function $F_2(x,Q^2)$ from this experiment for all beam energies combined, using $R=R_{QCD}$. Also shown are data from the EMC[13] and SLAC-MIT[14] experiments. Where necessary, the EMC and SLAC data were interpolated to the x bins of this experiment at each value of Q^2 using a third order polynomial. Note that there are no SLAC data in the lowest x bin. The relative normalizations between the experiments have not been adjusted. At x<0.255, all data have been multiplied by the factors indicated in the figure. Only statistical errors are shown.

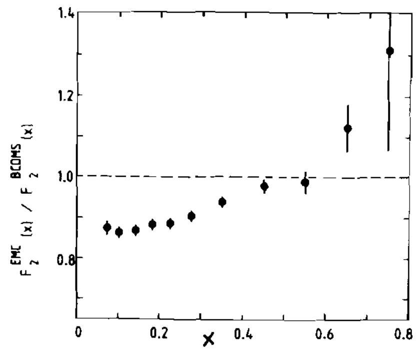

Fig.4. The ratio of the proton structure functions $F_2(x)$ from this and from the EMC experiment[13]. In each bin of x, the data are averaged over the Q^2 range common to both measurements. Only statistical errors are shown. Systematic errors are difficult to visualize because of correlation effects but can be found in detail in Ref.[3,13]. The systematic errors estimated for this experiment do not explain the observed discrepancy.

was observed in our measurement on a carbon target[2] which indicated a steeper x dependence of F_2 than measured in earlier experiments. A quantitative comparison to the SLAC data is difficult at small x where the experiments cover disjoint ranges of Q^2. At large x, the two experiments agree within the systematic errors.

In conclusion, we have presented a high statistics measurement of the proton structure functions F_2 and R from deep inelastic scattering of muons at high Q^2 on a hydrogen target. The systematic uncertainties are comparable to the statistical accuracy of the results. $R = \sigma_L/\sigma_T$ is found to be in good agreement with the perturbative QCD predictions.

Table 3. $F_2(x,Q^2)$ measured at 100 GeV beam energy. The average beam energy at the interaction vertex is <E> =99.1 GeV. Q^2 is given in GeV^2. $F_2(x,Q^2)$ is given both for $R = \sigma_L/\sigma_T = 0 (F_2^0)$ and for $R = R_{QCD}(F_2^1)$. The statistical error ΔF_2 applies to F_2^0 and can be scaled to apply to F_2^1. The systematic errors are given as multiplicative factors to be applied to $F_2(x,Q^2)$: f_b, f_s and f_r are the uncertainties due to beam momentum calibration, spectrometer magnetic field calibration and spectrometer resolution, respectively; f_d is the systematic error due to detector and trigger inefficiencies and f_n is due to the uncertainty in the relative normalization of data from external and internal targets. The overall normalization uncertainty discussed in the text is not shown here.

x	Q^2	F_2^0	ΔF_2	F_2^1	f_b	f_s	f_r	f_d	f_n
0.07	7.50	0.38934	0.00600	0.40205	0.997	0.959	1.001	1.015	1.010
	8.75	0.37624	0.00521	0.39363	0.997	0.959	1.013	1.015	1.010
0.10	7.50	0.38055	0.00424	0.38468	0.996	0.997	1.003	1.005	1.010
	8.75	0.38347	0.00351	0.38926	0.997	0.998	1.007	1.005	1.010
	10.25	0.37960	0.00362	0.38772	0.997	0.999	1.007	1.005	1.010
0.14	8.75	0.37560	0.00390	0.37768	0.996	0.997	1.002	1.000	1.010
	10.25	0.37676	0.00396	0.37965	0.996	0.997	1.004	1.000	1.010
	11.75	0.37259	0.00430	0.37641	0.997	0.998	1.006	1.000	1.010
	13.25	0.36575	0.00468	0.37062	0.997	0.998	1.002	1.000	1.010
	15.00	0.37196	0.00481	0.37847	0.997	0.999	1.005	1.000	1.010
0.18	8.75	0.36786	0.00489	0.36886	0.995	0.996	0.995	1.000	1.010
	10.25	0.36457	0.00474	0.36592	0.996	0.997	1.001	1.000	1.010
	11.75	0.36492	0.00501	0.36670	0.996	0.997	1.002	1.000	1.010
	13.25	0.36270	0.00534	0.36497	0.996	0.998	1.005	1.000	1.010
	15.00	0.36228	0.00521	0.36523	0.997	0.998	1.003	1.000	1.010
	17.00	0.35350	0.00571	0.35727	0.997	0.999	0.998	1.000	1.010
0.225	10.25	0.34051	0.00481	0.34120	0.995	0.997	0.999	1.000	1.010
	11.75	0.34545	0.00501	0.34635	0.996	0.997	1.000	1.000	1.010
	13.25	0.33693	0.00520	0.33805	0.996	0.998	1.001	1.000	1.010
	15.00	0.33517	0.00490	0.33659	0.996	0.998	0.999	1.000	1.010
	17.00	0.31962	0.00522	0.32138	0.997	0.999	1.002	1.000	1.010
	19.00	0.32172	0.00578	0.32395	0.997	0.999	1.004	1.000	1.010
	21.50	0.31154	0.00552	0.31436	0.997	0.999	1.003	1.000	1.010
	24.50	0.32112	0.00522	0.32498	0.997	1.000	0.999	1.000	1.000
	28.00	0.31410	0.00529	0.31917	0.997	1.000	1.003	1.000	1.000
0.275	10.25	0.30440	0.00536	0.30476	0.996	0.998	0.987	1.000	1.010
	11.75	0.29925	0.00545	0.29971	0.996	0.998	0.994	1.000	1.010
	13.25	0.30155	0.00574	0.30213	0.996	0.999	0.997	1.000	1.010
	15.00	0.30341	0.00527	0.30414	0.997	0.999	0.998	1.000	1.010
	17.00	0.30373	0.00564	0.30467	0.997	0.999	0.999	1.000	1.010
	19.00	0.28923	0.00592	0.29035	0.997	1.000	0.997	1.000	1.010
	21.50	0.29763	0.00559	0.29911	0.997	1.000	0.999	1.000	1.010
	24.50	0.27886	0.00498	0.28068	0.997	1.000	1.000	1.000	1.000
	28.00	0.28971	0.00507	0.29223	0.997	1.000	1.004	1.000	1.000
	32.50	0.28090	0.00471	0.28428	0.998	1.001	1.003	1.000	1.000
	37.50	0.26784	0.00583	0.27224	0.998	1.001	1.002	1.000	1.000
0.35	11.75	0.24001	0.00427	0.24021	0.998	1.002	0.988	1.000	1.010
	13.25	0.23349	0.00434	0.23373	0.998	1.002	0.991	1.000	1.010
	15.00	0.23093	0.00383	0.23122	0.998	1.002	0.993	1.000	1.010
	17.00	0.23689	0.00410	0.23727	0.998	1.002	0.995	1.000	1.010
	19.00	0.22257	0.00416	0.22300	0.998	1.002	0.996	1.000	1.010
	21.50	0.23218	0.00388	0.23275	0.998	1.002	0.998	1.000	1.010
	24.50	0.22318	0.00283	0.22389	0.998	1.002	0.997	1.000	1.004
	28.00	0.22454	0.00353	0.22548	0.998	1.002	0.996	1.000	1.000
	32.50	0.21917	0.00320	0.22042	0.998	1.002	1.002	1.000	1.000
	37.50	0.21761	0.00344	0.21929	0.998	1.002	0.999	1.000	1.000
	43.00	0.21422	0.00367	0.21644	0.998	1.002	1.000	1.000	1.000
0.45	11.75	0.16020	0.00409	0.16027	1.004	1.012	1.002	1.000	1.010
	13.25	0.15598	0.00430	0.15606	1.003	1.011	0.995	1.000	1.010
	15.00	0.15493	0.00378	0.15503	1.003	1.010	0.994	1.000	1.010
	17.00	0.15323	0.00403	0.15335	1.002	1.009	0.999	1.000	1.010
	19.00	0.15558	0.00429	0.15573	1.001	1.008	1.004	1.000	1.010
	21.50	0.14470	0.00362	0.14488	1.001	1.008	0.996	1.000	1.010
	24.50	0.14443	0.00256	0.14465	1.000	1.007	0.998	1.000	1.004
	28.00	0.13996	0.00313	0.14024	1.000	1.006	0.997	1.000	1.000
	32.50	0.14332	0.00282	0.14370	0.999	1.006	0.996	1.000	1.000
	37.50	0.14506	0.00310	0.14557	0.999	1.005	0.998	1.000	1.000
	43.00	0.14063	0.00311	0.14129	0.999	1.005	0.996	1.000	1.000
	49.50	0.13379	0.00310	0.13463	0.999	1.005	0.998	1.000	1.000
	57.00	0.13603	0.00354	0.13718	0.998	1.004	0.998	1.000	1.000

0.55	11.75	0.09286	0.00316	0.09289	1.016	1.031	1.021	1.000	1.010
	13.25	0.08784	0.00329	0.08787	1.014	1.028	1.015	1.000	1.010
	15.00	0.08998	0.00306	0.09002	1.012	1.025	1.012	1.000	1.010
	17.00	0.08469	0.00308	0.08473	1.010	1.023	1.008	1.000	1.010
	19.00	0.08286	0.00319	0.08291	1.008	1.021	1.006	1.000	1.010
	21.50	0.08279	0.00289	0.08285	1.007	1.018	1.003	1.000	1.010
	24.50	0.08513	0.00206	0.08520	1.005	1.017	1.006	1.000	1.004
	28.00	0.08099	0.00199	0.08108	1.004	1.015	1.008	1.000	1.004
	32.50	0.08516	0.00236	0.08528	1.003	1.013	1.005	1.000	1.000
	37.50	0.08100	0.00247	0.08115	1.002	1.012	1.002	1.000	1.000
	43.00	0.08005	0.00251	0.08024	1.001	1.010	1.000	1.000	1.000
	49.50	0.07690	0.00250	0.07715	1.000	1.009	0.999	1.000	1.000
	57.00	0.07387	0.00267	0.07418	1.000	1.009	0.999	1.000	1.000
	65.50	0.07196	0.00287	0.07237	0.999	1.008	0.998	1.000	1.000
0.65	13.25	0.04389	0.00187	0.04390	1.034	1.060	1.084	1.000	1.010
	15.00	0.04264	0.00166	0.04265	1.030	1.054	1.071	1.000	1.010
	17.00	0.04166	0.00184	0.04167	1.026	1.048	1.063	1.000	1.010
	19.00	0.04150	0.00198	0.04151	1.022	1.044	1.052	1.000	1.010
	21.50	0.04010	0.00178	0.04012	1.018	1.039	1.044	1.000	1.010
	24.50	0.04115	0.00121	0.04117	1.015	1.035	1.028	1.000	1.003
	28.00	0.03869	0.00121	0.03871	1.013	1.031	1.026	1.000	1.003
	32.50	0.03826	0.00143	0.03829	1.010	1.027	1.021	1.000	1.000
	37.50	0.03662	0.00161	0.03666	1.008	1.024	1.015	1.000	1.000
	43.00	0.03524	0.00166	0.03529	1.006	1.021	1.011	1.000	1.000
	49.50	0.03303	0.00166	0.03309	1.004	1.019	1.008	1.000	1.000
	57.00	0.03363	0.00184	0.03371	1.003	1.017	1.006	1.000	1.000
	65.50	0.02980	0.00186	0.02989	1.002	1.015	1.005	1.000	1.000
	75.00	0.03194	0.00217	0.03206	1.001	1.014	1.003	1.000	1.000
0.75	24.50	0.01357	0.00064	0.01357	1.040	1.076	1.088	1.000	1.000
	28.00	0.01365	0.00068	0.01366	1.033	1.067	1.072	1.000	1.000
	32.50	0.01307	0.00065	0.01308	1.027	1.059	1.064	1.000	1.000
	37.50	0.01169	0.00074	0.01170	1.022	1.052	1.051	1.000	1.000
	43.00	0.01105	0.00079	0.01106	1.018	1.046	1.046	1.000	1.000
	49.50	0.01082	0.00084	0.01083	1.014	1.040	1.037	1.000	1.000
	57.00	0.01148	0.00100	0.01149	1.011	1.036	1.025	1.000	1.000
	65.50	0.00966	0.00102	0.00968	1.008	1.032	1.021	1.000	1.000
	75.00	0.01031	0.00119	0.01033	1.006	1.028	1.017	1.000	1.000

Table 4. As Table 3; for the measurement at 120 GeV beam energy. The average beam energy at the interaction vertex is <E> = 117.9 GeV.

x	Q^2	F_2^0	ΔF_2	F_2^1	f_b	f_s	f_r	f_d	f_n
0.07	8.75	0.37824	0.00583	0.38956	0.997	0.999	1.003	1.015	1.010
	10.25	0.37381	0.00596	0.38982	0.997	0.999	1.008	1.015	1.010
0.10	10.25	0.38707	0.00456	0.39249	0.997	0.998	1.005	1.005	1.010
	11.75	0.38341	0.00476	0.39066	0.997	0.998	1.006	1.005	1.010
	13.25	0.38291	0.00516	0.39239	0.997	0.999	1.004	1.005	1.010

0.14	11.75	0.38246	0.00571	0.38505	0.996	0.997	1.002	1.000	1.010
	13.25	0.37607	0.00583	0.37936	0.996	0.998	1.004	1.000	1.010
	15.00	0.37557	0.00564	0.37987	0.997	0.998	1.004	1.000	1.010
	17.00	0.37197	0.00627	0.37759	0.997	0.999	1.002	1.000	1.010
	19.00	0.36233	0.00684	0.36935	0.997	0.999	1.000	1.000	1.010
0.18	11.75	0.36009	0.00686	0.36127	0.995	0.997	0.998	1.000	1.010
	13.25	0.35608	0.00688	0.35757	0.996	0.997	1.000	1.000	1.010
	15.00	0.34792	0.00643	0.34979	0.996	0.998	1.002	1.000	1.010
	17.00	0.35021	0.00693	0.35267	0.997	0.998	1.003	1.000	1.010
	19.00	0.34539	0.00745	0.34847	0.997	0.999	1.003	1.000	1.010
	21.50	0.35670	0.00694	0.36087	0.997	0.999	1.002	1.000	1.010
	24.50	0.33272	0.00798	0.33792	0.997	0.999	1.000	1.000	1.010
0.225	11.75	0.32274	0.00660	0.32331	0.995	0.997	1.002	1.000	1.010
	13.25	0.34040	0.00703	0.34116	0.996	0.997	1.002	1.000	1.010
	15.00	0.32526	0.00632	0.32619	0.996	0.998	1.001	1.000	1.010
	17.00	0.33403	0.00678	0.33525	0.996	0.998	1.000	1.000	1.010
	19.00	0.31631	0.00705	0.31776	0.997	0.999	1.002	1.000	1.010
	21.50	0.32392	0.00648	0.32585	0.997	0.999	1.003	1.000	1.010
	24.50	0.31374	0.00709	0.31622	0.997	0.999	1.001	1.000	1.010
	28.00	0.31301	0.00592	0.31632	0.997	1.000	1.003	1.000	1.000
	32.50	0.31897	0.00582	0.32366	0.997	1.000	1.002	1.000	1.000
0.275	13.25	0.30041	0.00785	0.30080	0.996	0.998	1.003	1.000	1.010
	15.00	0.31094	0.00731	0.31145	0.996	0.999	1.006	1.000	1.010
	17.00	0.29574	0.00722	0.29635	0.997	0.999	1.002	1.000	1.010
	19.00	0.29560	0.00754	0.29636	0.997	0.999	1.005	1.000	1.010
	21.50	0.29235	0.00676	0.29332	0.997	1.000	1.000	1.000	1.010
	24.50	0.28614	0.00484	0.28738	0.997	1.000	1.003	1.000	1.004
	28.00	0.28387	0.00463	0.28549	0.997	1.000	0.998	1.000	1.004
	32.50	0.28255	0.00472	0.28478	0.997	1.000	1.001	1.000	1.002
	37.50	0.28359	0.00609	0.28665	0.998	1.001	1.004	1.000	1.000
	43.00	0.26798	0.00615	0.27188	0.998	1.001	1.006	1.000	1.000
0.35	13.25	0.23697	0.00604	0.23713	0.998	1.002	1.006	1.000	1.010
	15.00	0.23426	0.00545	0.23446	0.998	1.002	1.006	1.000	1.010
	17.00	0.23448	0.00534	0.23473	0.998	1.002	1.001	1.000	1.010
	19.00	0.22909	0.00549	0.22939	0.998	1.002	1.004	1.000	1.010
	21.50	0.22136	0.00466	0.22173	0.998	1.002	0.997	1.000	1.010
	24.50	0.23127	0.00351	0.23176	0.998	1.002	1.004	1.000	1.004
	28.00	0.22575	0.00332	0.22638	0.998	1.002	1.003	1.000	1.004
	32.50	0.22033	0.00319	0.22116	0.998	1.002	1.000	1.000	1.003
	37.50	0.22098	0.00413	0.22210	0.998	1.002	1.000	1.000	1.000
	43.00	0.21710	0.00418	0.21858	0.998	1.002	1.004	1.000	1.000
	49.50	0.20737	0.00422	0.20928	0.998	1.002	1.001	1.000	1.000
	57.00	0.21152	0.00496	0.21417	0.998	1.002	1.004	1.000	1.000
0.45	13.25	0.15958	0.00593	0.15964	1.005	1.013	1.003	1.000	1.010
	15.00	0.16145	0.00548	0.16152	1.004	1.012	0.997	1.000	1.010
	17.00	0.15240	0.00528	0.15248	1.003	1.011	0.996	1.000	1.010
	19.00	0.15374	0.00554	0.15384	1.002	1.010	1.007	1.000	1.010
	21.50	0.15342	0.00480	0.15355	1.002	1.009	1.002	1.000	1.010
	24.50	0.14968	0.00319	0.14984	1.001	1.008	1.000	1.000	1.004
	28.00	0.14585	0.00303	0.14605	1.000	1.007	1.003	1.000	1.004
	32.50	0.14579	0.00291	0.14605	1.000	1.006	0.999	1.000	1.003

	37.50	0.14296	0.00316	0.14330	0.999	1.006	0.999	1.000	1.002
	43.00	0.14187	0.00365	0.14231	0.999	1.005	1.004	1.000	1.000
	49.50	0.13688	0.00367	0.13745	0.999	1.005	1.003	1.000	1.000
	57.00	0.13681	0.00386	0.13757	0.999	1.005	1.007	1.000	1.000
	65.50	0.13381	0.00421	0.13481	0.998	1.004	1.002	1.000	1.000
	75.00	0.12253	0.00479	0.12375	0.998	1.004	1.000	1.000	1.000
0.55	15.00	0.08494	0.00385	0.08496	1.015	1.030	1.018	1.000	1.010
	17.00	0.07999	0.00362	0.08002	1.013	1.027	1.015	1.000	1.010
	19.00	0.09073	0.00451	0.09077	1.011	1.024	1.006	1.000	1.010
	21.50	0.08537	0.00371	0.08541	1.009	1.022	1.007	1.000	1.010
	24.50	0.09156	0.00433	0.09161	1.007	1.019	1.006	1.000	1.010
	28.00	0.08154	0.00229	0.08160	1.006	1.017	1.006	1.000	1.004
	32.50	0.07923	0.00220	0.07931	1.004	1.015	1.003	1.000	1.003
	37.50	0.07860	0.00247	0.07870	1.003	1.014	1.004	1.000	1.002
	43.00	0.07617	0.00285	0.07629	1.002	1.012	1.004	1.000	1.000
	49.50	0.07888	0.00300	0.07905	1.001	1.011	1.003	1.000	1.000
	57.00	0.07464	0.00309	0.07485	1.001	1.010	1.001	1.000	1.000
	65.50	0.06671	0.00320	0.06696	1.000	1.009	1.000	1.000	1.000
	75.00	0.07039	0.00357	0.07074	0.999	1.008	0.999	1.000	1.000
	86.00	0.07020	0.00379	0.07066	0.999	1.007	1.002	1.000	1.000
0.65	17.00	0.04111	0.00214	0.04112	1.032	1.057	1.069	1.000	1.010
	19.00	0.04282	0.00238	0.04283	1.028	1.052	1.059	1.000	1.010
	21.50	0.04106	0.00218	0.04107	1.024	1.046	1.055	1.000	1.010
	24.50	0.03654	0.00230	0.03655	1.020	1.041	1.046	1.000	1.010
	28.00	0.03692	0.00225	0.03694	1.017	1.037	1.038	1.000	1.010
	32.50	0.03679	0.00136	0.03681	1.013	1.032	1.028	1.000	1.003
	37.50	0.04065	0.00170	0.04068	1.011	1.028	1.022	1.000	1.002
	43.00	0.03612	0.00184	0.03615	1.009	1.025	1.018	1.000	1.000
	49.50	0.03589	0.00198	0.03593	1.007	1.022	1.015	1.000	1.000
	57.00	0.03042	0.00193	0.03047	1.005	1.020	1.011	1.000	1.000
	65.50	0.03560	0.00231	0.03567	1.003	1.018	1.010	1.000	1.000
	75.00	0.03168	0.00243	0.03176	1.002	1.016	1.008	1.000	1.000
	86.00	0.03041	0.00251	0.03051	1.001	1.014	1.009	1.000	1.000
	99.00	0.03436	0.00295	0.03451	1.000	1.013	1.006	1.000	1.000
0.75	32.50	0.01335	0.00075	0.01335	1.035	1.070	1.075	1.000	1.000
	37.50	0.01194	0.00084	0.01194	1.029	1.061	1.068	1.000	1.000
	43.00	0.01238	0.00091	0.01239	1.024	1.054	1.061	1.000	1.000
	49.50	0.01155	0.00097	0.01156	1.019	1.048	1.054	1.000	1.000
	57.00	0.01169	0.00105	0.01170	1.015	1.042	1.046	1.000	1.000
	65.50	0.01056	0.00117	0.01057	1.012	1.037	1.041	1.000	1.000
	75.00	0.00992	0.00124	0.00993	1.009	1.033	1.030	1.000	1.000
	86.00	0.00961	0.00134	0.00963	1.006	1.029	1.026	1.000	1.000
	99.00	0.00815	0.00131	0.00817	1.004	1.026	1.020	1.000	1.000

Table 5. As Table 3, for the measurement at 200 GeV beam energy. The average beam energy at the interaction vertex is $\langle E \rangle = 196.3$ GeV.

x	Q^2	F_2^0	ΔF_2	F_2^1	f_b	f_s	f_r	f_d	f_n
0.07	17.00	0.39928	0.00521	0.41459	0.997	0.999	0.996	1.015	1.005
	19.00	0.39989	0.00527	0.41972	0.998	1.000	1.005	1.015	1.005
0.10	19.00	0.39548	0.00407	0.40180	0.997	0.999	1.004	1.005	1.005
	21.50	0.39338	0.00317	0.40171	0.997	0.999	1.006	1.005	1.005
	24.50	0.39402	0.00339	0.40528	0.997	0.999	1.003	1.005	1.005
0.14	21.50	0.37841	0.00361	0.38121	0.996	0.998	1.005	1.000	1.005
	24.50	0.37991	0.00378	0.38366	0.997	0.998	1.007	1.000	1.005
	28.00	0.37499	0.00362	0.37999	0.997	0.999	1.003	1.000	1.005
	32.50	0.36709	0.00356	0.37396	0.997	0.999	1.004	1.000	1.005
0.18	21.50	0.35061	0.00419	0.35183	0.996	0.997	1.005	1.000	1.005
	24.50	0.36077	0.00434	0.36243	0.996	0.998	1.002	1.000	1.005
	28.00	0.36004	0.00413	0.36224	0.997	0.998	1.003	1.000	1.005
	32.50	0.34712	0.00288	0.35007	0.997	0.999	1.004	1.000	1.003
	37.50	0.34052	0.00302	0.34450	0.997	0.999	0.998	1.000	1.002
	43.00	0.34255	0.00301	0.34801	0.997	1.000	1.001	1.000	1.002
0.225	28.00	0.32246	0.00384	0.32347	0.996	0.998	0.997	1.000	1.005
	32.50	0.32715	0.00365	0.32855	0.997	0.999	1.002	1.000	1.005
	37.50	0.31302	0.00276	0.31485	0.997	0.999	0.999	1.000	1.002
	43.00	0.31337	0.00269	0.31585	0.997	1.000	1.003	1.000	1.002
	49.50	0.30607	0.00264	0.30939	0.997	1.000	1.005	1.000	1.002
	57.00	0.31349	0.00363	0.31816	0.998	1.000	1.003	1.000	1.000
0.275	28.00	0.28822	0.00409	0.28872	0.997	0.999	1.003	1.000	1.005
	32.50	0.28252	0.00372	0.28319	0.997	1.000	0.996	1.000	1.005
	37.50	0.27908	0.00290	0.27997	0.997	1.000	1.000	1.000	1.003
	43.00	0.27264	0.00272	0.27380	0.997	1.000	0.998	1.000	1.002
	49.50	0.27001	0.00272	0.27157	0.997	1.000	1.004	1.000	1.002
	57.00	0.27276	0.00292	0.27491	0.997	1.001	1.001	1.000	1.002
	65.50	0.26985	0.00361	0.27275	0.998	1.001	1.004	1.000	1.000
	75.00	0.26068	0.00385	0.26446	0.998	1.001	1.007	1.000	1.000
0.35	32.50	0.22221	0.00276	0.22247	0.998	1.002	0.998	1.000	1.005
	37.50	0.21985	0.00209	0.22019	0.998	1.002	1.002	1.000	1.003
	43.00	0.21666	0.00201	0.21710	0.998	1.002	1.004	1.000	1.002
	49.50	0.21473	0.00196	0.21531	0.998	1.002	1.003	1.000	1.002
	57.00	0.21410	0.00203	0.21488	0.998	1.002	1.005	1.000	1.002
	65.50	0.20758	0.00210	0.20861	0.998	1.002	0.998	1.000	1.001
	75.00	0.20193	0.00258	0.20327	0.998	1.002	1.001	1.000	1.000
	86.00	0.20554	0.00273	0.20739	0.998	1.002	1.006	1.000	1.000
	99.00	0.20033	0.00297	0.20279	0.998	1.002	1.003	1.000	1.000
0.45	32.50	0.14298	0.00266	0.14306	1.002	1.010	1.006	1.000	1.005
	37.50	0.13689	0.00276	0.13699	1.002	1.009	1.003	1.000	1.005
	43.00	0.13873	0.00183	0.13886	1.001	1.008	1.004	1.000	1.002
	49.50	0.13676	0.00179	0.13693	1.000	1.007	1.001	1.000	1.002
	57.00	0.13594	0.00185	0.13616	1.000	1.006	0.997	1.000	1.002
	65.50	0.13030	0.00183	0.13059	0.999	1.006	1.003	1.000	1.002
	75.00	0.12735	0.00225	0.12772	0.999	1.005	1.002	1.000	1.000
	86.00	0.13085	0.00235	0.13136	0.999	1.005	1.005	1.000	1.000
	99.00	0.12724	0.00243	0.12791	0.999	1.005	1.000	1.000	1.000
	115.50	0.12334	0.00239	0.12426	0.998	1.004	1.003	1.000	1.000
0.55	32.50	0.07733	0.00202	0.07735	1.011	1.025	1.021	1.000	1.005
	37.50	0.08019	0.00227	0.08022	1.009	1.022	1.017	1.000	1.005
	43.00	0.07591	0.00135	0.07595	1.007	1.019	1.012	1.000	1.002
	49.50	0.07558	0.00136	0.07563	1.006	1.017	1.011	1.000	1.002

	57.00	0.07589	0.00145	0.07595	1.004	1.015	1.006	1.000	1.002
	65.50	0.07090	0.00142	0.07098	1.003	1.013	1.002	1.000	1.001
	75.00	0.07022	0.00155	0.07032	1.002	1.012	1.002	1.000	1.001
	86.00	0.07299	0.00191	0.07313	1.001	1.011	1.004	1.000	1.000
	99.00	0.06683	0.00188	0.06700	1.000	1.010	1.001	1.000	1.000
	115.50	0.06513	0.00185	0.06536	1.000	1.009	1.000	1.000	1.000
	137.50	0.06621	0.00196	0.06655	0.999	1.008	1.003	1.000	1.000
0.65	32.50	0.03721	0.00122	0.03722	1.028	1.053	1.052	1.000	1.005
	37.50	0.03407	0.00130	0.03408	1.024	1.046	1.049	1.000	1.005
	43.00	0.03538	0.00078	0.03539	1.019	1.041	1.041	1.000	1.001
	49.50	0.03512	0.00083	0.03513	1.016	1.036	1.036	1.000	1.001
	57.00	0.03327	0.00086	0.03329	1.013	1.032	1.027	1.000	1.001
	65.50	0.03248	0.00092	0.03250	1.011	1.028	1.019	1.000	1.001
	75.00	0.03213	0.00100	0.03215	1.008	1.025	1.012	1.000	1.001
	86.00	0.03359	0.00126	0.03362	1.006	1.022	1.009	1.000	1.000
	99.00	0.03080	0.00128	0.03084	1.005	1.020	1.010	1.000	1.000
	115.50	0.02839	0.00125	0.02844	1.003	1.017	1.007	1.000	1.000
	137.50	0.02780	0.00130	0.02787	1.001	1.015	1.004	1.000	1.000
0.75	43.00	0.01252	0.00042	0.01252	1.048	1.090	1.110	1.000	1.000
	49.50	0.01189	0.00044	0.01189	1.041	1.079	1.099	1.000	1.000
	57.00	0.01076	0.00046	0.01076	1.034	1.070	1.092	1.000	1.000
	65.50	0.01068	0.00052	0.01068	1.028	1.061	1.084	1.000	1.000
	75.00	0.01117	0.00058	0.01117	1.024	1.054	1.078	1.000	1.000
	86.00	0.00999	0.00058	0.01000	1.018	1.048	1.066	1.000	1.000
	99.00	0.00905	0.00060	0.00906	1.015	1.042	1.059	1.000	1.000
	115.50	0.00813	0.00061	0.00814	1.011	1.037	1.048	1.000	1.000
	137.50	0.00903	0.00068	0.00904	1.007	1.032	1.037	1.000	1.000

Table 6. As Table 3, for the measurement at 280 GeV beam energy. The average beam energy at the interaction vertex is <E> = 277.0 GeV.

	Q^2	F_2^0	ΔF_2	F_2^1	f_b	f_s	f_r	f_d	f_n
0.10	32.50	0.39629	0.00559	0.40558	0.997	0.999	1.008	1.005	1.005
	37.50	0.39408	0.00630	0.40695	0.998	1.000	1.004	1.005	1.005
0.14	37.50	0.37285	0.00654	0.37701	0.997	0.999	1.005	1.000	1.005
	43.00	0.37063	0.00645	0.37628	0.997	0.999	1.004	1.000	1.005
	49.50	0.35668	0.00661	0.36420	0.997	1.000	1.004	1.000	1.005
	57.00	0.37001	0.00802	0.38075	0.998	1.000	1.004	1.000	1.005
0.18	37.50	0.34630	0.00695	0.34807	0.996	0.998	0.998	1.000	1.005
	43.00	0.35894	0.00694	0.36142	0.997	0.999	0.999	1.000	1.005
	49.50	0.33701	0.00706	0.34020	0.997	0.999	1.002	1.000	1.005
	57.00	0.34082	0.00475	0.34527	0.997	1.000	1.002	1.000	1.002
	65.50	0.33512	0.00504	0.34112	0.998	1.000	1.003	1.000	1.002
0.225	37.50	0.31199	0.00658	0.31280	0.996	0.998	0.996	1.000	1.005
	43.00	0.30882	0.00631	0.30989	0.997	0.999	1.004	1.000	1.005
	49.50	0.31671	0.00659	0.31821	0.997	0.999	1.001	1.000	1.005
	57.00	0.30994	0.00435	0.31194	0.997	1.000	1.001	1.000	1.002
	65.50	0.31282	0.00470	0.31557	0.997	1.000	0.998	1.000	1.002

	75.00	0.30247	0.00499	0.30609	0.997	1.000	1.000	1.000	1.002
	86.00	0.30229	0.00533	0.30722	0.998	1.001	1.003	1.000	1.001
0.275	37.50	0.27396	0.00704	0.27435	0.997	0.999	0.997	1.000	1.005
	43.00	0.27856	0.00659	0.27909	0.997	1.000	1.000	1.000	1.005
	49.50	0.26652	0.00657	0.26720	0.997	1.000	0.997	1.000	1.005
	57.00	0.27485	0.00459	0.27580	0.997	1.000	0.995	1.000	1.002
	65.50	0.26066	0.00471	0.26187	0.997	1.000	1.004	1.000	1.002
	75.00	0.27476	0.00518	0.27649	0.997	1.001	1.004	1.000	1.002
	86.00	0.25960	0.00508	0.26182	0.998	1.001	1.000	1.000	1.002
	99.00	0.25794	0.00630	0.26097	0.998	1.001	0.998	1.000	1.000
	115.50	0.25851	0.00693	0.26278	0.998	1.001	0.998	1.000	1.000
0.35	43.00	0.20759	0.00472	0.20778	0.998	1.002	0.995	1.000	1.005
	49.50	0.21481	0.00480	0.21507	0.998	1.002	0.997	1.000	1.005
	57.00	0.21242	0.00329	0.21277	0.998	1.002	0.995	1.000	1.002
	65.50	0.20092	0.00333	0.20136	0.998	1.002	0.996	1.000	1.002
	75.00	0.20936	0.00360	0.20997	0.998	1.002	0.997	1.000	1.002
	86.00	0.20583	0.00358	0.20664	0.998	1.002	0.995	1.000	1.002
	99.00	0.20313	0.00375	0.20421	0.998	1.002	0.996	1.000	1.002
	115.50	0.20358	0.00441	0.20511	0.998	1.002	0.998	1.000	1.000
	137.50	0.20044	0.00472	0.20266	0.998	1.002	0.998	1.000	1.000
0.45	43.00	0.12927	0.00441	0.12933	1.003	1.011	0.989	1.000	1.005
	49.50	0.13776	0.00453	0.13784	1.002	1.010	0.989	1.000	1.005
	57.00	0.13211	0.00296	0.13221	1.001	1.009	0.994	1.000	1.002
	65.50	0.12867	0.00308	0.12880	1.001	1.008	0.996	1.000	1.002
	75.00	0.13325	0.00326	0.13342	1.000	1.007	0.998	1.000	1.002
	86.00	0.12660	0.00317	0.12682	1.000	1.006	0.996	1.000	1.002
	99.00	0.13142	0.00336	0.13172	0.999	1.006	0.998	1.000	1.002
	115.50	0.11975	0.00329	0.12014	0.999	1.005	0.996	1.000	1.001
	137.50	0.11797	0.00388	0.11853	0.999	1.005	0.999	1.000	1.000
	175.00	0.11841	0.00365	0.11937	0.998	1.004	0.998	1.000	1.000
0.55	43.00	0.07503	0.00349	0.07505	1.012	1.027	0.995	1.000	1.005
	49.50	0.07680	0.00348	0.07682	1.010	1.024	0.994	1.000	1.005
	57.00	0.07392	0.00221	0.07395	1.008	1.021	0.996	1.000	1.002
	65.50	0.06995	0.00234	0.06999	1.006	1.018	0.996	1.000	1.002
	75.00	0.07265	0.00258	0.07270	1.005	1.016	0.999	1.000	1.002
	86.00	0.06750	0.00247	0.06756	1.004	1.015	1.000	1.000	1.002
	99.00	0.06949	0.00262	0.06957	1.003	1.013	1.001	1.000	1.002
	115.50	0.06775	0.00263	0.06786	1.002	1.012	0.999	1.000	1.001
	137.50	0.07042	0.00324	0.07058	1.001	1.010	0.998	1.000	1.005
	175.00	0.05990	0.00273	0.06013	0.999	1.009	0.996	1.000	1.000
	230.00	0.06091	0.00366	0.06133	0.999	1.007	0.996	1.000	1.000
0.65	49.50	0.03371	0.00212	0.03372	1.027	1.051	1.032	1.000	1.005
	57.00	0.03359	0.00136	0.03360	1.022	1.045	1.025	1.000	1.002
	65.50	0.03077	0.00138	0.03078	1.018	1.039	1.016	1.000	1.002
	75.00	0.03236	0.00156	0.03237	1.015	1.035	1.012	1.000	1.002
	86.00	0.03091	0.00160	0.03092	1.012	1.031	1.009	1.000	1.001
	99.00	0.03182	0.00173	0.03184	1.010	1.027	1.007	1.000	1.001
	115.50	0.02900	0.00167	0.02902	1.007	1.024	1.007	1.000	1.001
	137.50	0.03160	0.00221	0.03164	1.005	1.021	1.006	1.000	1.000
	175.00	0.02724	0.00189	0.02729	1.002	1.017	1.008	1.000	1.000
	230.00	0.02965	0.00248	0.02975	1.000	1.014	1.007	1.000	1.000

0.75	57.00	0.01165	0.00077	0.01165	1.054	1.098	1.124	1.000	1.000
	65.50	0.01225	0.00087	0.01225	1.046	1.086	1.109	1.000	1.000
	75.00	0.01111	0.00091	0.01111	1.038	1.076	1.092	1.000	1.000
	86.00	0.00985	0.00088	0.00985	1.032	1.067	1.077	1.000	1.000
	99.00	0.01010	0.00098	0.01010	1.027	1.059	1.054	1.000	1.000
	115.50	0.00833	0.00093	0.00833	1.021	1.051	1.050	1.000	1.000
	137.50	0.00925	0.00106	0.00926	1.016	1.044	1.041	1.000	1.000
	175.00	0.00832	0.00098	0.00833	1.010	1.035	1.036	1.000	1.000
	230.00	0.00798	0.00130	0.00799	1.005	1.028	1.020	1.000	1.000

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Бенвенути А.С. и др. E1-89-540

Измерение структурных функций протона $F_2(x,Q^2)$ и R с высокой статистической точностью в глубоконеупругом рассеянии мюонов при больших значениях Q^2

Приведены результаты измерения структурных функций протона $F_2(x,Q^2)$ и R с высокой статистической точностью. Измерения выполнены в экспериментах, в которых изучалось глубоконеупругое рассеяние мюонов в пучке 100, 120, 200 и 280 ГэВ. Для анализа полученных данных отобрано $1{,}8\cdot10^6$ событий, расположенных в кинематической области $0{,}06 \le x \le 0{,}80$ и 7 ГэВ$^2 \le Q^2 \le$ 260 ГэВ^2. Получено, что при малых значениях x структурная функция R отличается от нуля, что согласуется с предсказаниями пертурбативной модели КХД.

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Benvenuti A.C. et al. E1-89-540

A High Statistics Measurement of the Proton Structure Functions $F_2(x,Q^2)$ and R from Deep Inelastic Muon Scattering at High Q^2

We present results on a high statistics study of the proton structure functions $F_2(x,Q^2)$ and $R=\sigma_L/\sigma_T$ measured in deep inelastic scattering of muons on a hydrogen target. The analysis is based on $1.8\cdot10^6$ events after all cuts, recorded at beam energies of 100, 120, 200 and 280 GeV and covering a kinematic range $0.06 \le x \le 0.80$ and 7 GeV$^2 \le Q^2 \le$ 260 GeV^2. At small x, we find R to be different from zero in agreement with predictions of perturbative QCD.

The investigation has been performed at the Laboratory of High Energies, JINR.

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