# ОБЪЕДИНЕННЫЙ ИНСТИТУТ ЯДЕРНЫХ ИССЛЕДОВАНИЙ <br> -ЛАБОРАТОРИЯ ЯДЕРНЫХ ПРОБЛЕМ <br> 1Levenberg, V.Pokrovaky, Rhen De-Hou, L. Tarasova, I. Yutlandov 

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THE ( $p, \mathrm{pn}$ ) AND ( $\mathrm{p}, \mathrm{n}$ ) REACTIONS ON $\mathrm{Sc}^{45}$
INDUCED BY HIGH-ENERGY PROTONS
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## E-1384



THE ( $p, p n$ ) AND ( $p, n$ ) REAETIONS ON Sc 45 INDUCED BY HIGH-ENERGY PROTONS

The present paper proceeds with our work on the study of simple nuclear reactions on complex nuclei, in particular, of the influence of the target-nucleus structure upon them. The ${ }_{21} \mathrm{Sc}^{43}$ nucleus close by A and Z to ${ }_{20} \mathrm{Ca}^{48}$, already studied by ourselves, was used as a target. The chosen target gave also the possibility of determining the relative yields of isomers from the reaction ( $\mathrm{p}, \mathrm{pn}$ ).
2. Experimental Procedure

### 2.1. The target and the conditions of irradiation

The target was pressed in the form of a rectangular tablet ( $15 \times 4 \times 1 \mathrm{~mm}{ }^{3}$ ) of scandium oxide. The conclusion on the proper degree of the target material purity was drawn basing on the fact that in the scandium fraction separated after the irradiation no isotopes with mass numbers $>44$ have been found. Those isotopes would be inevitably produced in the presence of heavy admixtures.

Targets were irradiated in the internal proton beam of the Joint Nuclear Research Institute synchrocyclotron during 15-20 minutes. The thickness of the target along the beam was $\approx 1 \mathrm{~mm}$. The variation of the incident proton energy was achieved by suitable choice of target radius. The determination of the proton beam intensity was made by the yield of the reaction $A l^{27} \quad(p, 3 p n) \mathrm{Na}^{24}$.

The contribution of the reaction ( $n, 2 n$ ) to the cross-section of the reaction ( $p, p_{n}$ ) was neglected, the earlier estimates $/ 1 /$ being taken into consideration.

### 2.2 Chemical treatment of the target

The major mass of the irradiated target was dissolved in the concentrated hydrochloric acid saturated with gaseous $\mathrm{HCl}, 15 \mathrm{mg}$ of the titanium carrier being present. In order to speed up the process of the complete target dissolution scandium and titanium chlorides and the undissolved fraction of the scandium oxide were transformed into sulfate by e vaporating with concentrated $\mathrm{H}_{2} \mathrm{SO}_{4}$. The sulfates Sc and Ti , thus obtained, were easily dissolved in hot water. Scandium and titanium hydro-oxides were precipitated from the solution by adding $\mathrm{NH}_{4} \mathrm{OH}$. The precipitation washed was dissolved in hot concentrated HCl . A small amount of $30 \% \mathrm{H}_{2} \mathrm{O}_{2}$ was added to the solution and Sc was extracted by tributilphosphate $/ 2 /$. Then radiochemical purification of scandium and titanium fractions was made.

The purification of the scandium fraction consisted of two operations: the precipitation of scandium ftoride with the aid of $\mathrm{Na}_{2} \mathrm{SiF}_{6}$ and the extraction of scandium by tributilphosphate from the concentrated solution of HCl in the presence of $\mathrm{H}_{2} \mathrm{O}_{2}$ and some milligramms of titanium as holdback carrier. Finally scandium was precipitated in the hydroxide form. $\mathrm{On}_{\mathrm{n}}$ completing the measurements scandium hydroxide was heated and weighed in the $\mathrm{S}_{\mathbf{2}} \mathrm{O}_{3}$ form.

The purification of titanium fraction consisted of three operations: the precipitation of titanium hydroxide in the presence of the complexon III and iron ions; the scavenging by the iron sulfide in the presence of tartaric acid; the extraction of titanium cupferronate from IN HCl by chloroform: Finally titanium was precipitated in the hydroxide form. $\mathrm{O}_{\mathrm{n}}$ accomplishing the measurements titanium hydroxide was heated and weighed in $\mathrm{T}_{\mathrm{i}} \mathrm{O}_{2}$ form.
2.3. Measurements of activity

The measurements of the sample activity were performed with a scintillation $y$--spectrometer $/ 1 /$. Radioactive characteristics of isotopes $/ 3,4,5$ / used in the calculation of the cross-sections of the reactions under study are given in Table 1.

## Table 1.

| Nucleus | Half-life | Energy of the <br> specific $\gamma-$ <br> line (KeV) | Number of <br> v-rays/decay |
| :---: | :---: | :---: | :---: |
| $\mathrm{Na}^{24}$ | $I 5,0 \mathrm{~h}$ | $I 368$ | $I 00$ |
| $\mathrm{Sc}^{44 \mathrm{~m}}$ | 59 | h | $I I 60$ |
| $\mathrm{Sc}^{44 \mathrm{~g}}$ | $3,9 \mathrm{~h}$ | $I I 60$ | $I 00$ |
| $\mathrm{TI}^{45}$ | $3,09 \mathrm{~h}$ | $5 I I$ | $I 00$ |
|  |  | $I 00$ |  |

The decay scheme of $\mathrm{Sc}^{44}$ is shown in Fig. 1. The law of changing with time $\mathrm{I}_{1180}$, the intensity of the 1160 $\mathrm{KeV} \quad y$-line, is as follows:

$$
I_{11 \sigma 0}=\left(A_{g}^{\circ}-A_{m}^{\circ} \frac{\lambda_{\varepsilon}}{\lambda_{\varepsilon}-\lambda_{m}}\right) e^{-\lambda_{g} t}+A_{m}^{\circ}-\frac{\lambda_{g}}{\lambda_{g}-\lambda_{m}} e^{-\lambda_{m} t}
$$

where
$A^{\circ} \quad$ is the activity at the end of irradiation,
$\lambda$ is the decay constant,
$t \quad$ is the time passed from the end of irradiation, and the subscripts $m$ and $g$ refer to the isomeric and ground state of $\mathrm{Sc}{ }^{44}$ respectively.

The activity $A_{m}^{0}=\lambda_{m} N_{m}^{N_{m}}$, where $N_{m}^{0}$ is the number of $S c{ }^{44 m}$ nuclei produced for the time of irradiation, i.e. the value necessary for calculating the cross-section. The activity $A_{g}^{0}$ involves also the term taking into account the accumulation of $S c^{448}$ from $\mathrm{Sc}^{44 m_{1}}$ during irradiation. However, in our case this contribution can be neglected. The error introduced into the cross-section under study $\sigma_{g}$ is not larger than $0.2 \%$.

Thus, the measurements of $I_{1160^{\circ}}$ provide all the necessary information for the determination of $\sigma_{m}$ and $\sigma_{a}$.

- As for the detection of annihilation radiation of $\mathrm{Ti}^{65}$ one may say that under the conditions of our measurements positron annihilation occured mainly on the crystal surface and only one 511 KeV gamma-ray per decay should have been registered. However, due to annihilation in the surrounding shielding etc. this number was somewhat larger than unity and was determined experimentally with the $\mathrm{Na}_{\mathrm{a}}{ }^{22}$ isotope, the decay scheme of which is well known.


## 3. Experimental Results

The values of the cross-sections of the reactions $\mathrm{Sc}^{45}$ ( $\mathrm{p}, \mathrm{pn}$ ) and $\mathrm{Sc} \mathrm{c}^{5} \quad(\mathrm{p}, \mathrm{n}) \mathrm{in} \mathrm{mb}$, the ratios of the cross-
sections of $\mathrm{S}_{\mathrm{c}}{ }^{448}$ and $\mathrm{S}_{\mathrm{c}}{ }^{44 \mathrm{~m}}$ productions and the cross-sections of the monitor reaction/6/ in the energy range of incident protons from 120 to 670 MeV are enlisted in Table 2. For the sake of comparison the cross-sections of the reactions ( $\mathrm{p}, \mathrm{pn}$ ) and $(\mathrm{p}, \mathrm{n})$ on $\mathrm{C}_{\mathrm{a}}{ }^{48}$, taken from ref. ${ }^{1 /}$ are also given in the same Table.

Table 2

| $\mathrm{E}_{\mathrm{p}}, \mathrm{MeV}$ | I20 | 200 | 300 | 400 | 500 | 600 | 670 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $S c^{45}(p, p n)$ | $\begin{array}{r} 70, I \\ \pm \quad 1,8 \end{array}$ | $\begin{array}{r} 50,4 \\ \pm \quad I, 2 \end{array}$ | 48,5 $\pm I, 2$ | 47,7 $\pm 1,0$ | $43, I$ $\pm I, 0$ | 42,0 $\pm 0,7$ | $\begin{array}{r} 39,4 \\ \pm \quad 0,7 \end{array}$ |
| $S c^{45}(p, n)$ | $\begin{array}{r} 3,80 \\ \pm 0,07 \end{array}$ | $\begin{array}{r} 2,29 \\ \pm 0,03 \end{array}$ | $\begin{array}{r} I, 82 \\ \pm 0,04 \end{array}$ | $\begin{array}{r} I, 40 \\ \pm 0,07 \end{array}$ | $\begin{array}{r} I, I 4 \\ \pm 0,09 \end{array}$ | $\begin{array}{r} I, 07 \\ \pm 0,09 \end{array}$ | $\begin{array}{r} 0,83 \\ \pm 0,02 \end{array}$ |
| $S c^{44 g} / S c^{44 m}$ | $\begin{array}{r} 2, I 0 \\ \pm 0,06 \end{array}$ | $\begin{array}{r} 2,2 I \\ \pm 0,03 \end{array}$ | $\begin{array}{r} 2, I 9 \\ \pm 0,01 \end{array}$ | $\begin{array}{r} 2,22 \\ \pm 0,01 \end{array}$ | 2,19 $\pm 0,06$ | $\begin{array}{r} 2,18 \\ \pm 0,02 \end{array}$ | $\begin{array}{r} 2,20 \\ \pm 0,04 \end{array}$ |
| $C a^{48}(p, p n)$ | $I I 8 \pm 2$ | $106 \pm 10$ | $106 \pm 4$ | $101 \pm 4$ | $104 \pm 1$ | $110 \pm 8$ | $110 \pm 2$ |
| $\mathrm{Ca}^{48}(\mathrm{p}, \mathrm{n})$ | $\begin{array}{r} 7,8 \\ \pm 0,3 \end{array}$ | $\begin{array}{r} 4,7 \\ \pm 1,2 \end{array}$ | $\begin{array}{r} 4,1 \\ \pm 0,3 \end{array}$ | 3,6 $+0,1$ | $\begin{array}{r} 3,9 \\ \pm 0,2 \end{array}$ | $\begin{array}{r} 2,2 \\ \pm 0,2 \end{array}$ | $\begin{array}{r} 2,6 \\ \pm 0,1 \end{array}$ |
| $A 1^{27}(p, 3 p n)$ | 10,2 | 9,1 | 11,0 | 11,3 | 11,1 | 11,0 | 10,9 |

The above values are average from three or four determinations, with standard errors. The total accuracy of the cross-section determination is $\approx \overline{\mathbf{0}} \%$ according to our evaluation. In our estimation as well as in calculation of the cross-sections and standard errors possible systematic errors due to the inaccuracy in the decay schemes and in the cross-section of the monitor reaction were not taken into consideration.

It is worth noting that the evaluation of the accuracy of the determination of the isomeric cross-section ratio is about $5 \%$ and depends, mainly, upon the accuracy of the decay curve resolving.
4. Discuasion of the Results

### 4.1. Excitation functions

As is seen from Table 2 and Fig. 2, the cross-sections of the reactions under study decrease monotonously with increasing energy of the incident proton. The cross-section of the reaction ( $p, n$ ) is reduced more sharply than that of the reaction ( $p, p n$ ).

The behaviour of the excitation functions of the reactions $\mathrm{S}_{\mathrm{c}}{ }^{45}$ ( $\mathrm{p}, \mathrm{pn}$ ) and $\mathrm{Ca}^{45}$ ( $\mathrm{p}, \mathrm{pn}$ ) differ from each other. In the case of $\mathrm{C}_{\mathrm{a}}{ }^{48}$ the cross-section of the reaction ( $\mathrm{p}, \mathrm{pa}$ ) beginning from 200 MeV remains practically constant. This difference appears to be due to a possiblecontribution of the reaction $\mathrm{Ca}^{48}$ ( $\mathrm{p}, 2 \mathrm{p}$ ) to the value of the reation
$(p, p n) / 1 /$. The values of the ( $p, 2 p$ ) reaction, judging by the published data $/ 7,8 /$ tend to increasing with increasing incident proton energy, which may give rise to the constancy of : $\sigma_{p, p n}$ observed.

$$
\text { 4.2 The absol ute values of } \sigma_{p, p n}
$$

First of all, one should note a considerable difference in the values of thecross-sections of the reactions ( $\mathrm{p}, \mathrm{pn}$ ) on nuclei close by $A$ and $Z$ ( see Table 2). This circumstance directly shows the strong influence of the target-nuclens structure.

At present such reactions are supposed to take place by direct interaction of the incident proton with the nucleons of the nuclear diffuse surface. This assumption was explicitaly discussed and treated experimentally for the $\mathrm{GeV}_{\mathrm{e}} \mathrm{V}$ incident particle energy range by Benioff $/ 9 /$ and a number of other authors e.g. $10,1 \mathrm{l}$. According to our assumptions $/ \mathbf{1 /}$, this mechanism becones predominating even in the proton energy range of the order of 200 MeV . Remsberg $/ 12 /$ has drawn the analogous conclusion. According to his evaluation at least $90 \%$ of the ( $p, p \mathrm{p}$ ) reaction occurs by the direct knock-on mechanism at $E_{p}=370 \mathrm{MeV}$. Then the cross-section of the ( $\mathrm{p}, \mathrm{pn}$ ) reaction should be proportional to the number of neutrons the knocking on of which from the nucleus does not give rise to excitation exceeding the nucleon binding energy.

Thus, for the ( $\mathrm{p}, \mathrm{pn}$ ) reaction those neutrons are available which are in a shell whose distance below the topmost occupied level is smaller than the binding energy of the least bound particle in the product nucleus. The least bound particle in the $\mathrm{Sc}^{44}$ nucleus is a neutron with the separationenergyof $9.7 \mathrm{Me}^{\mathrm{V}} / 5 /$. According to the scheme of nucleon energy levels in the nucleus which was calculated by Ross et al. ${ }^{13 /}$, in the case of $\mathrm{Sc}^{45}$ neatrons situated on the levels $1 f_{7 / 2}(4), 1 d_{3 / 2}(4), 2 s_{1 / 2}(2)$ satisfy this condition. $I_{n}$ brackets is given the number of neutrons on the appropriate level. Now if one makes use of the calculation scheme and parameters, quoted in ref. $/ 9 /$, then for the proton energy of 3 GeV the cross-section of the ( $\mathrm{p}, \mathrm{pn}$ ) reaction is determined by the expression

$$
\sigma_{p, p n}=36 \Sigma \mathrm{NM},
$$

where $N$ is the number of neutrons on the given levels and $M$ is their fractional availability for the ( $p, p n$ ) reaction. Summation is performed over all the available levels. The calculation gives the value of the $\mathrm{Sc}^{45}$ ( $\mathrm{p}, \mathrm{pn}$ ) reaction cross-section to be 39.5 mb . In our calculation we used the value of $\mathbb{M}$ for the half density radius parameter $r_{0}=1.07 \mathrm{f}$.

Taking into consideration weak energy dependence $\sigma_{p, p n}$, one may say that the above evaluation is in good agrement, with our data. This confirms once more the assumption on the primary role of the mechanism of direct neutron knock-on process in the energy region of the order of a magnitude of hundreds MeV .

In the case of $\mathrm{Ca}^{18}$. the same levels $1 \mathrm{f}_{7 / 2}$ (8), $1 \mathrm{~d}_{3 / 2}$ (4), $2 \mathrm{~s}_{1 / 2}$ (2) appear to be available. The increase of the number of available neutrons from 10 to 14 should give rise to the proportional increase of the cross-section of the ( $p, \mathrm{pn}$ ) reaction. $\mathrm{A}_{s}$ is seen from Table 2, the cross-section of the reaction $\mathrm{C}_{\mathrm{a}}{ }^{4 s}$ ( $\mathrm{p}, \mathrm{pn}$ ) is larger than it might be expected from the above considerations. However, this excees may be explained by the contribation of the ( $p, 2 \mathrm{p}$ ) reaction. Thus, for $\mathrm{E}_{\mathrm{p}}=400 \mathrm{MeV}$ the cross-section of the reaction $\mathrm{Ca}^{48}$ ( $\mathrm{p}, \mathrm{pn}$ ) should have been about 70 mb . With this proton energy the cross-sections of the reaction $\mathrm{Si}^{30}(\mathrm{p}, 2 \mathrm{p})$ and $\mathrm{Zn}^{68}(\mathrm{p}, 2 \mathrm{p})$ are about $20 \mathrm{mb} / 8$ / while in the reaction $\mathrm{Zr}^{96}(\mathrm{p}, 2 \mathrm{p})$ it is about $40 \mathrm{mb} / 7 /$. The excess of the experimental cross-section of the reaction $C_{a}{ }^{48}$ ( $\mathrm{p}, \mathrm{pn}$ ) over the expected one is about $30-35 \mathrm{mb}$, which agrees fairly well with the quoted cross-sections of ${ }^{*}$ Copftiotents $M_{\text {for }} S^{45}{ }^{\text {and }} \mathrm{Ca}^{48}$ are praotioally equal.
the reaction ( $p, 2 p$ ). We confined ourselves to the evaluation of the contribution of the reaction ( $p, 2 p$ ) only at 400 MeV , since at larger energies of incident protons there is no information on the cross-section of the reaction ( $p, 2 \mathrm{p}$ ), while at lower energies the comparison would not be so convincing due to the reduction of relative role of the direct knock-on mechanism.
4.3. Comparison of the reactions ( $p, p n$ ) and ( $p, n$ )

In our previous paper $/ 1 /$ it has been noted that the ratio $\sigma_{p, p n} / \sigma_{p, n}$ is strongly dependent upon the incident proton energy and practically is independent of the number of nucleons in the target-nucleus. As is seen from Fig. 3, the corresponding ratios for $\mathrm{Sc}^{45}$ agree well with the previous situation.

However, if one takes into account that $\sigma_{p, p n} \quad$ for $\mathrm{Ca}^{48}$ and $\mathrm{Th}^{232}$ contains a noticeable contribution from the reaction ( $p, 2 \mathrm{p}$ ) , then one should, evidently, divide all the available data into two groups which are somewhat different by the value of the ratio $\sigma_{p, p n} / \sigma_{p, n}$. One group consists of $\mathrm{S}^{45}$ and $\mathrm{Ga}^{69}$ nuclei, and the other consists of $\mathrm{Ca}{ }^{48}, \mathrm{Y}^{89}$, $\mathrm{Th}^{232}$ with smaller values of $\sigma_{p, p n} / \sigma_{p, n}$. Such a difference is due, most likely, to the fact that the previously made assumption $/ 1 /$ on the equal number of neutrons available for the reactions ( $p, p n$ ) and ( $p, n$ ) is justifiable only in the first approximation. Indeed, taking into account the contribution of the reaction ( $\mathrm{p}, 2 \mathrm{p}$ ), it can be seen from Table 2 that $\sigma_{p, n}$ from $\mathrm{Sc}{ }^{45}$ to Ca a changes considerably sharper, than $\quad \sigma_{p, p n}$. This may be accounted for the fact that a smaller number of neutrons is. available for the reaction ( $p, n$ ), namely, only neutrons of the highest level completely or partially populated. It is natural that in future this assumption should be checked experimentally.

### 4.4 Mechanism of the reaction ( $p, n$ ).

It is natural to think that the mechanism of the reaction ( $p, n$ ) consists in scattering at a large angle of the incident proton on the neutron of the target nucleus. The neutron leaves the nucleus carrying away a larger fraction of energy and the proton is captured by the nucleus.

By assuming that this mechanism is valid the energy dependence of the cross-section of the reaction ( $p, n$ ) should be analogous to the energy dependence of the differential cross-section of elementary n-p scattering at angles corresponding to the scattering-particle energy $\leq 8 \mathrm{MeV}$ (in the laboratory system). It should be noted that the change of the upper energy limit of the scattering particle from 8 to 10 MeV influences upon the absolute value of the differential cross-section ( $\sim 10 \%$ ) and does not affect practically the character of energy dependence.
*
Fig. 4 shows the energy dependence of the differential cross-section of $n$-p scattering calculated in the above way by the data of ${ }^{17-20 /}$. Also the relative values of $\sigma_{p, n}$ for $\mathrm{Sc}^{45}$ and $\mathrm{Ca}{ }^{48}$ are given. For the convenience of comparison all the data are normalized to unity with $E_{p}=300 \mathrm{MeV}$. It is seen that at $\mathrm{E}_{p} \geqslant 300 \mathrm{MeV}$ the energy dependence of the differential cross section of $n-p$ scattering and that of the cross section of the reaction ( $p, n$ ), in fact coincide. A certain spread of points for $\mathrm{C}_{\mathrm{a}}{ }^{48}$ can be accounted for, evidently, by experimental difficulties in observing the reaction ( $p, n$ ). Thus, from the analysis of Fig. 4 one may arrive at the conclusion that the reaction ( $p, n$ ) may proceed direct interaction beginning from $E_{p}=300 \mathrm{MeV}$.

The dependence of the isomeric cross-section ratios upon the incident proton energy is shown in Fig. 5. From $\mathrm{E}_{p} \approx 200 \mathrm{MeV}$ the ratio $\sigma_{g} / \sigma_{\mathrm{m}}$ becomes constant. Its average value in the energy range $200-670 \mathrm{MeV}$ is $220 \pm 0.01$. This value is consistent with the value 2.1 obtained by Remsberg $/ 12 /$ for $\mathrm{E}_{p}=370 \mathrm{MeV}$. At the same time the total cross-section of the reaction $\mathrm{Sc}^{45}$ ( $\mathrm{p}, \mathrm{pn}$ ) according to his data amounts to ( $34.5 \pm 1.6$ ) mb, while according to our results at this proton energy the production cross-section of only $\mathrm{Sc}^{448}$ is about 33 mb . The reasons of such a divergence are not clear.

The isomeric cross-section ratio in the reaction ( $\mathrm{p}, \mathrm{pn}$ ) can be calculated by assuming the mechanism of direct neutron knock-on as it has been done by Porile and Tanaka $/ 11$ /. The calculation scheme is as follows. As a result of neutron knock-on from the levels $1 \mathrm{f}_{7 / 2}, 1 \mathrm{~d}_{3 / 2}, 2 \mathrm{~s}_{1 / 2} \quad$ (avallable for the reaction) of $\mathrm{Sc}^{45} \quad(7 / 2)$ a set of states is formed with the angular momenta $j$, ranging from $\left|\frac{2}{2}-j_{1}\right| \quad$ to $\frac{7}{2}+j_{2}$ and the relative weights proportional to $(2 j+1)$. Here $j_{i}$ is the angular momentum of the ejected neutron. The de-excitation of these states takes place as a cascade of $\gamma$-rays.

Further consideration of the process is performed in the manner of Huizenga and Vandenbosch $/ 21 /$. It is suggested that $y$-radiation is of adipole character and the branching ratio of the transition from the state with spin $\mathfrak{j}$ to state with spin $j_{f}=(j-1), j,(j+1)$ is given by the expression:

$$
P_{\left(j_{f}\right)} \approx\left(2 \mathrm{i}_{f}+1\right) \exp \left[-\left(\mathrm{j}_{f}+1 / 2\right)^{2} / 2 \quad \sigma^{2}[]\right.
$$

The average number of $\gamma$-rays emitted per cascade in the case of ( $n, \gamma$ ) -reactions is equal to $3-4$. It may be expected that multiplicity of $\gamma$-rays in neutron knocking- on in the reaction ( $\mathrm{p}, \mathrm{pn}$ ) is not larger than the above number. Various spin states of the residual nucleus produced as a result of gamma-ray emission enter either into isomeric or ground states of $\mathrm{Sc}^{44}$ depending on which transition requires smaller spin change. Thus, the states with spin $j_{j} \geq 6$ give rise to the production of $\mathrm{Sc}^{44 \mathrm{~m}}(7+)$, the states with spin $j_{j} \leq 4$ give rise to the production of $\mathrm{Sc}^{448}\left(3^{+}\right)$, and the state with $j_{s}=5$ is distributed between them equally.

Taking into account different contributions of the neutron levels available for the reaction, one may write the expression for the isomeric cross-section ratio in the following form:


[^0]The results of calculation for various values of the parameter $\sigma$, and for various $\gamma$-ray multiplicity are listed in Table 3. It is easily seen that the experimental value $\sigma_{\mathrm{g}} / \sigma_{\mathrm{m}}$ agrees best of all with calculation when the value of the parameter $\sigma$ is close to 4 . The assumption on the $\gamma$-ray multiplicity influences weakly upon $\sigma_{a} / \sigma_{m}$

The value of the parameter $\sigma$ may be estimated also theoretically by the formula, suggested by Bloch $/ 22 /$ :
where

| $\sigma(0)$ | is the value of the parameter with zero excitation energy; |
| :--- | :--- |
| $\mathrm{g}_{n, \alpha}$ | is the number of nucleons in the given state; |
| $\mathrm{m}_{a}$ | is the set of constants characterizing the projection of the nucleon angular momentum |
|  | in the given state; |

a
is obtained from the condition that $e^{a}$ should be equal to the ratio of the number of nucleons at the highest level (for the given nucleus) to the number of the remaining vacancies at the same level.

The summation refers only to the upper totally or partially populated level.

Table 3

| Levels and the number of emitted $y$-rays | Parameter ${ }^{\text {d }}$ |  |  |
| :---: | :---: | :---: | :---: |
|  | 3 | 4 | 5 |
| $\begin{aligned} & 1 \mathrm{f}_{7 / 2} \\ & 1 \mathrm{~d}_{3 / 2} \\ & 2 \mathrm{~s}_{1 / 2} \end{aligned} \quad \mathrm{~N}_{\gamma}=2$ | 2.75 | 2.07 | 1.82 |
| $\begin{aligned} & 1 \mathrm{f}_{Y / 2} \\ & 1 \mathrm{~d}_{s / 2} \\ & 2 \mathrm{~s}_{1 / 2} \end{aligned} \quad N_{V}=3$ | 3.16 | 2.10 | 1.74 |
| $\begin{array}{ll} 1 f_{7 / 2} & \\ l d_{3 / 2} & \mathrm{~N}_{y}=4 \\ 2 \mathrm{~s}_{1 / 2} & \ddots \\ \hline \end{array}$ | 3.57 | 2.13 | 1.69 |
| $\begin{array}{ll} \mathrm{lf}_{y / 2} & { }^{\mathrm{N}}=2=2 \\ \mathrm{ld}_{3 / 2} & \mathrm{~N}_{\mathrm{y}}=3 \\ 2 \mathrm{~s}_{\mathrm{y} / 2} & \\ \hline \end{array}$ | 2.74 | 1.98 | 1.70 |
| $\begin{array}{ll} 1 \mathrm{f}_{7 / 2} & \mathrm{~N}_{v}=3 \\ 1 \mathrm{~d}_{\mathrm{s} / 2} & \mathrm{~N}_{\gamma=4} \\ 2 \mathrm{~s}_{1 / 2} & { }_{2}=4 \end{array}$ | 3.16 | 2.04 | 1.66 |

The values of the sum $\Sigma_{\alpha} \quad g_{n, \alpha}$ m $_{\alpha}^{2} \quad$ up to the values which are of interest to us are given in Table 4 for two cases. In the left hand side they are given without spin-orbital interaction being taken into account and for the total number of nucleons $/ 22 /$. In the right hand side they are given for one sort of nucleons with the account of the spinorbital interaction. In the latter case $\sigma^{2}(0)$ has the form of the sum of similar items referring to neutrons an protons, respectively. The configuration of external nucleons $S c^{45}$ can be presented as ( $\left.1 f\right)^{5}$ for the first case and as

Table 4

| States | 1 s | $1 p$ | $1{ }^{1}$ | 2 s | 17 | ${ }_{1} \mathrm{~s} / 2$ | $1 p_{3 / 2}$ | $1 p_{1 / 2}$ | ${ }_{1 d_{s / 2}}$ | ${ }_{20}{ }_{3}$ | ${ }_{1 d}$ | $1 f_{212}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\Sigma_{a} \mathcal{E}_{n, \alpha}$ | 4 | 12 | 20 | 4 | 28 | 2 | 4 | 2 | 6 | 2 | 4 | 8 |
| $\Sigma_{a} B_{n, a} n_{\alpha}^{2}$ | I | II | 45 | I | II9 | I/2 | 10/2 | I/2 | 35/2 | I/2 | 10/2 | 84/2 |

$\mathrm{P}\left(\mathrm{lf}_{7 / 2}\right)^{\text {and }} \mathrm{n}\left(\mathrm{lf}_{7 / 2}\right)^{4}$ for the second case. The calculated values of the parameter $\quad \sigma \quad$ amount to 4,2 and 3,9 respectively. It is seen that the consideration of the spin-orbital interaction allows to obtain perfect agreement of the calculation value with the experimental data.

It appears to be of interest to check the applicability of comparatively simple presentations which form the basis of the formula for $\sigma^{2(0)} \quad / 22 /$ for other nuclei as well, in particular for heavier ones.

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Fig. 1. $\dot{D}_{\text {ecay }}$ scheme of $\mathrm{Sc}^{\mathbf{4 4}}$.


Fig. 2 Excitation functions of the reactions $\mathrm{Sc}^{\mathbf{4 5}}$ ( $\mathrm{p}, \mathrm{pn}$ ) and $\mathrm{Sc}^{\mathbf{4 5}}$ ( $\mathrm{p}, \mathrm{n}$ ).


Fig. 3 The dependence of the ratio $\sigma_{p, p n} / \sigma_{p, n}$ upon the energy of incident protons. Crosses correspond to $\mathrm{Sc}^{45}$ (the present paper), open circles to $\mathrm{Ca}^{48} / 1 /$,
 $\mathrm{Th}^{232 / 15,16 / .}$


Fig. 4. Energy dependence of the differential cross-section of n-p scattering and $\sigma_{\dot{p}, n}$. The solid curve correspond to the differential cross-section of $n-p$ scattering at large angles ( see the text), crosses to $\sigma_{p, n}$ for $S_{c}{ }^{45}$, open circles to $\sigma_{p, n}$ for $\mathrm{Ca}^{48}$


Fig.5. Dependence of the ratio of $\mathrm{Sc}^{44 \mathrm{~g}}$ and $\mathrm{Sc}^{44 \mathrm{~m}}$ production cross-section upon incident proton energy.


[^0]:    *Here $\sigma$ is a known parameter entering into the expression for nualearlevel density,
    Both this parameter and the cross seotions of nuclear reaotions are denoted by $\sigma$, what is so customary, that we considered it possible not to change them.

